

**RD Sharma**  
**Solutions**  
**Class 12 Maths**  
**Chapter 6**  
**Ex 6.3**

### Chapter Determinants Ex 6.3 Q1(i)

If the vertices of a triangle are  $(x_1, y_1)$ ,  $(x_2, y_2)$  and  $(x_3, y_3)$  then the area of the triangle is given by :

$$\Delta = \frac{1}{2} \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix}$$

Substituting the values

$$\Delta = \frac{1}{2} \begin{vmatrix} 3 & 8 & 1 \\ -4 & 2 & 1 \\ 5 & -1 & 1 \end{vmatrix}$$

expanding the determinant along  $R_1$

$$\begin{aligned} &= \frac{1}{2} \left[ 3 \begin{vmatrix} 2 & 1 \\ -1 & 1 \end{vmatrix} - 8 \begin{vmatrix} -4 & 1 \\ 5 & 1 \end{vmatrix} + 1 \begin{vmatrix} -4 & 2 \\ 5 & -1 \end{vmatrix} \right] \\ &= \frac{1}{2} [3(3) - 8(-9) + 1(-6)] \\ &= \frac{1}{2} [9 + 72 - 6] = \frac{75}{2} \text{ sq. units} \end{aligned}$$

The area of the  $\Delta$  is  $\frac{75}{2}$  sq. units

**Chapter Determinants Ex 6.3 Q1(ii)**

The area is given by:

$$\Delta = \frac{1}{2} \begin{vmatrix} 2 & 7 & 1 \\ 1 & 1 & 1 \\ 10 & 8 & 1 \end{vmatrix}$$

expanding along  $R_1$

$$= \frac{1}{2} [2(-7) - 7(-9) + 1(-2)]$$

$$= \frac{1}{2} [-14 + 63 - 2]$$

$$= \frac{47}{2} \text{ sq. units}$$

The area of the  $\Delta$  is  $\frac{47}{2}$  sq. units

**Chapter Determinants Ex 6.3 Q1(iii)**

The area is given by:

$$\Delta = \frac{1}{2} \begin{vmatrix} -1 & -8 & 1 \\ -2 & -3 & 1 \\ 3 & 2 & 1 \end{vmatrix}$$

$$= \frac{1}{2} [-1(-5) + 8(-5) + 1(5)]$$

$$= \frac{1}{2} [5 - 40 + 5] = \frac{-30}{2} = 15 \text{ sq. units}$$

$\therefore$  Area can not be negative, so answer will be 15 sq. units.

The area of the  $\Delta$  is 15 sq. units.

**Chapter Determinants Ex 6.3 Q1(iv)**

The area is given by:

$$\Delta = \frac{1}{2} \begin{vmatrix} 0 & 0 & 1 \\ 6 & 0 & 1 \\ 4 & 3 & 1 \end{vmatrix}$$

Expanding along  $R_1$

$$= \frac{1}{2} [0 - 0 + 1(18)] = 9 \text{ sq. units}$$

The area is 9 sq. units

**Chapter Determinants Ex 6.3 Q2(i)**

If 3 points are collinear, then the area of the triangle then form will be zero.

Hence

$$\frac{1}{2} \begin{vmatrix} 5 & 5 & 1 \\ -5 & 1 & 1 \\ 10 & 7 & 1 \end{vmatrix} = 0$$

Expanding along  $R_1$

$$\begin{aligned} &= \frac{1}{2} [5(-6) - 5(-15) + 1(-35 - 10)] \\ &= \frac{1}{2} [-35 + 75 - 45] \\ &= \frac{1}{2} [0] \\ &= 0 \end{aligned}$$

Since the area of the triangle is zero, hence the points are collinear.

### Chapter Determinants Ex 6.3 Q2(ii)

If 3 points are collinear, then the area of the triangle then form will be zero.

Hence

$$\frac{1}{2} \begin{vmatrix} 1 & -1 & 1 \\ 2 & 1 & 1 \\ 4 & 5 & 1 \end{vmatrix} = 0$$

Expanding along  $R_1$

$$\begin{aligned} &= \frac{1}{2} [1(-4) + 1(-2) + 1(6)] \\ &= 0 \end{aligned}$$

Since the area of the triangle is zero, hence the points are collinear.

### Chapter Determinants Ex 6.3 Q2(iii)

If the points are collinear, then the area of the triangle will be zero.

So

$$\frac{1}{2} \begin{vmatrix} 3 & -2 & 1 \\ 8 & 8 & 1 \\ 5 & 2 & 1 \end{vmatrix} = 0$$

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Expanding along  $R_1$

$$\begin{aligned} &= \frac{1}{2} [3(6) + 2(3) + 1(-24)] \\ &= \frac{1}{2} [18 + 6 - 24] \\ &= \frac{1}{2} [0] \\ &= 0 \end{aligned}$$

Since the area of the triangle is zero, hence given points are collinear.

### Chapter Determinants Ex 6.3 Q2(iv)

If given points are collinear, then the area of the triangle must be zero.

Hence

$$\begin{aligned} &= \frac{1}{2} \begin{vmatrix} 2 & 3 & 1 \\ -1 & -2 & 1 \\ 5 & 8 & 1 \end{vmatrix} \\ &= \frac{1}{2} [2(-10) - 3(-6) + 1(2)] \\ &= \frac{1}{2} [-20 + 18 + 2] \\ &= \frac{1}{2} [0] \\ &= 0 \end{aligned}$$

Hence the given points are collinear.

### Chapter Determinants Ex 6.3 Q3

If the given points are collinear, the area of the triangle must be zero.

Hence

$$\frac{1}{2} \begin{vmatrix} a & 0 & 1 \\ 0 & b & 1 \\ 1 & 1 & 1 \end{vmatrix}$$

Expanding along  $R_1$

$$\begin{aligned} &= \frac{1}{2} [a(b-1) - 0(0-1) + 1(-b)] = 0 \\ \text{or } ab - a - 0 - b &= 0 \\ \text{or } ab &= a + b \end{aligned}$$

Hence proved

### Chapter Determinants Ex 6.3 Q4

If the given points are collinear, then the area of the triangle must be zero.

Hence

$$\frac{1}{2} \begin{vmatrix} a & b & 1 \\ a' & b' & 1 \\ a-a' & b-b' & 1 \end{vmatrix} = 0$$

or

$$\begin{aligned} &\frac{1}{2} [a(b'-b+b') - b(a'-a+a') + 1(a'b - a'b' - ab' + a'b')] = 0 \\ \text{or } \frac{1}{2} [ab' - ab + ab' - a'b + ab - a'b + a'b - ab'] &= 0 \\ \text{or } ab' - a'b &= 0 \\ ab' &= a'b \end{aligned}$$

Hence proved

### Chapter Determinants Ex 6.3 Q5

If the points are collinear, then the area of the triangle must be zero.

Hence

$$\begin{vmatrix} 1 & -5 & 1 \\ -4 & 5 & 1 \\ \lambda & 7 & 1 \end{vmatrix} = 0$$

Expanding along  $R_1$

$$\begin{aligned} 1(-2) + 5(-4 - \lambda) + 1(-28 - 5\lambda) &= 0 \\ -2 - 20 - 5\lambda - 28 - 5\lambda &= 0 \\ -50 - 10\lambda &= 0 \\ \lambda &= -5 \end{aligned}$$

Hence  $\lambda = -5$

### Chapter Determinants Ex 6.3 Q6

$$\text{Area} = \frac{1}{2} \begin{vmatrix} x & 4 & 1 \\ 2 & -6 & 1 \\ 5 & 4 & 1 \end{vmatrix}$$

$$\pm 2 \times 35 = \begin{vmatrix} x & 4 & 1 \\ 2 & -6 & 1 \\ 5 & 4 & 1 \end{vmatrix}$$

$$\pm 70 = x(-10) - 4(-3) + 1(38)$$

$$\pm 70 = -10x + 12 + 38$$

$$\pm 70 = -10x + 50 \quad \text{--- (1)}$$

Taking (+) sign

$$+70 = -10x + 50$$

$$10x = -20 \text{ or } x = -2$$

Again taking (-) sign

$$-70 = -10x + 50$$

$$10x = 120 \text{ or } x = 12$$

Hence  $x = -2, 12$

### Chapter Determinants Ex 6.3 Q7

$$\text{Area} = \frac{1}{2} \begin{vmatrix} 1 & 4 & 1 \\ 2 & 3 & 1 \\ -5 & -3 & 1 \end{vmatrix}$$

$$= \frac{1}{2} [1(6) - 4(7) + 1(-6 + 15)]$$

$$= \frac{1}{2} [6 - 28 + 9]$$

$$= \frac{1}{2} [-13]$$

$$= \frac{13}{2} \text{ sq. units} \quad [\because \text{Area can not be negative}]$$

Also, since the area of the triangle is non-zero.

Hence these points are non-collinear.

### Chapter Determinants Ex 6.3 Q8

$$\begin{aligned}\text{Area} &= \frac{1}{2} \begin{vmatrix} -3 & 5 & 1 \\ 3 & -6 & 1 \\ 7 & 2 & 1 \end{vmatrix} \\ &= \frac{1}{2} [-3(-8) - 5(-4) + 1(48)] \\ &= \frac{1}{2} [24 + 20 + 48] \\ &= 46 \text{ sq. units}\end{aligned}$$

Hence the area is 46 sq. units.

### Chapter Determinants Ex 6.3 Q9

If the given points are collinear, then the area of the triangle must be zero.

$$\text{so } \frac{1}{2} \begin{vmatrix} k & 2-2k & 1 \\ -k+1 & 2k & 1 \\ -4-k & 6-2k & 1 \end{vmatrix} = 0$$

expanding along  $R_1$

$$k(2k - 6 + 2k) - (2 - 2k)(-k + 1 + 4 + k) + 1(1 - k) \times (6 - 2k) - 2k(-4 - k) = 0$$

$$k(4k - 6) - (2 - 2k)(5) + 1[6 - 2k - 6k + 2k^2 + 8k + 2k^2] = 0$$

$$4k^2 - 6k - 10 + 10k + 6 + 4k^2 = 0$$

$$8k^2 + 4k - 4 = 0$$

$$8k^2 + 8k - 4k - 4 = 0 \quad (\text{Middle term splitting})$$

$$8k(k + 1) - 4(k + 1) = 0$$

$$(8k - 4)(k + 1) = 0$$

$$\text{If } 8k - 4 = 0 \quad \text{or} \quad \text{if } k + 1 = 0$$

$$k = \frac{1}{2} \quad \quad \quad k = -1$$

$$\text{Hence } k = -1, \frac{1}{2}$$

### Chapter Determinants Ex 6.3 Q10

Since the points are collinear, hence the area of the triangle must be zero.

$$\text{so } \frac{1}{2} \begin{vmatrix} x & -2 & 1 \\ 5 & 2 & 1 \\ 8 & 8 & 1 \end{vmatrix} = 0$$

$$\text{or } x(-6) + 2(-3) + 1(24) = 0$$

$$\text{or } -6x - 6 + 24 = 0$$

$$-6x + 18 = 0$$

$$x = 3$$

Hence  $x = 3$

### Chapter Determinants Ex 6.3 Q11

Since the points are collinear, hence the area of the triangle must be zero.

$$\frac{1}{2} \begin{vmatrix} 3 & -2 & 1 \\ x & 2 & 1 \\ 8 & 8 & 1 \end{vmatrix} = 0$$

$$\begin{aligned} 3(-6) + 2(x - 8) + 1(8x - 16) &= 0 \\ -18 + 2x - 16 + 8x - 16 &= 0 \\ 10x &= 50 \\ x &= 5 \end{aligned}$$

Hence  $x = 5$

### Chapter Determinants Ex 6.3 Q12(i)

Let  $A(x, y)$ ,  $B(1, 2)$  and  $C(3, 6)$  are 3 points in a line.

Since these points are collinear, hence area of the triangle must be zero.

$$\frac{1}{2} \begin{vmatrix} x & y & 1 \\ 1 & 2 & 1 \\ 3 & 6 & 1 \end{vmatrix} = 0$$

Expanding along  $R_1$

$$\begin{aligned} x(-4) - y(-2) + 1(0) &= 0 \\ -4x + 2y &= 0 \\ \text{or } 2x - y &= 0 \\ \text{or } y &= 2x \end{aligned}$$

Hence the equation is  $y = 2x$

### Chapter Determinants Ex 6.3 Q12(ii)

Let  $A(x, y)$ ,  $B(3, 1)$  and  $C(9, 3)$  are 3 points in a line.

Since these points are collinear, hence the area of the triangle  $ABC$  must be zero.

$$\frac{1}{2} \begin{vmatrix} x & y & 1 \\ 3 & 1 & 1 \\ 9 & 3 & 1 \end{vmatrix} = 0$$

Expanding along  $R_1$

$$\begin{aligned} x(-2) - y(-6) + 1(0) &= 0 \\ -2x + 6y &= 0 \\ x - 3y &= 0 \end{aligned}$$

Hence the equation of the line is  $x - 3y = 0$

### Chapter Determinants Ex 6.3 Q13(i)



$$\text{Area} = \frac{1}{2} \begin{vmatrix} k & 0 & 1 \\ 4 & 0 & 1 \\ 0 & 2 & 1 \end{vmatrix}$$

$$\pm 4 = \frac{1}{2} \begin{vmatrix} k & 0 & 1 \\ 4 & 0 & 1 \\ 0 & 2 & 1 \end{vmatrix}$$

Expanding along  $R_1$

$$\pm 8 = k(-2) - 0(4 - 0) + 1(8)$$

$$\pm 8 = -2k + 8$$

Taking positive (+) sign

$$+8 = -2k + 8 \quad \text{or } k = 0$$

Taking negative (-) sign

$$-8 = -2k + 8 \quad \text{or } k = 8$$

Hence  $k = 0, 8$