

Time : 01:00:00 Hrs

Total Marks : 50

Section-A

- 1) Which of the following is an algebraic identity? 1
 (a) $(x + y)^2 = x^2 - 2xy + y^2$ (b) $(x + y)^2 = x^2 + 2xy - y^2$ (c) $(x + y)^2 = x^2 + 2xy + y^2$
 (d) $(x + y)^2 = -x^2 + 2xy + y^2$
- 2) The number 0 is called a 1
 (a) zero polynomial (b) binomial (c) trinomial (d) linear polynomial
- 3) Which of the following is a polynomial? 1
 (a) $x^2 + x + \frac{3}{x^2}$ (b) $\sqrt{x} + 5$ (c) $x^{3/4} - 7x + 4$ (d) $\frac{3}{2}x^3 - \frac{4}{3}x^2 + 2x - 1$
- 4) $y + \frac{1}{y}$ is: 1
 (a) polynomial of degree 1 (b) polynomial of degree 2 (c) polynomial of degree 3 (d) Not a polynomial
- 5) The degree of the polynomial $p(x)=3$ is: 1
 (a) 3 (b) 1 (c) 0 (d) 2
- 6) Degree of polynomial $(x^3 + 5)(4 - x^5)$ is: 1
 (a) 0 (b) 5 (c) 3 (d) 2
- 7) What is remainder when $x^3 - 2x^2 + x + 1$ is divided by $(x-1)$? 1
 (a) 0 (b) -1 (c) 1 (d) 2
- 8) $(x+2)$ is a factor of $2x^3 + 5x^2 - x - k$. The value of k is: 1
 (a) 6 (b) -24 (c) -6 (d) 24
- 9) If $2(a^2 + b^2) = (a + b)^2$ then 1
 (a) $a=2b$ (b) $b=2a$ (c) $a=b$ (d) $a+b=0$
- 10) If $x + \frac{1}{x} = 4$ then the value of $x^2 + \frac{1}{x^2}$ is: 1
 (a) 18 (b) 14 (c) 16 (d) 20

Section-B

- 11) $1 + x^2 + x^4 - x - x^3$ 2
- 12) $2x^3 - 7x + x^2 + 3x^4$ 2
- 13) $\frac{x}{2} - \frac{x^2}{3} + \frac{x^3}{4}$ 2
- 14) $2 - y^2 - y^3 + 2y^8$ 2
- 15) Check whether the polynomial $q(t) = 4t^3 + 4t^2 - t - 1$ is divided by $x+1$ 2
- 16) Polynomials $kx^3 + 3x^2 - 3$ and $2x^3 - 5x + k$, when divided by $(x-4)$ leave the same remainder in each case. Find the value of k . 2
- 17) If $x^3 - 5x^2 - px + 25 = (x - 4)q(x)$ then what is the value of p ? 2
- 18) If $x^2 - 3x + 2$ is a factor of the polynomial $x^4 - ax^3 + b$ then find the values of a and b . 2
- 19) Factorise: $x^3 - 3x^2 - 9x - 5$ 2

20) Factorise: $16x^3 - 2y^3$

2

Section-C

21) $5y^2 - 3y + 2$

5

22) The polynomial $p(x) = 2x^3 - 3x^2 + ax - 3a + 9$ when divided by $x+1$, leaves the remainder 16. Find the value of a. Also, find the remainder when $p(x)$ is divided by $x+2$.

5

23) Evaluate 105×93 without multiplying directly.

5

24) Prove that $(a + b)^3 + (b + c)^3 + (c + a)^3 - 3(a + b)(b + c)(c + a) = 2(a^3 + b^3 + c^3 - 3abc)$

5

Section-A

1) (c) $(x + y)^2 = x^2 + 2xy + y^2$

1

2) (a) zero polynomial

1

3) (d) $\frac{3}{2}x^3 - \frac{4}{3}x^2 + 2x - 1$

1

4) (d) Not a polynomial

1

5) (c) 0

1

6) (b) 5

1

7) (c) 1

1

8) (a) 6

1

9) (c) $a=b$

1

10) (b) 14

1

Section-B

11) -1

2

12) 2

2

13) $\frac{1}{4}$

2

14) 8

2

15) Yes

2

16) 1

2

17) 2

2

18) $a = \frac{15}{7}, b = \frac{8}{7}$

2

19) $(x+1)(x+1)(x-5)$

2

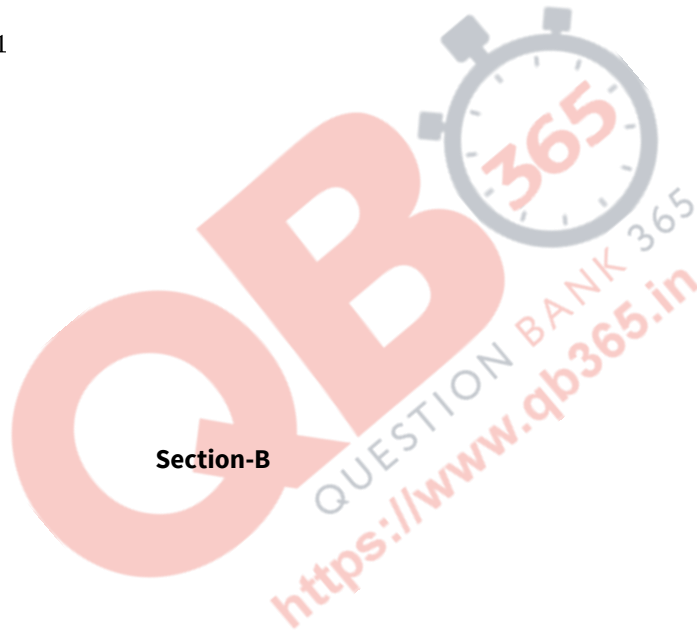
20) $2(2x - y)(4x^2 + 2xy + y^2)$

2

Section-C

21) 5, -3, 2

5



$$22) p(x) = 2x^3 - 3x^2 + ax - 3a + 9$$

5

By remainder theorem,

$$p(-1) = 16 \quad | \quad x + 1 = 0 \Rightarrow x = -1$$

$$\Rightarrow 2(-1)^3 - 3(-1)^2 + a(-1) - 3a + 9 = 16$$

$$\Rightarrow -2 - 3 - a - 3a + 9 = 16$$

$$\Rightarrow 4a = -12$$

$$\Rightarrow a = -3$$

$$\therefore p(x) = 2x^3 - 3x^2 - 3x - 3 \times (-3) + 9$$

$$= 2x^3 - 3x^2 - 3x + 18$$

\therefore Remainder when $p(x)$ is divided by $x+2 = p(-2)$

| By remainder theorem: $x + 2 = 0 \Rightarrow x = -2$

$$= 2(-2)^3 - 3(-2)^2 - 3(-2) + 18$$

$$= -16 - 12 + 6 + 18 = -4$$

$$23) 105 \times 93$$

5

$$=(100+5) \times (100+7)$$

$$=(100+5) \times \{100+(-7)\}$$

$$=(100)^2 + \{5+(-7)\}(100) + (5)(-7) \quad | \text{ Using Identity IV}$$

$$=10000-200-35=9765$$

$$24)$$

5

$$\text{L.H.S} = (a+b)^3 + (b+c)^3 + (c+a)^3 - 3(a+b)(b+c)(c+a)$$

$$= \{(a+b) + (b+c) + (c+a)\} [(a+b)^2 + (b+c)^2 + (c+a)^2 - (a+b)(b+c) - (b+c)(c+a) - (c+a)(a+b)]$$

$$= 2(a+b+c)[a^2 + 2ab + b^2 + b^2 + 2bc + c^2 + c^2 + 2ca + c^2 - ab - ac - b^2 - bc - bc - ba - c^2 - ca - ca - cb - a^2 - ab]$$

| Using Identity I

$$= 2(a+b+c)(a^2 + b^2 + c^2 - ab - bc - ca)$$

$$= 2(a^3 + b^3 + c^3 - 3abc) \quad | \text{ Using Identity VIII}$$

