

**PRACTICE PAPER -2 (2020-21) CLASS XII  
MATHEMATICS**

**TIME ALLOWED: 3 HOURS**

**MAXIMUM MARKS: 80**

**GENERAL INSTRUCTIONS:**

1. This question paper contains two parts A and B. Each part is compulsory. Part A carries 24 marks and Part B carries 56 marks.
2. Part-A has Objective Type Questions and Part -B has Descriptive Type Questions.
3. Both Part A and Part B have choices.

**Part – A**

1. It consists of two sections- I and II.
2. Section I comprises of 16 very short answers type questions.
3. Section II contains 2 case studies. Each case study comprises of 5 case-based MCQs. An examinee is to attempt any 4 out of 5 MCQs.

**Part – B**

1. It consists of three sections- III, IV and V.
2. Section III comprises of 10 questions of 2 marks each.
3. Section IV comprises of 7 questions of 3 marks each.
4. Section V comprises of 3 questions of 5 marks each.
5. Internal choice is provided in 3 questions of Section –III, 2 questions of Section IV and 3 questions of Section-V. You have to attempt only one of the alternatives in all such questions.

**PART – A  
SECTION – I**

**(All questions are compulsory. In case of internal choices attempt any one)**

1. Write the smallest reflexive relation on set  $A = \{1, 2, 3, 4\}$ .

**Or**

If  $f : A \rightarrow B$  is an injection such that range of  $f = \{a\}$ . Determine the number of elements in A.

2. If R is a symmetric relation on a set A, then write a relation between R and  $R^{-1}$ .
3. Let  $A = \{1, 2, 3\}$ . Then, what is the number of equivalence relations containing (1, 2) ?

**Or**

If  $A = \{a, b, c\}$  and  $B = \{-2, -1, 0, 1, 2\}$ , write total number of one-one functions from A to B.

4. If  $\begin{bmatrix} a+b & 2 \\ 5 & ab \end{bmatrix} = \begin{bmatrix} 6 & 2 \\ 5 & 8 \end{bmatrix}$ , find the values of a and b.

5. If I is the identity matrix and A is a square matrix such that  $A^2 = A$ , then what is the value of  $(I + A)^2 - 3A$ ?

**Or**

Write a square matrix which is both symmetric as well as skew-symmetric.

6. A matrix A of order  $3 \times 3$  is such that  $|A| = 4$ . Find the value of  $|2A|$ .

7. Write a value of  $\int e^x \sec x (1 + \tan^2 x) dx$

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Or

Write a value of  $\int \frac{1 - \sin x}{\cos^2 x} dx$

8. Find the area bounded by the curves  $y = \sin x$  between the ordinates  $x = 0$ ,  $x = \pi$  and the  $x$ -axis.

9. If  $\sin x$  is an integrating factor of the differential equation  $\frac{dy}{dx} + Py = Q$ , then write the value of  $P$ .

Or

Write the order of the differential equation associated with the primitive

$$y = C_1 + C_2 e^x + C_3 e^{-2x+C_4}, \text{ where } C_1, C_2, C_3, C_4 \text{ are arbitrary constants.}$$

10. Find a vector in the direction of  $\vec{a} = 2\hat{i} - \hat{j} + 2\hat{k}$ , which has magnitude of 6 units.

11. For what value of  $\lambda$  are the vectors  $\vec{a} = 2i + \lambda i + k$  and  $\vec{b} = i - 2j + 3k$  perpendicular to each other?

12. If  $\vec{a}$  and  $\vec{b}$  are mutually perpendicular unit vectors, write the value of  $|\vec{a} + \vec{b}|$ .

13. The cartesian equation of a line AB is  $\frac{2x-1}{\sqrt{3}} = \frac{y+2}{2} = \frac{z-3}{3}$ . Find the direction cosines of a line parallel to AB.

14. Write the distance between the parallel planes  $2x - y + 3z = 4$  and  $2x - y + 3z = 18$ .

15. If  $P(A) = 0.3$ ,  $P(B) = 0.6$ ,  $P(B/A) = 0.5$ , find  $P(A \cup B)$ .

16. If  $X$  is a random-variable with probability distribution as given below :

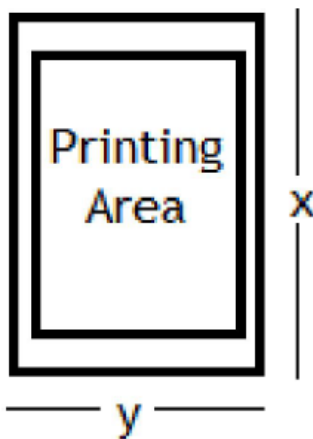
X:	0	1	2	3
$P(X = x)$ :	k	3k	3k	k

Find the value of  $k$ .

### SECTION II

( Both the Case study based questions are compulsory. Attempt any 4 sub parts from each question 17 and 18 . Each part carries 1 mark )

17. Following is the pictorial description for a page.



The total area of the page is  $150 \text{ cm}^2$ . The combined width of the margin at the top and bottom is 3 cm and the side 2 cm.

Using the information given above, answer the following :

(i) The relation between  $x$  and  $y$  is given by

(a)  $(x - 3)y = 150$

(b)  $xy = 150$

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- (c)  $x(y - 2) = 150$   
(d)  $(x - 2)(y - 3) = 150$

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(ii) The area of page where printing can be done, is given by

- (a)  $xy$   
(b)  $(x + 3)(y + 2)$   
(c)  $(x - 3)(y - 2)$   
(d)  $(x - 3)(y + 2)$

(iii) The area of the printable region of the page, in terms of  $x$ , is

- (a)  $156 + 2x + 450/x$   
(b)  $156 - 2x + 450/x$   
(c)  $156 - 2x - 45/x$   
(d)  $156 - 2x - 450/x$

(iv) For what value of ' $x$ ', the printable area of the page is maximum?

- (a) 15 cm  
(b) 10 cm  
(c) 12 cm  
(d) 15 units

(v) What should be dimension of the page so that it has maximum area to be printed?

- (a) Length = 1 cm, width = 15 cm  
(b) Length = 15 cm, width = 10 cm  
(c) Length = 15 cm, width = 12 cm  
(d) Length = 150 cm, width = 1 cm

18. Let  $X$  denotes the no. of colleges where you will apply after your results and  $P(X = x)$  denotes your probability of getting admission in  $x$  number of colleges. It is given that

$$P(X = x) = \begin{cases} kx, & \text{if } x = 0 \text{ or } 1 \\ 2kx, & \text{if } x = 2 \\ k(5 - x), & \text{if } x = 3 \text{ or } 4 \\ 0, & \text{if } x > 4 \end{cases}; \text{ where } k \text{ is a positive constant.}$$

Based on the above information answer the following :

(i) The value of  $k$  is

- (a) 1  
(b)  $1/3$   
(c)  $1/7$   
(d)  $1/8$

(ii) The probability that you will get admission in exactly one college, is

- (a)  $1/2$   
(b)  $1/3$   
(c)  $1/8$   
(d)  $1/5$

(iii) The probability that you will get admission in at most two colleges, is

- (a)  $7/12$   
(b)  $5/8$   
(c)  $5/21$   
(d)  $8/17$

(iv) What is the probability that you will get admission in at least 2 colleges?

- (a) 1/3  
 (b) 2/7  
 (c) 3/8  
 (d) 7/8

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- (v) What is the probability that you will get admission in more than 4 colleges?  
 (a) 0  
 (b) 1  
 (c) 1/2  
 (d) 1/8

**PART – B  
 SECTION III**

19. If  $\frac{dy}{dx} = e^{-2y}$  and  $y = 0$  when  $x = 5$ , then the value of  $x$  when  $y = 3$ .
20. If the points  $A(-1, 3, 2)$ ,  $B(-4, 2, -2)$  and  $C(5, 5, \lambda)$  are collinear, find the value of  $\lambda$ .
21. Find a vector in the direction of  $\vec{a} = 2\hat{i} - \hat{j} + 2\hat{k}$  which has magnitude 6 units.
22. Find the principal value of  
 $\tan^{-1}\left(\tan\frac{7\pi}{6}\right) + \cot^{-1}\left(\cot\frac{7\pi}{6}\right)$ .
23. Evaluate  
 $\int_0^{\frac{\pi}{2}} \log\left(\frac{3+5\cos x}{3+5\sin x}\right) dx$ .
- OR Evaluate  $\int \frac{\log(\sin x)}{\tan x} dx$
24. Find the slope of the normal to the curve  $x = a \cos^3 \theta$ ,  $y = a \sin^3 \theta$  at  $\theta = \frac{\pi}{4}$ .
25. If  $y = \tan^{-1}\left(\frac{\cos x}{1 + \sin x}\right)$  find  $\frac{dy}{dx}$
26. Find matrices  $X$  and  $Y$ , if

$$X + Y = \begin{bmatrix} 5 & 2 \\ 0 & 9 \end{bmatrix} \quad \text{and} \quad X - Y = \begin{bmatrix} 3 & 6 \\ 0 & -1 \end{bmatrix}$$

- OR Find the value of  $k$  so that the points  $A(5, 5)$ ,  $B(k, 1)$  and  $C(11, 7)$  are collinear.
27. A bag contains 15 tickets numbered from 1 to 15. A ticket is drawn and then another ticket is drawn without replacement. Find the probability that both tickets will show even numbers.
- OR A die is tossed thrice. Find the probability of getting an odd number at least once.
28. Using integration, find the area of the region bounded by the line  $y - 1 = x$ , the  $x$ -axis and the ordinates  $x = -2$  and  $x = 3$ .

**SECTION IV**

(All questions are compulsory. In case of internal choices attempt any one.)

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29. Let  $Z$  be the set of all integers and  $R$  be the relation on  $Z$  defined as  $R = \{(a, b) : a, b \in Z, (a - b) \text{ is divisible by } 5\}$ . Prove that  $R$  is an equivalence relation.
30. Using integration, find the area of the region bounded by the following curves, after making a rough sketch:

$$y = 1 + |x + 1|, \quad x = -3, \quad x = 3, \quad y = 0.$$

OR Find the area bounded by the parabola  $y^2 = 4x$  and the straight line  $x + y = 3$ .

31. Evaluate

$$\int_0^\pi \frac{x \sin x}{1 + \cos^2 x} dx$$

32. Find the intervals in which  $f(x) = (x + 1)^3 (x - 3)^3$  is increasing or decreasing.

33. If  $x = \tan\left(\frac{1}{a} \log y\right)$ , show that  $(1 + x^2) \frac{d^2y}{dx^2} + (2x - a) \frac{dy}{dx} = 0$ .

34. If  $x = ae^\theta (\sin \theta - \cos \theta)$  and  $y = ae^\theta (\sin \theta + \cos \theta)$ , find  $\frac{dy}{dx}$ .

OR If  $y^x = e^{y-x}$ , prove that  $\frac{dy}{dx} = \frac{(1 + \log y)^2}{\log y}$

35. Solve the following differential equation

$$(x^2 - 1) \frac{dy}{dx} + 2xy = \frac{1}{x^2 - 1}; \quad |x| \neq 1$$

**SECTION V**

(All questions are compulsory. In case of internal choices attempt any one.)

36. Find the equation of the plane through the intersection of the planes  $\vec{r} \cdot (\hat{i} + 3\hat{j}) - 6 = 0$  and  $\vec{r} \cdot (3\hat{i} - \hat{j} - 4\hat{k}) = 0$ , whose perpendicular distance from origin is unity.

OR

Find the distance of the point  $(2, 3, 4)$  from the line  $\frac{x+3}{3} = \frac{y-2}{6} = \frac{z}{2}$  measured parallel to the plane  $3x + 2y + 2z - 5 = 0$ .

37. Solve the following LPP Graphically :

Maximise  $z = 1000x + 600y$

Subject to  $x + y \leq 200, x \geq 20, y \geq 4x, x, y \geq 0$ .

OR

Solve the following linear programming problem graphically:

Maximise  $z = 6x + 5y$  subject to  $3x + 5y \leq 15, 5x + 2y \leq 10, x, y \geq 0$ .

36. Solve the following system of equations  $3x + 2y + z = 6; 4x - y + 2z = 5; 7x + 3y - 3z = 7$ .

If  $A = \begin{bmatrix} 3 & 2 & 1 \\ 4 & -1 & 2 \\ 7 & 3 & -3 \end{bmatrix}$  find  $A^{-1}$ .

OR

Find  $AB$ , use this to solve the system of equations  $x - y = 3$ ,  $2x + 3y + 4z = 17$ ,  $y + 2z = 7$ .

Where  $A = \begin{bmatrix} 1 & -1 & 0 \\ 2 & 3 & 4 \\ 0 & 1 & 2 \end{bmatrix}$  and  $B = \begin{bmatrix} 2 & 2 & -4 \\ -4 & 2 & -4 \\ 2 & -1 & 5 \end{bmatrix}$ .

