

# 11th Standard -Physics

## Mechanical Properties of Solids

### Inter molecular Force

In a solid, atoms and molecules are arranged in such a way that each molecule is acted upon by the forces due to the neighbouring molecules. These forces are known as inter molecular forces.

- **Elasticity**

The property of the body to regain its original configuration (length, volume or shape) when the deforming forces are removed, is called elasticity.

- The change in the shape or size of a body when external forces act on it is determined by the forces between its atoms or molecules. These short range atomic forces are called elastic forces.

- **Perfectly elastic body**

A body which regains its original configuration immediately and completely after the removal of deforming force from it, is called perfectly elastic body. Quartz and phosphor bronze are the examples of nearly perfectly elastic bodies.

- **Plasticity**

The inability of a body to return to its original size and shape even on removal of the deforming force is called plasticity and such a body is called a plastic body.

• **Stress**

Stress is defined as the ratio of the internal force  $F$ , produced when the substance is deformed, to the area  $A$  over which this force acts. In equilibrium, this force is equal in magnitude to the externally applied force. In other words,

$$\text{Stress} = \frac{F}{A}$$

The SI unit of stress is newton per square metre ( $\text{Nm}^{-2}$ ). In CGS units, stress is  $\text{me cm}^{-2}$ . Dimensional formula of stress is  $[\text{ML}^{-1}\text{T}^{-2}]$ .

• **Stress is of two types:**

(i) Normal stress: It is defined as the restoring force per unit area perpendicular to the surface of the body. Normal stress is of two types: tensile stress and compressive stress.

(ii) Tangential stress: When the elastic restoring force or deforming force acts parallel to the surface area, the stress is called tangential stress.

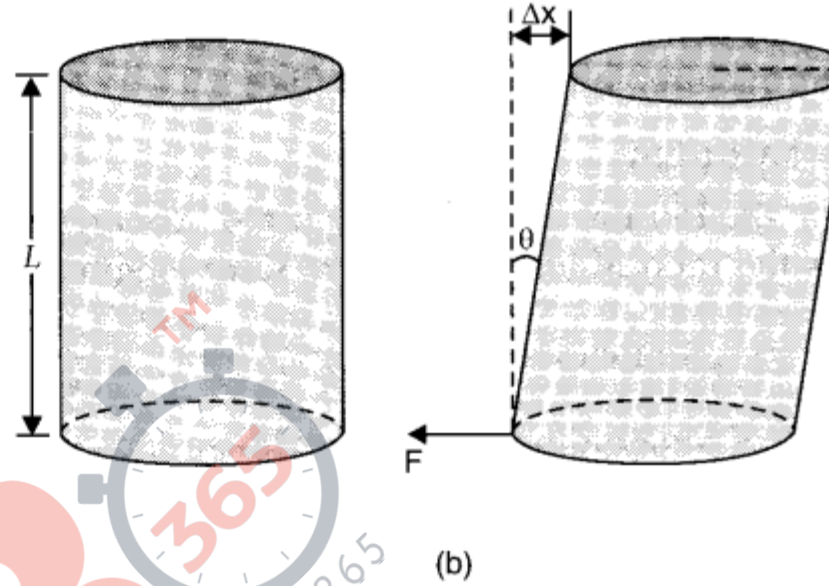
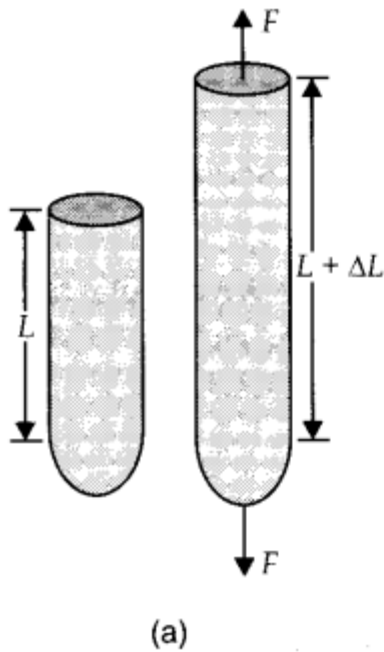
• **Strain**

It is defined as the ratio of the change in size or shape to the original size or shape. It has no dimensions, it is just a number.

**Strain is of three types:**

(i) Longitudinal strain: If the deforming force produces a change in length alone, the strain produced in the body is called longitudinal strain or tensile strain. It is given as:

$$\text{Longitudinal strain} = \frac{\text{Change in length } (\Delta l)}{\text{Original length } (l)}$$



(ii) Volumetric strain: If the deforming force produces a change in volume alone, the strain produced in the body is called volumetric strain. It is given as:

$$\text{Volumetric strain} = \frac{\text{Change in volume } (\Delta V)}{\text{Original volume } (V)}$$

(iii) Shear strain: The angle tilt caused in the body due to tangential stress expressed is called shear strain. It is given as:

$$\text{Shear strain} = \theta = \frac{\Delta L}{L}$$

- The maximum stress to which the body can regain its original status on the removal of the deforming force is called elastic limit.

## Hooke's Law

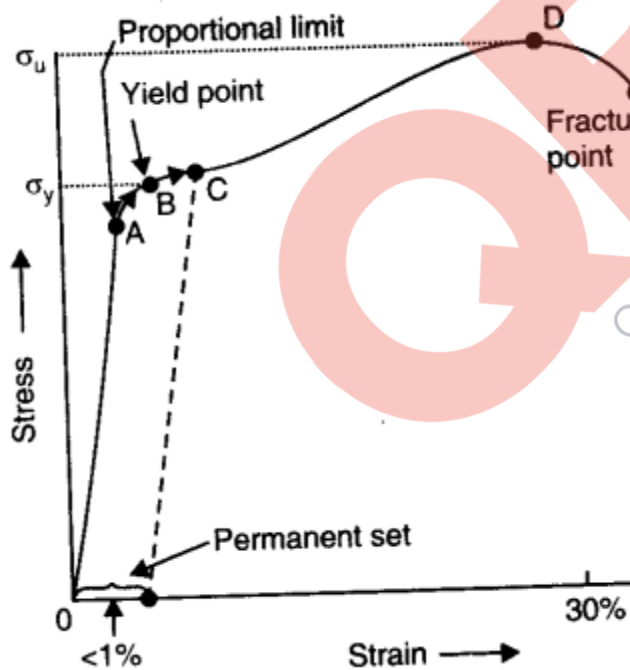
Hooke's law states that, within elastic limits, the ratio of stress to the corresponding strain produced is a constant. This constant is called the modulus of elasticity. Thus

$$\text{Modulus of elasticity} = \frac{\text{Stress}}{\text{Strain}}$$

Since strain is a pure number, the units of this constant are the same as those of stress,  $\text{Nm}^{-2}$ .

### • Stress Strain Curve

Stress strain curves are useful to understand the tensile strength of a given material. The given figure shows a stress-strain curve of a given metal.



- The curve from 0 to A is linear. In this region Hooke's Proportional limit law is obeyed.
- In the region from A to C stress and strain are not proportional. Still, the body regains its original dimension, once the load is removed.

- Point B in the curve is yield point or elastic limit and the corresponding stress is known as yield strength of the material.
- The curve beyond B shows the region of plastic deformation.
- The point D on the curve shows the tensile strength of the material. Beyond this point, additional strain leads to fracture, in the given material.

### • Young's Modulus

For a solid, in the form of a wire or a thin rod, Young's modulus of elasticity within elastic limit is defined as the ratio of longitudinal stress to longitudinal strain. It is given as:

$$\text{Young's modulus, } Y = \frac{F/A}{\Delta l/l} = \frac{Fl}{A \cdot \Delta l} = \frac{mgl}{\pi r^2 \cdot \Delta l}$$

It has the unit of longitudinal stress and dimensions of  $[ML^{-1}T^{-2}]$ . Its unit is Pas

### • Bulk Modulus

Within elastic limit the bulk modulus is defined as the ratio of longitudinal stress and volumetric strain. It is given as:

$$\text{Bulk modulus, } B = \frac{F/A}{\Delta V/V} = -\frac{P}{\Delta V/V}$$

- ve indicates that the volume variation and pressure variation always negate each other.

- Reciprocal of bulk modulus is commonly referred to as the "compressibility". It is defined as the fractional change in volume per unit change in pressure.

### • Shear Modulus or Modulus of Rigidity

It is defined as the ratio of the tangential stress to the shear strain.

Modulus of rigidity is given by

$$\eta = \frac{\text{Tangential stress}}{\text{Shear strain}} = \frac{F/A}{\theta}$$

### • Poisson's Ratio

The ratio of change in diameter ( $\Delta D$ ) to the original diameter ( $D$ ) is called lateral strain. The ratio of change in length ( $\Delta l$ ) to the original length ( $l$ ) is called longitudinal strain. The ratio of lateral strain to the longitudinal strain is called Poisson's ratio.

$$\sigma = \frac{\text{Lateral strain}}{\text{Longitudinal strain}} = \frac{\Delta D/D}{\Delta l/l}$$

For most of the substances, the value of  $\sigma$  lies between 0.2 to 0.4. When a body is perfectly incompressible, the value of  $\sigma$  is maximum and equals to 0.5.

### • Elastic Fatigue

It is the property of an elastic body by virtue of which its behaviour becomes less elastic under the action of repeated alternating deforming forces.

#### • Relations between Elastic Moduli

For isotropic materials (i.e., materials having the same properties in all directions), only two of the three elastic constants are independent. For example, Young's modulus can be expressed in terms of the bulk and shear moduli.

$$\frac{3}{Y} = \frac{1}{\eta} + \frac{1}{3B}$$

$$\text{Also, } Y = 3B(1 - \sigma) = 2\eta(1 + \sigma)$$

$$\begin{aligned}
 W &= \frac{YA}{L} \left[ \frac{1}{2} l^2 \right]_0^l \\
 &= \frac{YA}{L} \left[ \frac{1}{2} l^2 \right] \\
 &= \frac{1}{2} \left( \frac{YAl}{L} \right) \cdot l \\
 &= \frac{1}{2} \cdot F \cdot l
 \end{aligned}$$

Which equal to the elastic potential energy  $U$ .

$$\therefore U = \frac{1}{2} F \cdot l = \frac{1}{2} \times \text{Force} \times \text{extension}$$

Now the potential energy per unit volume is

$$\begin{aligned}
 \Rightarrow \frac{1}{2} \frac{F \cdot l}{V} &= \frac{1}{2} \left( \frac{YAl}{L} \right) \cdot \frac{l}{V} \\
 \frac{1}{2} \times \frac{Fl}{AL} &= \frac{1}{2} \left( \frac{YAl}{L} \right) \cdot \frac{l}{AL} && [V = AL] \\
 &= \frac{1}{2} \left( \frac{Yl}{L} \right) \cdot \frac{l}{L} \\
 &= \frac{1}{2} \left( \frac{F}{A} \right) \cdot \frac{l}{L} \\
 &= \frac{1}{2} \times \text{Stress} \times \text{Strain}
 \end{aligned}$$

Hence, the elastic potential energy of a wire (energy density) is equal to half the product of its stress and strain.

• IMPORTANT TABLES

TABLE 9.1 Young's moduli, elastic limit and tensile strengths of some materials.

Substance	Young's modulus $10^9\text{N/m}^2$	Elastic limit $10^7\text{N/m}^2$	Tensile strength $10^7\text{N/m}^2$
	$\sigma_y$	%	$\sigma_u$
Aluminium	70	18	20
Copper	120	20	40
Iron (wrought)	190	17	33
Steel	200	30	50
Bone			
(Tensile)	16		12
(Compressive)	9		12

TABLE 9.2 Shear moduli (G) of some common materials

Material	$G(10^9 \text{ Nm}^{-2} \text{ or GPa})$
Aluminium	25
Brass	36
Copper	42
Glass	23
Iron	70
Lead	5.6
Nickel	77
Steel	84
Tungsten	150
Wood	10



TABLE 9.3 Bulk moduli (B) of some common Materials

<i>Material Solids</i>	<i>B(10<sup>9</sup> Nm<sup>-2</sup> or GPa)</i>
Aluminium	72
Brass	61
Copper	140
Glass	37
Iron	100
Nickel	260
Steel	160
<b>Liquids</b>	
Water	2.2
Ethanol	0.9
Carbon disulphide	1.56
Glycerine	4.76
Mercury	25
<b>Gases</b>	
Air (at STP)	$1.0 \times 10^{-4}$