## CBSE Board Paper Solution-2020

| Class | $: \mathbf{X}$ |
| :--- | :--- |
| Subject | $:$ Mathematics (Standard) - |
|  | Theory |

## General instructions:

Read the following instructions very carefully and strictly follow them:
(i) This question paper comprises four sections - A, B, C and $D$. This question paper carries 40 question All questions are compulsory
(ii) Section A: Question Numbers 1 to 20 comprises of 20 question of one mark each.
(iii) Section B: Question Numbers 21 to 26 comprises of 6 question of two marks each.
(iv) Section C: Question Numbers 27 to 34 comprises of 8 question of three marks each.
(v) Section D: Question Numbers 35 to 40 comprises of 6 question of four marks each.
(vi) There is no overall choice in the question paper. However, an internal choice has been provided in 2 question of the mark, 2 question of one mark, 2 questions of two marks. 3 question of three marks
and 3 question of four marks. You have to attempt only one of the choices in such questions.
(vii) In addition to this. Separate instructions are given with each section and question, wherever necessary.
(viii) Use of calculations is not permitted.

## Section A

Question numbers 1 to 20 carry 1 mark each.
Question numbers 1 to 10 are multiple choice questions.
Choose the correct option.

1. On dividing a polynomial $p(x)$ by $x^{2}-4$, quotient and remainder are found to be $x$ and 3 respectively. The polynomial $p(x)$ is
(A) $3 x^{2}+x-12$
(B) $x^{3}-4 x+3$
(C) $x^{2}+3 x-4$
(D) $x^{2}-4 x-3$

## Answer:

Correct Answer: (B) $x^{3}-4 x+3$

## Explanation:

$$
\begin{aligned}
P(x) & =(\text { divisor }) \times(\text { quotient })+\text { Remainder } \\
& =\left(x^{2}-4\right) x+3 \\
& =x^{3}-4 x+3
\end{aligned}
$$

2) In Figure-1, ABC is an isosceles triangle, rightangled at $\mathbf{C}$. Therefore
(A) $A B^{2}=2 A C^{2}$
(B) $B C^{2}=2 A B^{2}$
(C) $A C^{2}=2 A B^{2}$
(D) $A B^{2}=4 A C^{2}$


Figure-1

## Answer:

## Correct Answer: (A) $A B B^{2}=2 A C^{2}$

## Explanation:

Given that ACB is an isosceles triangle right angled at C.

Therefore, $A C=B C$
Using Pythagoras theorem in the given triangle, we have

$$
\begin{aligned}
A B^{2} & =A C^{2}+B C^{2} \\
& =A C^{2}+A C^{2} \\
& =2 A C^{2}
\end{aligned}
$$

3) The point on the $x$-axis which is equidistant from ( $-4,0$ ) and 10,0 ) is
(A) $(7,0)$
(B) $(5,0)$
(C) $(0,0)$
(D) $(3,0)$

## OR

The centre of a circle whose end points of a diameter are $(-6,3)$ and 6,4$)$ is
(A) $(8,-1)$
(B) $(4,7)$
(C) $\left(0, \frac{7}{2}\right)$
(D) $\left(4, \frac{7}{2}\right)$

## Answer:

## Correct Answer: (D) $(3,0)$

## Explanation:

The required point and the given points as well lie on the x -axis.
The required point $(x, 0)$ is the mid-point of the line joining points $(-4,0)$ and $(10,0)$.

So,

$$
\begin{aligned}
x & =(-4+10) / 2 \\
& =6 / 2 \\
& =3
\end{aligned}
$$

Required point $=(x, 0)$

$$
=(3,0)
$$

## OR

## Correct Answer: (C) (0, 7/2)

## Explanation:

The centre of a circle is the mid-point of its diameter.
End points of the diameter are: $(-6,3)$ and $(6,4)$
Coordinates of the centre $=((-6+6) / 2,(3+4) / 2)$

$$
=(0,7 / 2)
$$

4) The value(s) of $k$ for which the quadratic equation $2 x^{2}+k x+2=0$ has equal roots, is
(A) 4
(B) $\pm 4$
(C) -4
(D) 0

## Answer:

Correct Answer: (B) $\pm 4$

## Explanation:

The given equation is:
$2 x^{2}+k x+2=0$
Discriminant $=b^{2}-4 a c$
Here, $b=k, a=2$, and $c=2$
So, Discriminant $=k^{2}-4 \times 2 \times 2$

$$
=k^{2}-16
$$

A quadratic equation has equal roots if its discriminant is zero.

$$
k^{2}-16=0
$$

$$
\begin{aligned}
& \mathrm{k}^{2}=16 \\
& \mathrm{k}= \pm 4
\end{aligned}
$$

5) Which of the following is not an A.P.?
(A) - 1.2, 0.8, $2.8 \ldots$
(B) $3,3+\sqrt{2}, 3+2 \sqrt{2}, 3+3 \sqrt{2}, \ldots$
(C) $\frac{4}{3}, \frac{7}{3}, \frac{9}{3}, \frac{12}{3}, \ldots$
(D) $\frac{-1}{5}, \frac{-2}{5}, \frac{-3}{5}, \ldots$

## Answer:

Correct Answer: (C) $\frac{4}{3}, \frac{7}{3}, \frac{9}{3}, \frac{12}{3}, \ldots$

## Explanation:

$$
\begin{gathered}
\frac{4}{3}, \frac{7}{3}, \frac{9}{3}, \frac{12}{3}, \ldots \\
\begin{aligned}
& \frac{7}{3}-\frac{4}{3}=\frac{7-4}{3} \\
&=\frac{3}{3} \\
&=1 \\
& \frac{9}{3}-\frac{7}{3}=\frac{9-7}{3} \\
&= \frac{2}{3} \\
& \Rightarrow \quad \frac{3}{3} \neq \frac{2}{3}
\end{aligned}
\end{gathered}
$$

Difference between consecutive terms is not same. So, this is not an A.P.
6) The pair of linear equations
$\frac{3 x}{2}+\frac{5 y}{3}=7$ and $9 x+10 y=14$ is
(A) consistent
(B) inconsistent
(C) consistent with one solution
(D) consistent with many solutions

## Answer:

Correct Answer: (B) Inconsistent Explanation:
$\frac{3 x}{2}+\frac{5 y}{3}=7$
$\frac{9 x+10 y}{6}=7$
$9 x+10 y=42 \quad \ldots(1)$
$9 x+10 y=14 \quad \ldots(2)$
Ratios of coefficients of $x$ and that of $y$ are
$\frac{9}{9}=\frac{10}{10}=\frac{1}{1}$
Ratio of constants $=\frac{42}{14}=\frac{3}{1} \neq \frac{1}{1}$
Ratios of coefficients of $x$ and $y$ are equal but they are not equal to the ratio of constants.
So, the given equations represent a paif of parallel lines and so they do not have a common solution.
7) In Figure-2 $P Q$ is tangent to the circle with centre at $O$, at the point $B$. If $\angle A O B=100^{\circ}$, then $\angle A B P$ is equal to
(A) $50^{\circ}$
(B) $40^{\circ}$
(C) $60^{\circ}$
(D) $80^{\circ}$


Figure-2

## Answer:

Correct Answer: (A) 50º Explanation:
$O A=O B$ (radii)
So, $\angle O A B=\angle O B A$

$$
\begin{aligned}
& =\left(180^{\circ}-100^{\circ}\right) / 2 \\
& =40^{\circ}
\end{aligned}
$$

Now, a radius of a circle meets a tangent at $90^{\circ}$.
So, $\angle A B P=\angle O B P-\angle O B A$

$$
=90^{\circ}-40^{\circ}=50^{\circ}
$$

8) The radius of a sphere (in cm ) whose volume is $12 \pi \mathrm{~cm}^{3}$, is
(A) 3
(B) $3 \sqrt{3}$
(C) $3^{2 / 3}$
(D) $3^{1 / 3}$

## Answer:

## Correct Answer: (C)32/3

## Explanation:

$$
\begin{aligned}
& \text { Volume of sphere }
\end{aligned} \begin{aligned}
& \frac{4}{3} \pi r^{3} \\
12 \pi & =\frac{4}{3} \pi r^{3} \\
r^{3} & =3^{2} \\
r & =3^{2 / 3}
\end{aligned}
$$

9) The distance between the points ( $m,-n$ ) and $(-m, n)$ is
(A) $\sqrt{m^{2}+n^{2}}$
(B) $m+n$
(C) $2 \sqrt{m^{2}+n^{2}}$
(D) $\sqrt{2 m^{2}+2 n^{2}}$

## Answer:

Correct Answer: (C) $2 \sqrt{\mathrm{~m}^{2}+\mathrm{n}^{2}}$
Explanation:

$$
\begin{aligned}
\text { Distance } & =\sqrt{m-(-m)^{2}+(-n-n)^{2}} \\
& =\sqrt{(m+m)^{2}+(-2 n)^{2}} \\
& =2 \sqrt{m^{2}+n^{2}}
\end{aligned}
$$

## 10) In Figure-3. From an external point $P$, two

 tangents $P Q$ and $P R$ are drawn to a circle of radius $4 \mathbf{c m}$ with centre 0 . If $\angle Q P R=90^{\circ}$, then length of $P Q$ is(A) 3 cm
(B) 4 cm
(C) 2 cm
(D) $2 \sqrt{2} \mathrm{~cm}$


Figure-3

## Answer:

Correct Answer: (B) 4 cm

## Explanation:

Tangents are drawn from an external point $P$.
So, line joining centre $O$ and point $P$ bisects $\angle P Q R$.
OP bisects $\angle \mathrm{QPR}=90^{\circ}$.
In $\triangle$ OQP,
$\angle \mathrm{Q}=90^{\circ}$ (radius meets tangent at $90^{\circ}$ )
$\angle \mathrm{QPO}=45^{\circ}=\angle \mathrm{QOP}$

Thus, $\mathrm{OQ}=\mathrm{PQ}=4 \mathrm{~cm}$

Fill in the blanks in question number 11 to 15
11) The probability of an event that is sure to happen is $\qquad$

## Answer: 1

12) Simplest form of $\frac{1+\tan ^{2} A}{1+\cot }$ $\qquad$ .

## Answer:

$\cot ^{2} \mathrm{~A}$
$\frac{1+\tan ^{2} A}{1+\cot ^{2} A}=\frac{\sec ^{2} A}{\operatorname{cosec}^{2} A}=\frac{\sin ^{2} A}{\cos ^{2} A}=\cot ^{2} A$
13) $A O B C$ is a rectangle whose three vertices are $A(0,-3), O(0,0)$ and $B(4,0)$. The length of its diagonal is $\qquad$

## Answer:

In right-angled triangle $A O B$,
$A B=\sqrt{O A^{2}+O B^{2}}=\sqrt{3^{2}+4^{2}}=\sqrt{25}=5$

14) In the formula $\bar{x}=a+\left(\frac{\sum f_{i} u_{i}}{\sum f_{i}}\right) \times h, u_{i}=$

Answer:
$\frac{x_{i}-a}{h}$
15) All concentric circles are $\qquad$ to each other.

Answer: similar

Answer the following question numbers 16 to 20.
16) Find the sum of the first $\mathbf{1 0 0}$ natural numbers.

## Answer:

$1+2+3+\ldots .100$ is an A. P.
Here first term $a=1$
Common difference $d=1$
Sum of $n$ terms of an A.P. $=\frac{n}{2}[2 a+(n-1) d]$
The sum of first 100 natural numbers

$$
\begin{aligned}
& =\frac{100}{2}[2 \times 1+(100-1) \times 1] \\
& =\frac{100(101)}{2} \\
& =50 \times 101 \\
& =5050
\end{aligned}
$$

17) In Figure-4 the angle of elevation of the top of a tower from a point $C$ on the ground, which is

30 m away from the foot of the tower, is $30^{\circ}$.
Find the height of the tower.


Figure-4

## Answer:

$\tan 30^{\circ}=\frac{A B}{30}$
$\frac{1}{\sqrt{3}}=\frac{A B}{30}$
$A B=\frac{30}{\sqrt{3}}=10 \sqrt{3}$
So, the height of the tower is $10 \sqrt{3} \mathrm{~m}$.
18) The LCM of two numbers is 182 and their HCF is 13. If one of the numbers is 26 , Find the other.

## Answer:

LCM $\times$ HCF $=$ Pr oduct of the two numbers
$182 \times 13=26 \times x$
$\mathrm{x}=\frac{182 \times 13}{26}=91$
So, the other number is 91 .
19) Form a quadratic polynomial, the sum and product of whose zeroes are (-3) and 2 respectively.

## OR

Can ( $x^{2}-1$ ) be a remainder while dividing
$x^{4}-3 x^{2}+5 x-9$ by $\left(x^{2}+3\right)$ ? Justify your answer with reasons.

## Answer:

$x^{2}-$ (sum of zeroes) $x+$ product of zeroes
$=x^{2}-(-3) x+2$
$=x^{2}+3 x+2$
So, the required polynomial is $x^{2}+3 x+2$.

## OR

When a polynomial $p(x)$ is divided by another polynomial $g(x)$, then the degree of remainder $r(x)<$ degree of $g(x)$
Therefore, for the given question $x^{2}-1$ cannot be a remainder while dividing $x^{4}-3 x^{2}+5 x-9$ by $x^{2}+3$ because $\operatorname{deg}\left(x^{2}-1\right)=\operatorname{deg}\left(x^{2}+3\right)$.

## 20) Evaluate:

$$
\frac{2 \tan 45^{\circ} \times \cos 60^{\circ}}{\sin 30^{\circ}}
$$

## Answer:

$\frac{2 \tan 45^{\circ} \times \cos 60^{\circ}}{\sin 30^{\circ}}$
$=\frac{2 \times 1 \times \frac{1}{2}}{\frac{1}{2}}$
$=2$

## SECTION B

Question number 21 to 26 carry 2 marks each.
21) In the given Figure-5, DE \|AC and DF||AE. Prove that $\frac{B F}{F E}=\frac{B E}{E C}$.


Answer:

In $\triangle A B C, D E \| A C$
So, using basic proportionality theorem, we get

$$
\begin{equation*}
\frac{B D}{D A}=\frac{B E}{E C} \tag{1}
\end{equation*}
$$

In $\triangle B A E, D F \| A E$
So, using basic proportionality theorem, we get

$$
\begin{equation*}
\frac{B D}{D A}=\frac{B F}{F E} \tag{2}
\end{equation*}
$$

From (1) and (2), we get

$$
\frac{B E}{E C}=\frac{B F}{F E}
$$

## 22) Show that $5+2 \sqrt{7}$ is an irrational number,

 where $\sqrt{7}$ is given to be an irrational number. ORCheck whether $12^{\mathrm{n}}$ can end with the digit 0 for any natural number $n$.

## Answer:

Let us assume, to the contrary, that $5+2 \sqrt{7}$ is rational. That is, we can find coprime $a$ and $b(b \neq 0)$ such that $5+2 \sqrt{7}=\frac{a}{b}$
$\therefore 2 \sqrt{7}=\frac{a}{b}-5$
Rearranging this equation, we get $\sqrt{7}=\frac{1}{2}\left(\frac{a}{b}-5\right)=\frac{a-5 b}{2 b}$

Since, $a$ and $b$ are integers, we get $\frac{a-5 b}{2 b}$ is rational, and so $\sqrt{7}$ is a rational.
But this contradicts the fact that $\sqrt{7}$ is irrational.
This contradiction has arisen because of our incorrect assumption that $5+2 \sqrt{7}$ is rational.
So, we conclude that $5+2 \sqrt{7}$ is irrational.

## OR

If the number $12^{n}$, for any $n$, were to end with the digit zero, then it would be divisible by 5 .
That is, the prime factorisation of $12^{n}$ would contain the prime 5 . This is not possible
$\because 12^{n}=(2 \times 2 \times 3)^{n}$
So, the prime numbers in the factorisation of $12^{n}$ are 2 and 3 .
So, the uniqueness of the Fundamental Theorem of Arithmetic guarantees that there are no other primes in the factorisation of $12^{n}$.
So, there is no natural number n for which $12^{n}$ ends with the digit zero.
23) If $A, B$ and $C$ are interior angles of a $\angle A B C$, then show that

$$
\cos \left(\frac{B+C}{2}\right)=\sin \frac{A}{2}
$$

## Answer:

Given that $A, B$ and $C$ are interior angles of a triangle $A B C$.
$\therefore \quad A+B+C=180^{\circ}$
or $A=180^{\circ}-B-C$
Now,

$$
\begin{aligned}
\cos \left(\frac{B+C}{2}\right) & =\sin \left(90^{\circ}-\frac{B+C}{2}\right) \\
& =\sin \left(\frac{180^{\circ}-B-C}{2}\right) \\
& =\sin \left(\frac{A}{2}\right)
\end{aligned}
$$

## 24) In Figure 6, a quadrilateral $A B C D$ is drawn to circumscribe a circle.

## Prove that

 $A B+C D=B C+A D$.

Figure-6

## OR

In Figure-7, find the perimeter of $\angle A B C$, if $A P$
$=12 \mathrm{~cm}$.


Figure-7

## Answer:



We have to prove that

$$
A B+C D=B C+A D
$$

We know that lengths of tangents drawn from a point to a circle are equal.
Therefore, from figure, we have

$$
D R=D S, C R=C Q, A S=A P, B P=B Q
$$

Now,

$$
\begin{aligned}
\mathrm{LHS}=\mathrm{AB}+\mathrm{CD} & =(\mathrm{AP}+\mathrm{BP})+(\mathrm{CR}+\mathrm{DR}) \\
& =(A S+B Q)+(C Q+D S) \\
& =B Q+C Q+A S+D S \\
& =B C+A D \\
& =R H S
\end{aligned}
$$

## OR



Figure- 7
From the given figure, we have $A P=12 \mathrm{~cm}$
Since $A Q$ and $A B$ are the tangent to the circle from a common point $A$, hence $A P=A Q=12$

Similarly, $\mathrm{PB}=\mathrm{BD}$ and $\mathrm{CD}=\mathrm{CQ}$
Also, $A P=A B+P B$ and $A Q=A C+C Q$

$$
\begin{aligned}
\text { Perimeter of } A B C= & A B+B D+C D+A C \\
= & A B+P B+C Q+A C \\
& (\text { since } P B=B M \text { and } C M=C Q) \\
= & (A B+P B)+(C Q+A C) \\
= & A P+A Q \\
= & 12+12 \\
= & 24 \mathrm{~cm}
\end{aligned}
$$

Therefore, the perimeter of triangle $A B C=24 \mathrm{~cm}$

## 25) Find the mode of the following distribution:

| Marks | $\mathbf{0 - 1 0}$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number <br> of <br> Students | 4 | 6 | 7 | 12 | 3 | 6 |

## Answer:

| Marks | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of <br> Students | 4 | 6 | 7 | 12 | 5 | 6 |

From the given data, we have
$l=30, f_{1}=12, f_{0}=7, f_{2}=5, h=10$
Mode $=I+\left(\frac{f_{1}-f_{0}}{2 f_{1}-f_{0}-f_{2}}\right) \times h$
$=30+\left(\frac{12-7}{2 \times 12-7-5}\right) \times 10$
$=34.1667$
$\therefore$ Mode of the given data is 34.1667 .
26) $\mathbf{2}$ cubes, each of volume $125 \mathrm{~cm}^{3}$, are joined end to end. Find the surface area of the resulting cuboid.

## Answer:

Let the side of the old cube $=a$
The volume of the old cube $=125 \mathrm{~cm}^{3}$ (Given)
The volume of the cube $=a^{3}$
$\mathrm{a}^{3}=125 \mathrm{~cm}^{3}$
$a^{3}=5^{3}$
$\mathrm{a}=5 \mathrm{~cm}$
The dimensions of the resulting cuboid are:
Length, $\mathrm{I}=10 \mathrm{~cm}$
Breadth, b $=5 \mathrm{~cm}$
Height, $h=5 \mathrm{~cm}$
Total surface area of the resulting cuboid:

$$
\begin{aligned}
& =2(\mathrm{lb}+\mathrm{bh}+\mathrm{hl}) \\
& =2[10(5)+5(5)+5(10)] \\
& =2[50+25+50] \\
& =2[125] \\
& =250 \mathrm{~cm}^{2}
\end{aligned}
$$

## Section C

27) A fraction becomes $\frac{1}{3}$ when 1 is subtracted from the numerator and it becomes $\frac{1}{4}$ when 8 is added to its denominator. Find the fraction.

## OR

The present age of a father is three years more than three times the age of his son. Three years

## hence the father's age will be 10 years more than twice the age of the son. Determine their present ages.

## Answer:

Let the numerator of the fraction be $x$ and denominator be $y$.
Therefore, the fraction is $\frac{x}{y}$.
According to question,

$$
\frac{x-1}{y}=\frac{1}{3}
$$

$3 x-1=y$

$$
\begin{equation*}
3 x-3=y \tag{1}
\end{equation*}
$$

and $\frac{x}{y+8}=\frac{1}{4}$

$$
4 x=y+8
$$

$$
4 x-8=y
$$

From equations 1 and 2 , we get

$$
3 x-3=4 x-8
$$

$4 x-3 x=8-3$

$$
x=5
$$

Putting $x=5$ in equation (1),

$$
\begin{aligned}
3 \times 5-3 & =y \\
y & =12
\end{aligned}
$$

So, the required fraction $=\frac{5}{12}$.

Let the son's present age be $x$.
So, father's present age $=3 x+3$
3 years later:
Son's age $=x+3$
Father's age $=3 x+3+3=3 x+6$
But, according to the given condition,
3 years later father's age $=2 x+3+10$

$$
\begin{aligned}
& =2 x+6+10 \\
& =2 x+16
\end{aligned}
$$

So, we can write

$$
\begin{aligned}
3 x+6 & =2 x+16 \\
3 x-2 x & =16-6 \\
x & =10
\end{aligned}
$$

So, son's present age $=10$ years
and father's present age $=10 \times 3+3$
$=33$ years

## 28) Use Euclid Division Lemma to show that the square of any positive integer is either of the form $3 q$ or $3 q+1$ for some integer $q$.

## Answer:

Let $a$ be a positive integer and $b=3$.
By Euclid's Algorithm,
$a=3 m+r$ for some integer $m \geq 0$ and $0 \leq r<3$.
The possible remainders are 0,1 and 2 . Therefore, $a$ can be $3 m$ or $3 m+1$ or $3 m+2$.
Thus,

$$
\begin{aligned}
a^{2} & =9 m^{2} \text { or }(3 m+1)^{2} \text { or }(3 m+2)^{2} \\
& =9 m^{2} \text { or }\left(9 m^{2}+6 m+1\right) \text { or }\left(9 m^{2}+12 m+4\right) \\
& =3 \times\left(3 m^{2}\right) \text { or } 3\left(3 m^{2}+2 m\right)+1 \text { or } 3\left(3 m^{2}+4 m+1\right)+1 \\
& =3 k_{1} \text { or } 3 k_{2}+1 \text { or } 3 k_{3}+1
\end{aligned}
$$

where $k_{1}, k_{2}$ and $k_{3}$ are some positive integers.
Hence, square of any positive integer is either of the form $3 q$ or $3 q+1$ for some integer $q$.
29) Find the ratio in which $y$-axis divides the line segment joining the points $(6,-4)$ and $(-2,-7)$. Also find the point of intersection.

## OR

Show that the points ( $7,100,(-2,5)$ and (3, -4 ) are vertices of an isosceles right triangle.

## Answer:

Let the ratio in which the line segment joining $A(6,-4)$ and $B(-2,-7)$ is divided by the $y$-axis be $k: 1$.
Let the coordinate of point on $y$-axis be $(0, y)$.
Therefore,

$$
0=\frac{-2 k+6}{k+1} \quad \text { and } \quad y=\frac{-7 k-4}{k+1}
$$

Now,

$$
0=\frac{-2 k+6}{k+1}
$$

or $0=-2 k+6$
or $k=3$
Therefore, the required ratio is $3: 1$.
Also,

$$
\begin{aligned}
y & =\frac{-7 k-4}{k+1} \\
& =\frac{-7 \times 3-4}{3+1} \\
& =\frac{-25}{4}
\end{aligned}
$$

Therefore, the given line segment is divided by the point $\left(0, \frac{-25}{4}\right)$ in the ratio 3:1.

OR

Let the given points are $P(7,10), Q(-2,5)$ and $R(3,-4)$. Now, using distance formula we find distance between these points i.e., $P Q, Q R$ and $P R$.
Distance between points $P(7,10)$ and $Q(-2,5)$,

$$
\begin{aligned}
P Q & =\sqrt{(-2-7)^{2}+(5-10)^{2}} \\
& =\sqrt{81+25} \\
& =\sqrt{106}
\end{aligned}
$$

Distance between points $Q(-2,5)$ and $R(3,-4)$,

$$
\begin{aligned}
\mathrm{QR} & =\sqrt{(3+2)^{2}+(-4-5)^{2}} \\
& =\sqrt{25+81} \\
& =\sqrt{106}
\end{aligned}
$$

Distance between points $P(7,10)$ and $R(3,-4)$,

$$
\begin{aligned}
P R & =\sqrt{(3-7)^{2}+(-4-10)^{2}} \\
& =\sqrt{16+196} \\
& =\sqrt{212}
\end{aligned}
$$

Now,

$$
\begin{aligned}
\mathrm{PQ}^{2}+\mathrm{QR}^{2} & =106+106 \\
& =212=\mathrm{PR}^{2}
\end{aligned}
$$

i.e., $P Q^{2}+Q R^{2}=P R^{2}$

Therefore, points $P(5,-2), Q(6,4)$ and $R(7,-2)$ form an isosceles right triangle because sides PQ and QR are equal.

## 30) Prove that:

$$
\sqrt{\frac{1+\sin A}{1-\sin A}}=\sec A+\tan A
$$

## Answer:

$$
\begin{aligned}
\text { LHS } & =\sqrt{\frac{1+\sin A}{1-\sin A}} \\
& =\sqrt{\frac{1+\sin A}{1-\sin A}} \times \sqrt{\frac{1+\sin A}{1+\sin A}} \\
& =(1+\sin A) \sqrt{\frac{1}{1-\sin ^{2} A}} \\
& =\frac{1+\sin A}{\sqrt{\cos ^{2} A}} \\
& =\frac{1+\sin A}{\cos A} \\
& =\frac{\sin A}{\cos A}+\frac{1}{\cos A} \\
& =\tan A+\sec A=R H S
\end{aligned}
$$

31) For an A.P., it is given that the first term
(a) $=5$, common difference (d) $=3$, and the $n^{\text {th }}$ term $\left(a_{n}\right)=50$. Find $n$ and sum of first $n$ terms $\left(S_{n}\right)$ of the A.P.

## Answer:

Here, $a=5, d=3, a_{n}=50$
We need to find $S_{n}$.
Firstly, we will find the value of $n$.
We know that

$$
a_{n}=a+(n-1) d
$$

So, $\quad 50=5+(n-1) 3$
or $50-5=(n-1) 3$
or $\frac{45}{3}+1=n$
or $\quad \mathrm{n}=16$
We know that sum of first $n$ terms of an AP is given by

$$
\begin{aligned}
S_{n} & =\frac{n}{2}\left(+a_{n}\right) \\
\text { So, } \quad S_{16} & =\frac{16}{2}(+50) \\
& =8 \times 55 \\
\text { or } \quad S_{16} & =440
\end{aligned}
$$

32) Construct a $\triangle A B C$ with sides $B C=6 \mathrm{~cm}, A B=5$ $\mathbf{c m}$ and $\angle A B C=60^{\circ}$. Then construct a triangle whose sides are $\frac{3}{4}$ of the corresponding sides of $\triangle A B C$.

## OR

Draw a circle of radius 3.5 cm . Take a point $P$ outside the circle at a distance of 7 cm from the centre of the circle and construct a pair of tangents

## to the circle from that point.

## Answer:



## Steps of Construction:

Step 1: Draw a $\triangle A B C$ with sides $A B=5 \mathrm{~cm}, B C=6 \mathrm{~cm}$ and $\angle A B C=60^{\circ}$.
Step 2: Draw a ray $B X$ making an acute angle with line $B C$ on the opposite side of vertex A .
Step 3: Locate 4 points $B_{1}, B_{2}, B_{3}, B_{4}$ on $B X$ such that $B_{1}=B_{1} B_{2}=B_{2} B_{3}=B_{3} B_{4}$.
Step 4: Join the points $C$ and $B_{4}$.
Step 5: Through the point $\mathrm{B}_{3}$, draw a line parallel to $\mathrm{CB}_{4}$ intersecting line segment $B C$ at point $C^{\prime}$.
Step 6: Draw a line through $C^{\prime}$ parallel to the line $A C$ to intersect line segment $A B$ at $A^{\prime}$.
The required triangle is $\Delta \mathrm{A}^{\prime} \mathrm{BC}^{\prime}$.

## OR



Step 1: Draw a circle of radius 3.5 cm with centre at point 0 . Locate a point $P$, at a distance of 7 cm from $O$, and join $O$ and $P$.
Step 2: Bisect OP. Let $M$ be the mid-point of OP.
Step 3: Draw a circle with centre at M and MO as radius. Q and $R$ are points of intersections of this circle with the circle having centre at O.
Step 4: Join PQ and PR.
$P Q$ and $P R$ are the required tangents.
33) Read the following passage and answer the question given at the end:

## Diwali Fair.

A game in a booth at a Diwali Fair involves using a spinner first. Then, if the spinner stops on an
even number, the player is allowed to pick a marble from a bag. The spinner and the marbles in the bag are represented in Figure - 8.

Prizes are given when a black marble is picked. Shweta plays the game once.


Figure-8
(i) What is the probability that she will be allowed to pick a marble from the bag?
(ii) (ii) Suppose she is allowed to pick a marble from the bag, what is the probability of getting a prize, when it is given that the bag contains 20 balls out of which 6 are black?

## Answer:

Numbers on spinner $=1,2,4,6,8,10$
Even numbers on spinner $=2,4,6,8,10$
Shweta will pick black marble, if spinner stops on even number.
Therefore,

$$
\begin{aligned}
n(\text { Even number }) & =5 \\
n(\text { Possible number }) & =6
\end{aligned}
$$

(i) P (Shweta allowed to pick a marble)
$=P$ (Even number)
$=\frac{\mathrm{n} \text { (Even number })}{\mathrm{n}(\text { Possible number })}$
$=\frac{5}{6}$
Therefore, the probability of allowing Shweta
to pick a marble is $\frac{5}{6}$.
(ii) Since, prizes are given, when a black marble is picked.

Number of black marbles $=6$
Total number of marbles $=20$
Therefore, $\mathrm{P}($ getting a prize $)=\mathrm{P}($ a black marble $)$

$$
\begin{aligned}
& =\frac{n(\text { Black marbles })}{n(\text { Total marbles })} \\
& =\frac{6}{20}
\end{aligned}
$$

$$
=\frac{3}{10}
$$

Therefore, the probabiltiy of geting prize is $\frac{3}{10}$.
34. In figure - 9, a square $O P Q R$ is inscribed in a quadrant OAQB of a circle. If the radius of circle is $\mathbf{6} \sqrt{\mathbf{2}} \mathbf{~ c m}$, find the area of the shaded region.


Figure-9

## Answer:

Given that, $\mathrm{OQ}=6 \sqrt{2} \mathrm{~cm}$
$O P Q R$ is a square.
Let the side of square $=a$
The diagonal of square $=a \sqrt{2}$
Here, OQ is a diagonal of square.

$$
\begin{array}{lr}
\Rightarrow & a \sqrt{2}=6 \sqrt{2} \\
\Rightarrow & a=6 \mathrm{~cm}
\end{array}
$$

Area of square $O P Q R=6^{2}$

$$
=36 \mathrm{~cm}^{2}
$$

Radius of the quadrant $\mathrm{OAQB}=$ Diagonal of the square OPQR

$$
=6 \sqrt{2} \mathrm{~cm}
$$

Area of the quadrant $O A Q B=\frac{90^{\circ}}{360^{\circ}} \times \frac{22}{7} \times(6 \sqrt{2})^{2}$

$$
=\frac{396}{7} \mathrm{~cm}^{2}
$$

Area of shaded region $=$ Area of the quadrant $O A Q B$

- Area of square OPQR

$$
\begin{aligned}
& =\frac{396}{7}-36 \\
& =\frac{144}{7} \\
& =20.6 \mathrm{~cm}^{2}
\end{aligned}
$$

## SECTION D

Obtain other zeroes of the polynomial
35) $p(x)=2 x^{4}-x^{3}-11 x^{2}+5 x+5$
if two of its zeroes are $\sqrt{5}$ and $-\sqrt{5}$.
OR

## What minimum must be added to

$2 x^{3}-3 x^{2}+6 x+7$ so that resulting polynomial will be divisible by $x^{2}-4 x+8$ ?

## Answer:

The given polynomial is $p(x)=2 x^{4}-x^{3}-11 x^{2}+5 x+5$.
The two zeroes of $p(x)$ are $\sqrt{5}$ and $-\sqrt{5}$.
Therefore, $(x-\sqrt{5})$ and $(x+\sqrt{5})$ are factors of $p(x)$.
Also, $(x-\sqrt{5})(x+\sqrt{5})=x^{2}-5$
and so $x^{2}-5$ is a factor of $p(x)$.
Now,

$$
\begin{gathered}
x ^ { 2 } - 5 \longdiv { 2 x ^ { 4 } - x ^ { 3 } - 1 1 x ^ { 2 } + 5 x + 5 } \\
2 x^{4} \quad-10 x^{2} \\
-\quad+ \\
\hline-x^{3}-x^{2}+5 x+5 \\
-x^{3}+5 x \\
+\quad- \\
\hline \begin{array}{ll}
-x^{2} & +5 \\
-x^{2} & +5 \\
+ & - \\
+ & 0
\end{array}
\end{gathered}
$$

$$
\begin{aligned}
2 x^{4}-x^{3}-11 x^{2}+5 x+5 & =\left(x^{2}-5\right)\left(2 x^{2}-x-1\right) \\
& =\left(x^{2}-5\right)\left(2 x^{2}-2 x+x-1\right) \\
& =\left(x^{2}-5\right)(2 x+1)(x-1)
\end{aligned}
$$

Equating $\left(x^{2}-5\right)(2 x+1)(x-1)$ to zero, we get
the zeroes of the given polynomial.
Hence, the zeroes of the given polynomial are :

$$
\sqrt{5},-\sqrt{5},-\frac{1}{2} \text { and } 1
$$

The given polynomial is $2 x^{3}-3 x^{2}+6 x+7$.
Here, divisor is $x^{2}-4 x+8$
Divide $2 x^{3}-3 x^{2}+6 x+7$ by $x^{2}-4 x+8$ and find the remainder.

$$
\begin{array}{r}
x ^ { 2 } - 4 x + 8 \longdiv { 2 x ^ { 3 } - 3 x ^ { 2 } + 6 x + 7 } \\
2 x^{3}-8 x^{2}+16 x \\
\frac{-\quad-}{5 x^{2}-10 x+7} \\
\frac{5 x^{2}-20 x+40}{} \\
\frac{-\quad-}{10 x-33}
\end{array}
$$

Remainder $=10 \mathrm{x}-33$
Therefore, we should add $-(10 x-33)$ to make it exactly divisible by $x^{2}-4 x+8$.
Thus, we should add $-10 x+33$ to $2 x^{3}-3 x^{2}+6 x+7$.
36) Prove that the ratio of the areas of two similar triangles is equal to the square of the ratio of their corresponding sides.

## Answer:

Given : $\triangle \mathrm{ABC} \sim \triangle \mathrm{DEF}$
To prove: $\frac{\text { Area } \triangle A B C}{\text { Area } \triangle D E F}=\left(\frac{A B}{D E}\right)^{2}=\left(\frac{B C}{E F}\right)^{2}=\left(\frac{A C}{D E}\right)^{2}$
Construction: Draw $\mathrm{AL} \perp \mathrm{BC}$ and $\mathrm{DM} \perp \mathrm{EF}$


Proof: Here $\frac{\text { Area } \triangle A B C}{\text { Area } \triangle D E F}=\frac{\frac{1}{2} \times B C \times A L}{\frac{1}{2} \times E F \times D M}=\frac{B C \times A L}{E F \times D M}$
In $\triangle \mathrm{ALB}$ and $\triangle \mathrm{DME}$

$$
\angle \mathrm{ALB}=\angle \mathrm{DME} \quad \text { Each } 90^{\circ}
$$

and $\angle B=\angle E \quad$ Since $\triangle A B C \sim \triangle D E F$
So, $\triangle \mathrm{ALB} \sim \triangle \mathrm{DME} \quad \mathrm{AA}$ similarity criterion
$\Rightarrow \frac{A L}{D M}=\frac{A B}{D E}$
But $\frac{A B}{D E}=\frac{B C}{E F}=\frac{A C}{D F}$ since $\triangle A B C \sim \triangle D E F$
Therefore, $\frac{\mathrm{AL}}{\mathrm{DM}}=\frac{\mathrm{BC}}{\mathrm{EF}}$
From Oand We have

$$
\frac{\text { Area }(\mathrm{ABC})}{\text { Area }(\mathrm{DEF})}=\frac{\mathrm{BC}}{\mathrm{EF}} \times \frac{\mathrm{AL}}{\mathrm{DM}}=\frac{\mathrm{BC}}{\mathrm{EF}} \times \frac{\mathrm{BC}}{\mathrm{EF}}=\left(\frac{\mathrm{BC}}{\mathrm{EF}}\right)^{2}
$$

But $\frac{A B}{D E}=\frac{B C}{E F}=\frac{A C}{D F}$ Since $\triangle A B C \sim \triangle D E F$
This implies that,

$$
\frac{\text { Area } \triangle A B C}{\text { Area } \triangle D E F}=\left(\frac{A B}{D E}\right)^{2}=\left(\frac{B C}{E F}\right)^{2}=\left(\frac{A C}{D E}\right)^{2}
$$

## 37) Sum of the areas of two squares is $544 \mathrm{~m}^{\mathbf{2}}$. If the difference of their perimeters is $\mathbf{3 2} \mathbf{~ m}$, find the sides of the two squares.

## OR

## A motorboat whose speed is $18 \mathrm{~km} / \mathrm{h}$ in still water takes 1 hour more to go 24 km upstream than to return downstream to the same spot. Find the speed of the stream.

## Answer:

Let the sides of first and second square be $x$ any $y$. Then,
Area of first square $=x^{2}$
And,
Area of second square $=y^{2}$
According to the question,
$x^{2}+y^{2}=544$
Now,
Perimeter of first square $=4 x$
And,
Perimeter of second square $=4 y$

According to the question,
$4 x-4 y=32$
From equation (2), we get

$$
4(x-y)=32
$$

or, $\quad x-y=\frac{32}{4}$
or, $\quad x-y=8$
or, $\quad x=8+y$
Subsituting this value of $x$ in equation(1), we get

$$
x^{2}+y^{2}=544
$$

or,

$$
(8+y)^{2}+y^{2}=544
$$

$$
\text { or, } 64+y^{2}+16 y+y^{2}=544
$$

or, $\quad 2 y^{2}+16 y+64=544$
or, $2 y^{2}+16 y+64-544=0$
or, $\quad 2 y^{2}+16 y-480=0$
or, $\quad 2\left(y^{2}+8 y-240\right)=0$
or, $\quad y^{2}+8 y-240=0$
or, $\quad y^{2}+20 y-12 y-240=0$
or, $y(y+20)-12(y+20)=0$
or,

$$
(y+20)(y-12)=0
$$

$\Rightarrow y+20=0$ or $y-12=0$
$\Rightarrow y=-20$ or $y=12$
Since side of a square cannot be negative, therefore $y=12$.

Substituting $y=12$ in equation (3), we get
$x=8+y=8+12=20$
Therefore,
Side of first square $=x=20 \mathrm{~cm}$
And,
Side of second square $=y=12 \mathrm{~cm}$

## OR

Let the speed of the stream be $x \mathrm{~km} / \mathrm{h}$.
Therefore, speed of the boat upstream $=(18-x) \mathrm{km} / \mathrm{h}$ and the speed of the boat downstream $=(18+x) \mathrm{km} / \mathrm{h}$.
The time taken to go upstream $=\frac{\text { distance }}{\text { speed }}$

$$
=\frac{24}{18-x} \text { hours }
$$

Similarly, the time taken to go downstream $=\frac{24}{18+x}$ hours
According to the question,

$$
\begin{array}{rlrl} 
& & \frac{24}{18-x}-\frac{24}{18+x} & =1 \\
& & & \\
& \text { or, } & \frac{24(18+x)-24(18-x)}{(18+x)(18-x)} & =1 \\
& \text { or, } & 24(18+x)-24(18-x) & =(18+x)(18-x) \\
\text { or, } & 432+24 x-432+24 x & =324-x^{2} \\
\text { or, } & x^{2}+48 x-324 & =0
\end{array}
$$

Using the quadratic formula, we get

$$
\begin{aligned}
x & =\frac{-48 \pm \sqrt{48^{2}-4(1)(-324)}}{2} \\
& =\frac{-48 \pm \sqrt{2304+1296}}{2} \\
& =\frac{-48 \pm \sqrt{3600}}{2} \\
& =\frac{-48 \pm 60}{2}
\end{aligned}
$$

Therefore, $x=\frac{-48+60}{2}$ or $x=\frac{-48-60}{2}$
$\Rightarrow \quad x=\frac{12}{2}$ or $x=\frac{-108}{2}$
$\Rightarrow \quad x=6$ or $x=-54$

Since $x$ is the speed of the stream, it cannot be negative. So, we ignore the root $x=-54$. Therefore, $x=6$ gives the speed of the stream as $6 \mathrm{~km} / \mathrm{h}$.
38. A solid toy is in the form of a hemisphere surmounted by a right circular cone of same radius. The height of the cone is $\mathbf{1 0} \mathbf{~ c m}$ and the radius of the base is 7 cm . Determine the volume of the toy. Also find the area of the coloured sheet required to cover the toy.

$$
\text { (Use } \pi=\frac{22}{7} \text { and } \sqrt{149}=12.2 \text { ) }
$$

## Answer:



Let $A B C$ be the hemisphere and $A D C$ be the cone standing on the base of the hemisphere.
Height of the cone $\left(h_{1}\right)=10 \mathrm{~cm}$
(Given)
Radius of the cone $\left(r_{1}\right)=7 \mathrm{~cm}$
(Given)
Since the hemisphere is surmounted by the right circular cone of same radius, therefore

Radius of the hemisphere $\left(r_{2}\right)=7 \mathrm{~cm}$
So,
Volume of the toy
$=$ Volume of the cone + Volume of the hemisphere
$=\frac{1}{3} \pi r_{1}^{2} h_{1}+\frac{2}{3} \pi r_{2}^{3}$
$=\left[\left(\frac{1}{3} \times \frac{22}{7} \times 7 \times 7 \times 10\right)+\left(\frac{2}{3} \times \frac{22}{7} \times 7 \times 7 \times 7\right)\right] \mathrm{cm}^{3}$
$=\left[\frac{1540}{3}+\frac{2156}{3}\right] \mathrm{cm}^{3}$
$=\frac{3696}{3} \mathrm{~cm}^{3}$
$=1232 \mathrm{~cm}^{3}$

Area of the coloured sheet required to cover the toy
$=$ CSA of hemisphere + CSA of cone
$=2 \pi r_{2}^{2}+\pi r \ell$
Where $\ell$ is the slant height of the cone

$$
\begin{aligned}
\ell & =\sqrt{r_{1}^{2}+h_{1}^{2}} \\
& =\sqrt{7^{2}+10^{2}} \\
& =\sqrt{49+100} \\
& =\sqrt{149} \\
& =12.2 \mathrm{~cm}
\end{aligned}
$$

So,

Area of the coloured sheet required to cover the toy
$=\left[\left(2 \times \frac{22}{7} \times 7 \times 7\right)+\left(\frac{22}{7} \times 7 \times 12.2\right)\right] \mathrm{cm}^{2}$
$=(308+268.4) \mathrm{cm}^{2}$
$=576.4 \mathrm{~cm}^{2}$
39. A statue 1.6 m tall, stands on the top of a pedestal.

From a point on the ground, the angle of elevation of the top of the statue is $60^{\circ}$ and from the same point the angle of elevation of the top of the pedestal is $45^{\circ}$. Find the height of the pedestal.
(Use $\sqrt{\mathbf{3}}=1.73$ )
Answer:


Let BD be a pedestal of height $\times m$ and AD be a statue of height 1.6 m . The angle of elevation of the top of
pedestal from a point C is $45^{\circ}$ and that of point statue from $C$ is $60^{\circ}$.

In the triangle $A B C$ :

$$
\frac{\mathrm{AB}}{\mathrm{BC}}=\tan 60^{\circ}
$$

$\frac{1.6+x}{B C}=\sqrt{3}$
Or, $\quad B C=\frac{1.6+x}{\sqrt{3}}$
... 1
In the triangle DBC:

$$
\frac{D B}{B C}=\tan 45^{\circ}
$$

Or, $\frac{x}{B C}=1$
Or, $\quad x=B C$
By equations 1 and 2, we get

$$
x=\frac{1.6+x}{\sqrt{3}}
$$

Or, $\quad \sqrt{3} x=1.6+x$
$\sqrt{3}-1 x=1.6$

$$
\text { Or, } \quad \begin{aligned}
x & =\frac{1.6}{\sqrt{3}-1} \times \frac{\sqrt{3}+1}{\sqrt{3}+1} \\
& =\frac{1.61 .73+1}{3-1} \\
& =\frac{1.6 \times 2.73}{2} \\
& =2.184 \mathrm{~m}
\end{aligned}
$$

Therefore, the height of the pedestal is 2.184 m .
40) For the following data, draw a 'less than' ogive and hence find the median of the distribution.

| Age(in <br> years): | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number <br> of <br> persons: | 5 | 15 | 20 | 25 | 15 | 11 | 9 |

## OR

The distribution given below show the number of wickets taken by bowlers in one-day cricket matches. Find the mean and the median of the number of wickets taken.

| Number <br> of <br> wickets | $20-60$ | $60-100$ | $100-140$ | $140-180$ | $180-220$ | $220-260$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Number <br> of <br> bowlers: | 7 | 5 | 16 | 12 | 2 | 3 |

## Answer:

| Age | Number of Persons <br> (Cumulative frequency) |
| :--- | :--- |
| Less than 10 | 5 |
| Less than 20 | $5+15=20$ |
| Less than 30 | $20+20=40$ |
| Less than 40 | $40+25=65$ |
| Less than 50 | $65+15=80$ |
| Less than 60 | $80+11=91$ |
| Less than 70 | $91+9=100$ |


| Age | No. of Persons <br> (f) | Cumulative frequency <br> (cf) |
| :--- | :--- | :--- |
| $0-10$ | 5 | 5 |
| $10-20$ | 15 | 20 |
| $20-30$ | 20 | 40 |
| $30-40$ | 25 | 65 |
| $40-50$ | 15 | 80 |
| $50-60$ | 11 | 91 |
| $60-70$ | 9 | 100 |

Plot the points $(10,5),(20,20), \ldots,(70,100)$ on a graph paper.


| Class interval | No. of bowlers $\mathrm{f}_{\mathrm{i}}$ | Class mark $\mathrm{x}_{\mathrm{i}}$ | $\mathrm{f}_{\mathrm{i}} \mathrm{x}_{\mathrm{i}}$ |
| :---: | :---: | :---: | :---: |
| $20-60$ | 7 | 40 | 280 |
| $60-100$ | 5 | 80 | 400 |
| $100-140$ | 16 | 120 | 1920 |
| $140-180$ | 12 | 160 | 1920 |
| $180-220$ | 2 | 200 | 400 |
| $220-260$ | 3 | 240 | 720 |
| Total | $\sum \mathrm{f}_{\mathrm{i}}=45$ |  | $\sum \mathrm{f}_{\mathrm{i}} \mathrm{x}_{\mathrm{i}}=5640$ |

$\bar{x}=\frac{\sum \mathrm{f}_{\mathrm{i}} \mathrm{x}_{\mathrm{i}}}{\sum \mathrm{f}_{\mathrm{i}}}=\frac{5640}{45}=125.33$

| Number of <br> wickets | Number of bowlers | Cumulative <br> Frequency |
| :--- | :--- | :--- |
| $20-60$ | 7 | 7 |$|$| $60-100$ | 5 |
| :--- | :--- |
| $100-140$ | 16 |
| $140-180$ | 12 |
| $180-220$ | 2 |
| $220-260$ | 3 |$\quad$| 12 |
| :--- |

$\mathrm{n}=45$
$\Rightarrow \frac{\mathrm{n}}{2}=\frac{45}{2}=22.5$
Median class $=100-140$
Median $=1+\frac{\left(\frac{n}{2}-c f\right)}{f} \times h$
$\mathrm{I}=100, \frac{\mathrm{n}}{2}=22.5, \mathrm{cf}=12, \mathrm{f}=16, \mathrm{~h}=40$
Median $=100+\frac{22.5-12}{16} \times 40$
$=100+26.25$
$=126.25$

