Maths (Basic) Delhi (Set 3)

General Instructions:

(i) This guestion paper comprises four sections – A, B, C and D. This guestion paper carries 40 questions. All questions are compulsory:

(ii) Section A : Q. No. 1 to 20 comprises of 20 questions of one mark each.

(iii) Section B: Q. No. 21 to 26 comprises of 6 questions of two marks each.

(iv) Section C: Q. No. 27 to 34 comprises of 8 questions of three marks each.

(v) Section D: Q. No. 35 to 40 comprises of 6 questions of four marks each.

(vi) There is no overall choice in the guestion paper. However, an internal choice has been provided in 2 questions of one mark each, 2 questions of two marks each, 3 questions of three marks each and 3 questions of four marks each. You have to **attempt** only one of the choices in such questions.

(vii) In addition to this, separate instructions are given with each section and question, wherever necessary.

(viii) Use of calculators is not permitted.

Question: 1

The median and mode respectively of a frequency distribution are 26 and 29. Then its UESTION mean is

- (a) 27.5
- (b) 24.5
- (c) 28.4
- (d) 25.8

Solution:

The empirical relationship between mean, median and mode is

Mode = 3Median - 2Mean $\Rightarrow 2Mean = 3Median - Mode$ $\Rightarrow 2$ Mean = $3 \times 26 - 29$ \Rightarrow Mean = $\frac{49}{2}$ = 24.5 Hence, the correct answer is option (b)

Ouestion: 2

If the distance between the points A(4, p) and B(1, 0) is 5 units, then the value(s) of p is (are) (a) 4 only (b) -4 only

(d) 0

Solution:

The distance between the points A(4, p) and B(1, 0) is given by

$$\sqrt{(4-1)^2 + (p-0)^2}$$

$$= \sqrt{3^2 + p^2}$$

$$= \sqrt{9+p^2}$$
According to the question,

$$\sqrt{9+p^2} = 5$$

$$\Rightarrow 9+p^2 = 5^2$$

$$\Rightarrow p^2 = 25-9$$

$$\Rightarrow p = \pm \sqrt{16}$$

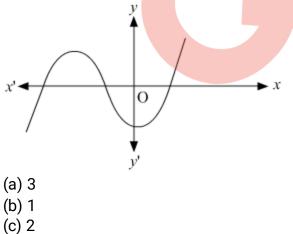
$$\Rightarrow p = \pm 4$$

Hence, the required answer is option (c).

Question: 3

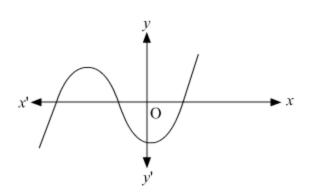
67 The graph of a polynomial is shown in figure, then the number of its zeroes is

BAT



(d) 4

Solution:



The number of zeroes is 3 as the graph of the polynomial cuts the x-axis at 3 points which means the value of y is zero at those points.

Hence, the correct answer is option (a).

Question: 4

2. 35 is

- (a) an integer
- (b) a rational number
- (c) an irrational number
- (d) a natural number

Solution:

- $2.\overline{35} = 2.35353535...$
- JESTION BANK $2.\overline{35}$ is a non-terminating repeating decimal.

And we know that every non-terminating repeating decimal is a rational number. Hence, the correct answer is option (b).

Question: 5

HCF of 144 and 198 is (a) 9 (b) 18 (c) 6 (d) 12

Solution:

Using Euclid's division algorithm, $198 = 144 \times 1 + 54$ $144 = 54 \times 2 + 36$ $54 = 36 \times 1 + 18$ $36 = 18 \times 2 + 0$ \Rightarrow HCF of 144 and 198 is 18. Hence, the correct answer is option (b).

Question: 6

The probability that a number selected at random from the numbers 1, 2, 3, ..., 15 is a multiple of 4 is

(a) 4/15

(b) 2/15

(c) 1/15

(d) 1/5

Solution:

The multiples of 4 from 1 to 15 are 4, 8 and 12.

QUESTION BAN Hence, the probability of selecting a multiple of four $=\frac{3}{15}$

Hence, the correct answer is option (c).

Ouestion: 7

225 can be expressed as (a) 5×3^2 (b) $5^2 \times 3$ (c) $5^2 \times 3^2$ (d) $5^3 \times 3$

Solution:

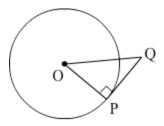
225 can be written as: $225=3\times3\times5\times5=3^2\times5^2$ Hence, the correct answer is option (c).

Ouestion: 8

QP is a tangent to a circle with centre O at a point P on the circle. If ΔOPQ is isosceles, then $\angle OQP$ equals.

- (a) 30°
- (b) 45°
- (c) 60°
- (d) 90°

Solution:



Given: PQ is a tangent to a circle with centre O such that $\triangle OPQ$ is isosceles.

The line joining the centre to the point of contact of a tangent to the circle is perpendicular to the tangent.

∴ ∠OPQ = 90°

One angle of $\triangle OPQ$ is a right angle and it is given that $\triangle OPQ$ is isosceles. Hence, the sides containing the right angle are equal sides. $\therefore OP = PQ$

As the angles opposite to two equal sides of a triangle are equal, we get $\angle OQP = \angle POQ$ QUESTION BANK

Applying the angle sum property in $\triangle OPQ$, we get

 $\angle OQP + \angle POQ + \angle OPQ = 180^{\circ}$ $\Rightarrow 2\angle OQP + 90^{\circ} = 180^{\circ}$ $\Rightarrow \angle OQP = 45^{\circ}$

Question: 9

If a and β are the zeroes of the polynomial $x^2 + 2x + 1$, then $1/a + a/\beta$ is equal to (a) -2

(b) 2

(C) 0

(d) 1

Solution:

The zeros of the polynomial $x^2 + 2x + 1$ are given to be α and β . We have, $\alpha + \beta = -\frac{2}{1} = -2$ and $\alpha\beta = \frac{1}{1} = 1$ Consider the given expression: $\frac{1}{\alpha} + \frac{1}{\beta}$ $= \frac{\alpha + \beta}{\alpha\beta}$ $= \frac{-2}{1}$ = -2Hence, the correct answer is option (a).

Question: 10

The coordinates of a point A on *y*-axis, at a distance of 4 units from *x*-axis and below it, are

- (a) (4, 0)
- (b) (0, 4)
- (c) (-4,0)
- (d) (0, -4)

Solution:

The coordinate of a point A on *y*-axis which is 4 units from *x*-axis and below it is (0,-4). Hence, the correct answer is option (d).

Question: 11

Fill in the blank.

If the equations kx - 2y = 3 and 3x + y = 5 represent two intersecting lines at unique point, then the value of k is _____.

OR

Fill in the blank. If quadratic equation $3x^2 - 4x + k = 0$ has equal roots, then the value of k is

Solution

Since the given equations represent two lines intersecting at a unique point, they've got a unique solution.

Therefore,

 $\begin{array}{l} \frac{a_1}{a_2} \neq \frac{b_1}{b_2} \\ \Rightarrow \frac{k}{3} \neq \frac{-2}{1} \\ \Rightarrow k \neq -6 \end{array}$

Hence, the given pair of linear equations in two variables will have a unique solution for all values of k except -6.

OR

Given that the quadratic equation $3x^2 - 4x + k$ has equal roots. $\Rightarrow D = 0$ $\Rightarrow b^2 - 4ac = 0$ where a = 3, b = -4, c = k $\Rightarrow (-4)^2 - 4 \times 3 \times k = 0$ $\Rightarrow 16 - 12k = 0$ $\Rightarrow 12k = 16$ $\Rightarrow k = \frac{4}{3}$ \Rightarrow The value of k is $\frac{4}{3}$ Question: 12 Fill in the blank. If tan (A + B) = $\sqrt{3}$ and tan (A - B) = $\frac{1}{\sqrt{3}}$, A > B, then the value of A is ______

Solution:

Given, $\tan (A + B) = \sqrt{3}$ and $\tan (A - B) = \frac{1}{\sqrt{3}}$ Therefore, $A + B = 60^{\circ}$ and $A - B = 30^{\circ}$ Adding the two equations, we get $2A = 90^{\circ}$ $\Rightarrow A = \frac{90^{\circ}}{2} = 45^{\circ}$

Question: 13

Fill in the blank.

The perimeters of two similar triangles are 25 cm and 15 cm respectively. If one side of the first triangle is 9 cm, then the corresponding side of second triangle is _____.

Solution:

We know that, the ratio of the perimeter of two similar triangles = ratio of their corresponding sides

$$\Rightarrow \frac{25}{15} = \frac{9}{x}$$
$$\Rightarrow x = \frac{9 \times 15}{25} = \frac{27}{5}$$
$$\Rightarrow x = 5.4$$

Hence, the corresponding side of the second triangle is 5.4 cm.

Question: 14

Fill in the blank.

If the point C(k, 4) divides the line segment joining two points A(2, 6) and B(5, 1) in ratio 2 : 3, the value of *k* is _____.

OR

Fill in the blank.

If points A(-3, 12), B(7, 6) and C(x, 9) are collinear, then the value of x is _____.

Solution:

Using the Section formula, we have

$$k = \frac{2 \times 5 + 3 \times 2}{2 + 3}$$
$$\Rightarrow k = \frac{10 + 6}{5}$$
$$\Rightarrow k = 3, 2$$

Using the Section formula, we have

$$k = \frac{2 \times 5 + 3 \times 2}{2 + 3}$$

$$\Rightarrow k = \frac{10 + 6}{5}$$

$$\Rightarrow k = 3.2$$
For collinear points, Area = 0.
i.e.

$$\frac{1}{2} |x_1 (y_2 - y_3) + x_2 (y_3 - y_1) + x_3 (y_1 - y_2)| = 0$$

$$|x_1 (y_2 - y_3) + x_2 (y_3 - y_1) + x_3 (y_1 - y_2)| = 0$$

$$|-3 (6 - 9) + 7 (9 - 12) + x (12 - 6)| = 0$$

$$|-3 (-3) + 7 (-3) + x (6)| = 0$$

$$|9 - 21 + 6x| = 0$$

$$|6x - 12| = 0$$

$$\Rightarrow 6x - 12 = 0$$

$$\Rightarrow 6x = 12$$

$$\Rightarrow x = 2$$
The value of x is 2.

Question: 15

If $\cot \theta = \frac{12}{5}$, then the value of $\sin \theta$ is _____.

Solution:

Given: $\cot \theta = \frac{12}{5}$ We know that $\csc^2 \theta - \cot^2 \theta = 1$ $\Rightarrow \csc^2 \theta = 1 + \cot^2 \theta$ $\Rightarrow \csc^2 \theta = 1 + \left(\frac{12}{5}\right)^2$ $\Rightarrow \csc^2 \theta = \left(\frac{13}{5}\right)^2$ $\Rightarrow \csc \theta = \frac{13}{5}$ $\Rightarrow \sin \theta = \frac{5}{13}$

Question: 16

The n^{th} term of an AP is (7 - 4n), then what is its common difference?

Solution:

Given: n^{th} term of an AP is (7 - 4n)Since n^{th} term of an AP is given by $T_n = a + (n - 1)d$, where a = First Term, d = Common Difference.

Therefore, we have 7-4n = a + (n-1)d $\Rightarrow 7-4n = (a-d) + nd$ Comparing both sides, we get d = -4Hence, the common difference is -4.

Question: 17

If $5\tan\theta = 3$, then what is the value of $\left(\frac{5\sin\theta - 3\cos\theta}{4\sin\theta + 3\cos\theta}\right)$?

Solution:

Given that $5 \tan \theta = 3$ $\Rightarrow \tan \theta = \frac{3}{5}$ $\Rightarrow \frac{\sin \theta}{\cos \theta} = \frac{3}{5}$ Let $\sin \theta = 3k$ and $\cos \theta = 5k$, where k is any integer.

Consider the given expression: $5 \sin \theta - 3 \cos \theta$ $4\sin\theta + 3\cos\theta$ $=\frac{5(3k)-3(5k)}{4(3k)+3(5k)}$ $=\frac{0}{27k}$

= 0

Question: 18

The areas of two circles are in the ratio 9:4, then what is the ratio of their BANK 365 circumferences?

Solution:

Given: Ratio of the areas of the two circle is 9:4. Let the areas of the the two circles be A_1 and A_2 . Hence, $\frac{A_1}{A_2} = \frac{9}{4}$ (1) Let the radii of the two circles be r_1 and r_2 . $\frac{\text{Area of the first circle}}{\text{Area of the second circle}} = \frac{\pi r_1^2}{\pi r_2^2}$ $\Rightarrow \frac{\pi r_1^2}{\pi r_2^2} = \frac{9}{4}$ [From (1)] $\Rightarrow \frac{r_1^2}{r_2^2} = \frac{9}{4}$ $\Rightarrow \frac{r_1}{r_2} = \frac{3}{2} \qquad \dots (2)$ Let the circumferences of the two circles be C_1 and C_2 . $\frac{C_1}{C_2} = \frac{2\pi r_1}{2\pi r_2}$ $\Rightarrow \frac{C_1}{C_2} = \frac{r_1}{r_2}$ $\Rightarrow \frac{C_1}{C_2} = \frac{3}{2}$ [From (2)]The ratio of their circumference is 3 : 2.

Ouestion: 19

If a pair of dice is thrown once, then what is the probability of getting a sum of 8?

Solution:

Total number of outcomes when two dices are thrown simultaneously is given by, Total outcomes $= 6 \times 6 = 36$ Favorable pair of outcomes for getting a sum of 8 is given by, (2, 6), (3, 5), (4, 4), (5, 3), (6, 2) \Rightarrow Total number of favourable outcomes = 5 Therefore. Required probability=Total number of favourable outcomes Total outcomes $=\frac{5}{36}$

Question: 20

The areas of two similar triangles ABC and PQR are 25 cm² and 49 cm² respectively. If QR = 9.8 cm, find BC. QUESTION BANK

Solution:

Given: \triangle ABC ~ \triangle PQR According to the property of similarity,

$$\therefore \frac{\operatorname{ar}(\triangle ABC)}{\operatorname{ar}(\triangle PQR)} = \left(\frac{BC}{QR}\right)^2$$
$$\Rightarrow \frac{25}{49} = \left(\frac{BC}{9.8}\right)^2$$
$$\Rightarrow \left(\frac{5}{7}\right)^2 = \left(\frac{BC}{9.8}\right)^2$$
$$\Rightarrow \frac{5}{7} = \frac{BC}{9.8}$$
$$\Rightarrow BC = \frac{5}{7} \times 9.8 = 7 \text{ cm}$$

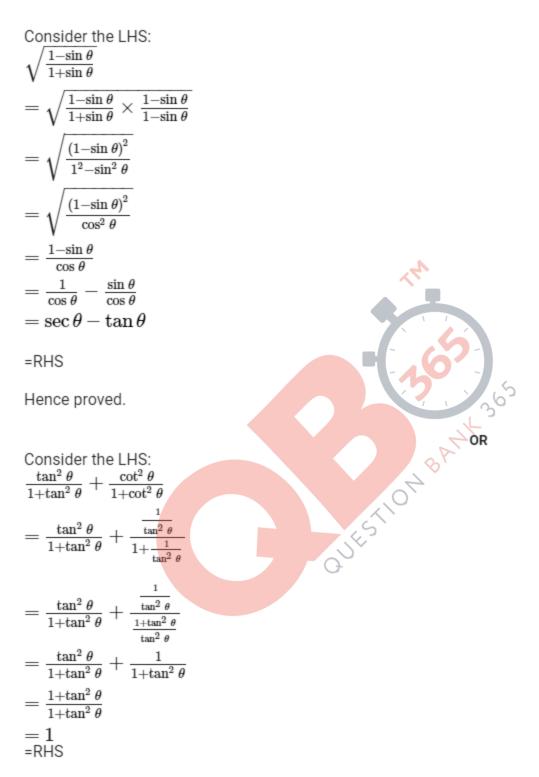
Question: 21

Prove that
$$\sqrt{rac{1-\sin heta}{1+\sin heta}}= {
m sec} heta-{
m tan} heta.$$

OR

Prove that
$$rac{ an^2 \ heta}{1+ an^2 \ heta} + rac{ an 2}{1+ an^2 \ heta} = 1$$

Solution:



Question: 22

Two different dice are thrown together, find the probability that the sum a of the numbers appeared is less than 5.

OR

Find the probability that 5 Sundays occur in the month of November of a randomly selected year.

Solution:

Two dices are thrown simultaneously. So, the total number of outcomes will be $6^2 = 36$.

Now, all the favorable pairs whose sum is less than 5 is given by (1, 1), (1, 2), (1, 3), (2, 3)1), (2, 2), (3, 1).

The total number of favorable outcomes is 6.

Hence, the required probability = 6/36 = 1/6.

OR

In any randomly selected year, the Month of November will have 30 days.

Now out of these 30 days, we will have 4 complete weeks (i.e. 28 days) having 4 Sundays.

For the remaining two days, we have the following possibilities: QUESTION

- (i) Saturday and Sunday,
- (ii) Sunday and Monday,
- (iii) Monday and Tuesday,
- (iv) Tuesday and Wednesday,
- (v) Wednesday and Thursday,
- (vi) Thursday and Friday,
- (vii) Friday and Saturday.

Thus, the possibility of having a 5th Sunday = 2/7.

Question: 23

A bag contains 5 red balls and some blue balls. If the probability of drawing a blue ball at random from the bag is three times that of a red ball, find the number of blue balls in the bag.

Solution:

Given, the number of red balls in the bag = 5Let the number of blue balls in the bag = x

Therefore, the total number of balls in the bag = x + 5

Let R and B denote the events of drawing a red ball and a blue ball respectively from the bag.

Then, according to the question, we have

$$P(B) = 3P(R)$$

$$\Rightarrow \frac{x}{x+5} = 3 \times \frac{5}{x+5}$$

$$\Rightarrow \frac{x}{x+5} = -\frac{15}{5}$$

$$\Rightarrow \frac{x}{x+5} = \frac{10}{x+5}$$

 $\Rightarrow x = 15$

Hence, the number of blue balls in the bag is 15.

Question: 24

The radii of two circles are 19 cm and 9 cm respectively. Find the radius New of a circle which has circumference equal to sum of their circumferences.

Solution:

The radii of two circles are given to be 19 cm and 9 cm respectively.

Let $r_1 = 19$ and $r_2 = 9$ The circumference of these two circles is given by $C_1 = 2\pi r_1 = 38\pi$ and $C_1 = 2\pi r_2 = 18\pi$

Let the radius of the new circle be *r* cm. Now, the circumference of the new circle is given by $C = C_1 + C_2 = 56\pi$ $\Rightarrow 2\pi r = 56\pi$ $\Rightarrow r = 28$ cm

Question: 25

Divide the polynomial $16x^2 + 24x + 15$ by (4x + 3) and write the quotient and the remainder.

Solution:

Division can be done as follows:

$$4x + 3 \overline{\smash{\big)}_{16x^2 + 24x + 15}}_{\underline{16x^2 + 12x}} \underline{12x + 15}_{\underline{12x + 15}} \underline{12x + 9}_{\underline{6}}$$

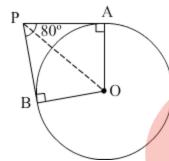
The quotient obtained is 4x + 3 and the remainder is 6.

Question: 26

If tangents PA and PB drawn from an external point P to a circle with centre O are inclined to each other at an angle of 80°, then find \angle POA.

Solution:

It is given that PA and PB are tangents.



Therefore, the radius drawn to these tangents will be perpendicular to the tangents. Thus, $OA \perp PA$ and $OB \perp PB$ $\Rightarrow \angle OBP = \angle OAP = 90^{\circ}$

ESTION

In AOBP,

Sum of all interior angles = 360° $\Rightarrow \angle OAP + \angle APB + \angle PBO + \angle BOA = 360^{\circ}$ $\Rightarrow 90^{\circ} + 80^{\circ} + 90^{\circ} + \angle BOA = 360^{\circ}$ $\Rightarrow \angle BOA = 100^{\circ}$

In $\triangle OPB$ and $\triangle OPA$, AP = BP (Tangents from a point) OA = OB (Radii of the circle) OP = OP (Common side)

Therefore, $\triangle OPB \cong \triangle OPA$ (SSS congruence criterion)Thus, $\angle POB = \angle POA$ (By CPCT)

 $\Rightarrow \angle POA = \frac{1}{2} \angle AOB = \frac{100^{\circ}}{2} = 50^{\circ}$

Question: 27

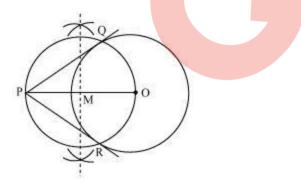
Draw a circle of radius 4 cm. From a point 7 cm away from the centre of circle. Construct a pair of tangents to the circle.

OR Draw a line segment of 6 cm and divide it in the ratio 3 : 2.

Solution:

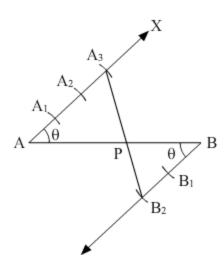
A pair of tangents to the given circle can be constructed as follows. **Step 1** Draw a circle of 4 cm radius and 0 as centre. Locate a point P, 7 cm away from 0. Join OP.

- Step 2 Bisect OP. Let M be the mid-point of PO.
- **Step 3** Taking M as centre and MO as radius, draw a circle.
- **Step 4** Let this circle intersect the previous circle at point Q and R.
- Step 5 Join PQ and PR. PQ and PR are the required tangents.



OR

We need to follow the following steps to construct the given



Step of construction

Step I- First of all we draw a line segment AB = 6 cm.

Step II- We draw a ray AX making an acute angle with AB.

Step III- Draw a ray BY parallel to AX by making an acute angle $\angle ABY = \angle BAX$.

Step IV- Mark three points A_1 , A_2 , A_3 on AX and two points B_1 , B_2 on BY in such a way that $AA_1 = A_1A_2 = A_2A_3 = BB_1 = B_1B_2$.

Step V- Join A₃B₂. This line intersects AB at a point P.

Thus, the given line segment AB has been divided internally in the ratio of 3:2

Question: 28

Prove that $(1 + \tan A - \sec A) \times (1 + \tan A + \sec A) = 2 \tan A$

OR

Prove that $\frac{\operatorname{cosec}\,\theta}{\operatorname{cosec}\,\theta-1} + \frac{\operatorname{cosec}\,\theta}{\operatorname{cosec}\,\theta+1} = 2 \sec^2 \theta$

Solution:

Consider the LHS:

$$(1 + \tan A - \sec A) (1 + \tan A + \sec A)$$

 $= [(1 + \tan A) - \sec A] [(1 + \tan A) + \sec A]$
 $= (1 + \tan A)^2 - \sec^2 A$
 $= 1 + 2 \tan A + \tan^2 A - \sec^2 A$
 $= 1 + 2 \tan A + (-1)$
 $= 2 \tan A$
=RHS

Hence proved.

LHS

$$= \frac{\cos ec\theta}{\csc e^{\theta} - 1} + \frac{\csc \theta}{\csc e^{\theta} + 1}$$

$$= \frac{\csc e^{\theta}(\csc e^{\theta} + 1) + \csc e^{\theta}(\csc e^{\theta} - 1)}{\csc e^{2} \theta - 1}$$

$$= \frac{2 \csc^{2} \theta + \csc e^{\theta} + \csc e^{\theta} - \csc e^{\theta}}{\csc e^{2} \theta - 1}$$

$$= \frac{2 \csc^{2} \theta}{\cot^{2} \theta} (\because \csc e^{2} \theta - 1 = \cot^{2} \theta)$$

$$= \frac{2}{\sin^{2} \theta} \times \frac{\sin^{2} \theta}{\cos^{2} \theta} (\because \csc e^{2} \theta = \frac{1}{\sin^{2} \theta} \text{ and } \cot^{2} \theta = \frac{\cos^{2} \theta}{\sin^{2} \theta})$$

$$= \frac{2}{\cos^{2} \theta}$$

$$= 2 \sec^{2} \theta (\because \sec^{2} \theta = \frac{1}{\cos^{2} \theta})$$

$$= \text{RHS}$$

Hence proved.

Question: 29

Given that $\sqrt{3}$ is an irrational number, show that $(5 + 2\sqrt{3})$ is an irrational number.

OR

An army contingent of 612 members is to march behind an army band of 48 members in a parade. The two groups are to march in the same number of columns. What is the maximum number of columns in which they can march?

Solution:

Given: $\sqrt{3}$ is an irrational number.

To prove: $5 + 2\sqrt{3}$ is an irrational number. Proof:

Suppose $5 + 2\sqrt{3}$ is a rational number.

Therefore it can be written in $\frac{p}{q}$ form, where p and q are coprime integers.

$$\Rightarrow 5 + 2\sqrt{3} = \frac{p}{q}$$
$$\Rightarrow 2\sqrt{3} = \frac{p}{q} - 5 = \frac{p - 5q}{q}$$
$$\Rightarrow \sqrt{3} = \frac{p - 5q}{2q}$$

Since p and q are integers, therefore $\frac{p-5q}{2q}$ must be a rational number.

But this is a contradiction as the LHS is an irrational number.

Our supposition was wrong.

Hence, $5+2\sqrt{3}$ is an irrational number. Hence proved.

We are given that an army contingent of 612 members is to march behind an army band of 48 members in a parade. The two groups are to march in the same number of columns. We need to find the maximum number of columns in which they can march.

OR

Members in army = 612 Members in band = 48. Therefore,

The maximum number of columns = H.C.F of 612 and 48. By applying Euclid's division lemma

 $612=48\times12+36$ $48=36\times1+12$ $36=12\times3+0$ Therefore, H.C.F. = 12 Hence, the maximum number of columns in which they can march is 12.

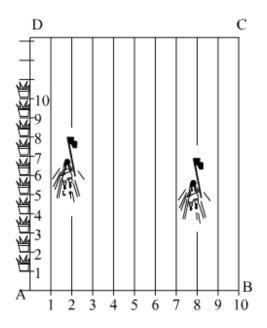
Question: 30

Read the following passage carefully and then answer the questions given at the end.

To conduct Sports Day activities, in your rectangular shaped school ground ABCD, lines have been drawn with chalk powder at a distance of 1 m each.

100 flower pots have been placed at a distance of 1 m from each other along AD, as

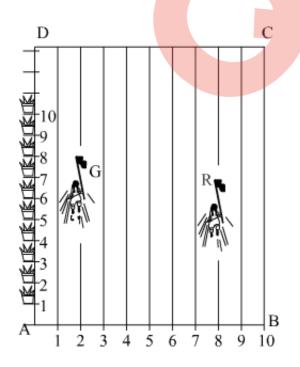
shown in Figure. Niharika runs 1/4th the distance AD on the 2nd line and posts a green flag. Preet runs 1/5th the distance AD on the eighth line and posts a red flag.



(i) What is the distance between the two flags?

(ii) If Rashmi has to post a blue flag exactly half way between the line segment joining QUESTION the two flags, where should she post the blue flag?

Solution:



It can be observed that Niharika posted the green flag at $\frac{1}{4}$ of the distance AD i.e., $\left(\frac{1}{4} \times 100\right)$ m = 25 m from the starting point of 2nd line. Therefore, the coordinates of this point G is (2, 25)

Similarly, Preet posted red flag at $\frac{1}{5}$ of the distance AD i.e., $\left(\frac{1}{5} \times 100\right)m = 20$ m from the starting point of 8th line. Therefore, the coordinates of this point R are (8, 20).

(i) Distance between these flags by using distance formula = GR

 $=\sqrt{\left(8-2\right)^{2}+\left(25-20\right)^{2}}=\sqrt{36+25}=\sqrt{61}\,\mathrm{m}$ (ii) The point at which Rashmi should post her blue flag is the mid-point of the line joining these points. Let this point be A (x, y). $x = \frac{2+8}{2}, y = \frac{25+20}{2}$ $x = \frac{10}{2} = 5, y = \frac{45}{2} = 22.5$ Hence, A(x, y) = (5, 22.5)

Therefore, Rashmi should post her blue flag at 22.5m on 5th line.

Question: 31

Solve graphically: 2x + 3y = 2, x - 2y = 8

Solution:

Given: 2x + 3y = 2x - 2y = 8

Consider the first equation 2x + 3y = 2.

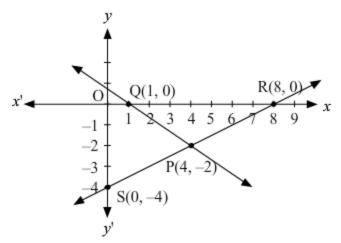
$$\begin{array}{c|cc} x & 4 & 1 \\ \hline y & -2 & 0 \end{array}$$

STION Hence, the points are P(4, -2) and Q(1, 0) respectively.

Considering the second equation x - 2y = 8.

Hence, the points are S(0, -4) and R(8, 0) respectively.

Now drawing the two lines on the coordinate axis, we get



Hence, the point of intersection of these two line is P(4, -2).

Question: 32

Find the zeros of the of the quadratic polynomial $6x^2 - 3 - 7x$ and verify the relationship between the zeros and the coefficients.

Solution:

The given quadratic polynomial is $6x^2 - 3 - 7x$. It can be rewritten as $6x^2 - 7x - 3$.

Let's factorize it by splitting the middle term. $\Rightarrow 6x^2 - 7x - 3$

 $\Rightarrow 6x^2 - 9x + 2x - 3$ $\Rightarrow 3x (2x - 3) + 1 (2x - 3)$ $\Rightarrow (2x - 3) (3x + 1)$

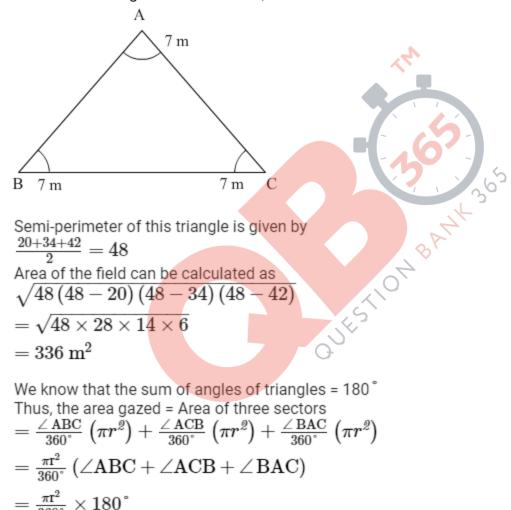
Its zeros are given by 2x - 3 = 0 and 3x + 1 = 0 $\Rightarrow x = \frac{3}{2}, \frac{-1}{3}$ Sum of zeros = $\frac{3}{2} + \frac{-1}{3} = \frac{7}{6} = \frac{-(-7)}{6} = \frac{-(\text{Cefficient of } x)}{(\text{Cefficient of } x^2)}$ Product of zeros = $\frac{3}{2} \times \frac{-1}{3} = \frac{-1}{2} = \frac{-3}{6} = \frac{-(\text{Constant term})}{(\text{Cefficient of } x^2)}$ Hence, the relation is verified.

Question: 33

Three horses are tied each with 7 m long rope at three corners of a triangular field having sides 20 m, 34 m and 42 m. Find the area of the plot which can be grazed by the horses.

Solution:

Given: Sides of the triangular field are 20m, 34m and 42m.



$$= \frac{\pi i}{360^{\circ}} \times \\ = \frac{1}{2}\pi r^2$$

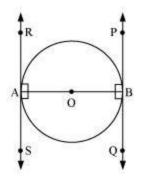
$$=\frac{1}{2}\pi(7)^2$$

$$= 77 \text{ m}^{2}$$

Question: 34

Prove that the tangents drawn at the end points of a diameter of a circle are parallel.

Solution:



Let AB be a diameter of the circle. Two tangents PQ and RS are drawn at points A and B respectively.

Radius drawn to these tangents will be perpendicular to the tangents.

Thus, $OA \perp RS$ and $OB \perp PQ$. We have $\angle OAR = 90^\circ$, $\angle OAS = 90^\circ$, $\angle OBP = 90^\circ$, $\angle OBQ = 90^\circ$

It can be observed t	hat
∠OAR = ∠OBQ	(Alternate interior angles)
∠OAS = ∠OBP	(Alternate interior angles)

Since alternate interior angles are equal, the lines PQ and RS will be parallel.

Question: 35

If 4 times the 4th term of an AP is equal to 18 times the 18th term, then find the 22nd term.

OR How many terms of the AP : 24, 21, 18, ... must be taken so that their sum is 78?

Solution:

OR

Let the first term be a and the common difference be d. According to question, $4a_4 = 18a_{18}$ $\Rightarrow 4(a+3d) = 18(a+17d)$ $\Rightarrow 4a+12d = 18a+306d$ $\Rightarrow -14a = 294d$ $\Rightarrow a = -\frac{294}{14}d = -21d$ 22nd term = $a_{22} = a + 21d = -21d + 21d = 0$ Given that 24, 21, 18, ... is an AP. Let n terms should be taken to make the sum 78 then 24 + 21 + 18 + ... to n terms = 78 Here a = 24, d = -3, $S_n = 78$, n = ? $S_n = \frac{n}{2} \{2a + (n-1)d\}$ $\Rightarrow 78 = \frac{n}{2} \{2 \times 24 + (n-1)(-3)\}$ $\Rightarrow 156 = n (48 - 3n + 3)$

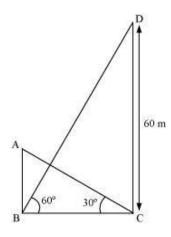
 $\Rightarrow 156 = n (48 - 3n + 3)$ $\Rightarrow 156 = n (51 - 3n)$ $\Rightarrow 3n^2 - 51n + 156 = 0$ $\Rightarrow 3 (n^2 - 17n + 52) = 0$ $\Rightarrow (n - 13) (n - 4) = 0$ $\therefore n = 4, 13$

Question: 36

The angle of elevation of the top of a building from the foot of a tower is 30°. The angle of elevation of the top of the tower from the foot of the building is 60°. If the tower is 60 m high, find the height of the building.

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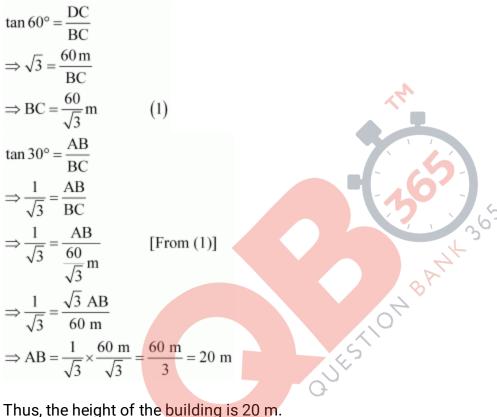
Solution:



Let AB denote the building and CD denote the tower. The height of the tower is given to be 60 m.

∴ CD = 60 m

We have to find the height of the building i.e. AB. In $\triangle BCD$,



Thus, the height of the building is 20 m.

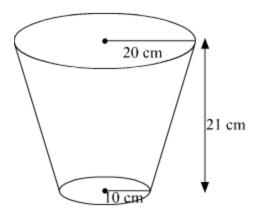
Question: 37

An open metal bucket is in the shape of a frustum of cone of height 21 cm with radii of its lower and upper ends are 10 cm and 20 cm respectively. Find the cost of milk which can completely fill the bucket at the rate of ₹ 40 per litre.

OR

A solid is in the shape of a cone surmounted on a hemisphere. The radius of each of them being 3.5 cm and the total height of the solid is 9.5 cm. Find the volume of the solid.

Solution:



Given, $r_1 = 10 \text{ cm}, r_2 = 20 \text{ cm}$ and h = 21 cmTherefore, the volume of the bucket (frustum) $= \frac{1}{3}\pi h (r_1^2 + r_2^2 + r_1 r_2)$ $= \frac{1}{3} \times \frac{22}{7} \times 21 \times (10^2 + 20^2 + 10 \times 20)$ $= \frac{1}{3} \times \frac{22}{7} \times 21 \times 700$ $= 15400 \text{ cm}^3$ $= \frac{15400}{1000} L$ = 15.4 LTherefore, the cost of milk = $Rs \, 15.4 \times 40 = Rs \, 616$ OR

Radius of the cone = Radius of the hemisphere = r (say) = 3.5 cm

Therefore, height of the cone = (9.5 - 3.5) = 6 cm (as the height of a hemisphere is equal to it's radius)

Therefore, Volume of the solid = Volume of cone + Volume of hemisphere

Question: 38

Find the mean of the following data :

Classes	0 - 20	20 - 40	40 - 60	60 - 80	80 - 100	100 – 120
Frequency	20	35	52	44	38	31

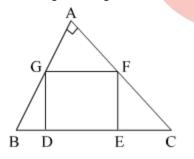
Solution:

Following is the given data:

Classes	f i	Xi	f _i x _i	
0-20	20	10	200	Ν
20-40	35	30	1050	•
40-60	52	50	2600	
60-80	44	70	3080	1
80-100	38	90	3420	1
100-120	31	110	3410	
	220		13,760	
Therefor	e, meai		$\frac{f_i x_i}{f_i} = \frac{137}{22}$	~ ~

Question: 39

In the given figure, DEFG is a square in a triangle ABC right angled at A.



Prove that (i) $\triangle AGF \sim \triangle DBG$ (ii) $\triangle AGF \sim \triangle EFC$

OR

In an obtuse $\triangle ABC$ ($\angle B$ is obtuse), AD is perpendicular to CB produced. Then prove that $AC^2 = AB^2 + BC^2 + 2BC \times BD$.

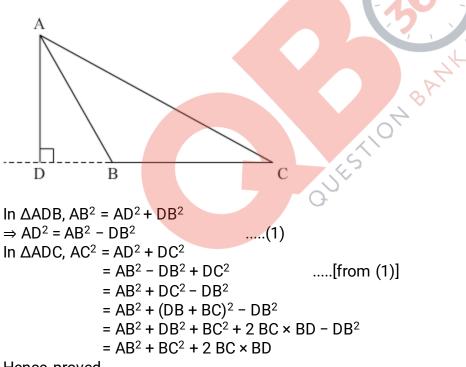
Solution:

Given: DEFG is a square inside a triangle ABC right angles at A. (i) In \triangle AGF and \triangle DBG, \angle AGF = \angle GBD (Corresponding angles as GF||||BC) \angle GAF = \angle GDB (both right angles) Therefore, \triangle AGF ~ \triangle DBG (By AA similarity theorem)

(ii) In $\triangle AGF$ and $\triangle EFC$, $\angle AFG = \angle FCE$ (Corresponding angles as $GF \parallel \parallel BC$) $\angle GAF = \angle FEC$ (both right angles) Therefore, $\triangle AGF \sim \triangle EFC$ (By AA similarity theorem) Hence proved.

Following is the $\triangle ABC$, where $\angle B$ is obtuse. AD is perpendicular to CB produced.

OR



Hence proved.

Question: 40

A person on tour has ₹ 4200 for his expenses. If he extends his tour for 3 days, he has to cut down his daily expenses by ₹ 70. Find the original duration of the tour.

Solution:

Let the original duration of tour be x days. The total amount with the person is Rs 4200. So, his daily expenses would be equal to $Rs \frac{4200}{x}$.

Now, according to the question, the tour has been extended for 3 days. Hence the total number of days = x+3 days New daily expenses = ${\rm Rs}\frac{4200}{x+3}$

Therefore, we have $\frac{4200}{x} - \frac{4200}{x+3} = 70$ $\Rightarrow 4200 \left(\frac{1}{x} - \frac{1}{x+3}\right) = 70$ $\Rightarrow 4200 \left[\frac{3}{x(x+3)}\right] = 70$ $\Rightarrow 180 = x^2 + 3x$ $\Rightarrow x^2 + 3x - 180 = 0$ $\Rightarrow (x+15) (x-12) = 0$ $\Rightarrow x = -15, 12$

Hence, x = 12 as x cannot be negative. Thus, the original duration of the tour was 12 days.