RD Sharma Solutions Class 12 Maths Chapter 13 Ex 13.2

Let x be the side of square.

Area
$$(A) = x^{2}$$

 $\frac{dA}{dt} = 2x \frac{dx}{dt}$
 $\left(\frac{dA}{dt}\right)_{8 \text{ cm}} = 2 \times (8) (4)$
 $\frac{dA}{dt} = 64 \text{ cm}^{2} / \text{min}$

Area increases at a rate of 64 cm²/min.

Derivatives as a Rate Measurer Ex 13.2 Q2

Let edge of the cube is x cm.

Let V be volume of cube,

$$V = x^{3}$$
$$\frac{dV}{dt} = 3x^{2}\frac{dx}{dt}$$
$$= 3(10)^{2} \times (3)$$
$$= 900 \text{ cm}^{3}/\text{sec}$$

So,

Volume increases at a rate of 900 cm³/sec.

Derivatives as a Rate Measurer Ex 13.2 Q3

Let x be the side of the square.

Here,
$$\frac{dx}{dt} = 0.2 \text{ cm/sec.}$$

 $P = 4x$
 $\frac{dP}{dt} = 4\frac{dx}{dt}$
 $= 4 \times (0.2)$
 $\frac{dP}{dt} = 0.8 \text{ cm/sec}$

So, perimeter increases at the rate of 0.8 cm / sec.

The circumference of a circle (C) with radius (r) is given by

 $C = 2\pi r$.

Therefore, the rate of change of circumference (C) with respect to time (t) is given by,

$$\frac{dC}{dt} = \frac{dC}{dr} \cdot \frac{dr}{dt} \text{ (By chain rule)}$$
$$= \frac{d}{dr} (2\pi r) \frac{dr}{dt}$$
$$= 2\pi \cdot \frac{dr}{dt}$$

It is given that $\frac{dr}{dt} = 0.7 \text{ cm/s}$.

Hence, the rate of increase of the circumference is $2\pi (0.7) = 1.4\pi$ cm/s.

Derivatives as a Rate Measurer Ex 13.2 Q5

Let r be the radius of the spherical soap bubble.

Here, $\frac{dr}{dt}$ = 0.2 cm/sec, r = 7 cm Surface Area (A) = $4\pi r^2$

$$\begin{aligned} \frac{dA}{dt} &= 4\pi \left(2r\right) \frac{dr}{dt} \\ \left(\frac{dA}{dt}\right)_{r=7} &= 4\pi \left(2 \times 7\right) \times 0. \\ &= 11.2\pi \text{ cm}^2/\text{sec.} \end{aligned}$$

So, area of bubble increases at the rate of 11.2 π cm²/sec.

Derivatives as a Rate Measurer Ex 13.2 Q6

The volume of a sphere (V) with radius (r) is given by,

$$V = \frac{4}{3}\pi r^3$$

 \therefore Rate of change of volume (V) with respect to time (t) is given by,

$$\frac{dV}{dt} = \frac{dV}{dr} \cdot \frac{dr}{dt} \text{ [By chain rule]}$$
$$= \frac{d}{dr} \left(\frac{4}{3}\pi r^3\right) \cdot \frac{dr}{dt}$$
$$= 4\pi r^2 \cdot \frac{dr}{dt}$$

It is given that
$$\frac{dV}{dt} = 900 \text{ cm}^3/\text{s}$$
.

$$\therefore 900 = 4\pi r^2 \cdot \frac{dr}{dt}$$
$$\Rightarrow \frac{dr}{dt} = \frac{900}{4\pi r^2} = \frac{225}{\pi r^2}$$

Therefore, when radius = 15 cm,

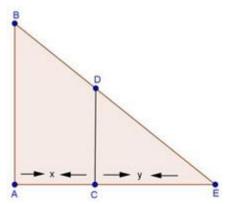
$$\frac{dr}{dt} = \frac{225}{\pi (15)^2} = \frac{1}{\pi}$$

Hence, the rate at which the radius of the balloon increases when the radius is 15 cm is $\frac{1}{\pi}$ cm/s.

Derivatives as a Rate Measurer Ex 13.2 Q7

Let r be the radius of the air bubble. Here, $\frac{dr}{dt} = 0.5$ cm/sec, r = 1 cm Volume $(V) = \frac{4}{3} \pi r^3$ $\frac{dV}{dt} = \frac{4}{3} \pi (3r^2) \frac{dr}{dt}$ $= 4\pi r^2 \frac{dr}{dt}$ $= 4\pi (1)^2 \times (0.5)$ $\frac{dV}{dt} = 2\pi$ cm³/sec.

So, volume of air bubble increases at the rate of 2π cm³/sec.



Let AB be the lamp-post. Suppose at time t, the man CD is at a distance of x meters from the lamp-post and y meters be the length of his shadow CB.

Here, $\triangle ABE$ and $\triangle CDE$ are similar, so

$$\frac{AB}{CD} = \frac{AE}{CE}$$

$$\frac{6}{2} = \frac{x+y}{y}$$

$$3y = x + y$$

$$2y = x$$

$$2\frac{dy}{dt} = \frac{dx}{dt}$$

$$\frac{dy}{dt} = \frac{5}{2} \text{ km/hi}$$

So, the length of his shadow increases at the rate of $\frac{5}{2}$ km/hr.

Derivatives as a Rate Measurer Ex 13.2 Q9

The area of a circle (A) with radius (r) is given by $A = \pi r^2$.

Therefore, the rate of change of area (A) with respect to time (t) is given by,

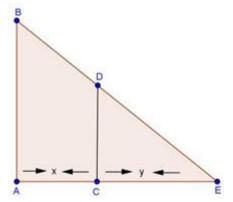
$$\frac{dA}{dt} = \frac{d}{dt} \left(\pi r^2\right) = \frac{d}{dr} \left(\pi r^2\right) \frac{dr}{dt} = 2\pi r \frac{dr}{dt} \text{ [By chain rule]}$$

It is given that $\frac{dr}{dt} = 4 \text{ cm/s}$.

Thus, when r = 10cm,

$$\frac{dA}{dt} = 2\pi \left(\mathbf{19}(\mathbf{4}) = 80\pi \right)$$

Hence, when the radius of the circular wave is 8 cm, the enclosed area is increasing at the rate of $80\pi\,cm^2/s$



Let *AB* be the height of pole. Suppose at time t, the man *CD* is at a distance of x meters from the lamp-post and y meters be the length of his shadow *CE*, then

$$\frac{dx}{dt} = 1.1 \text{ m/sec}$$

 $\triangle ABE$ is similar to $\triangle CDE$,

$$\frac{AB}{CD} = \frac{AE}{CE}$$

$$\frac{600}{160} = \frac{x+y}{y}$$

$$\frac{15}{4} = \frac{x+y}{y}$$

$$15y = 4x + 4y$$

$$11y = 4x$$

$$11\frac{dy}{dx} = 4\frac{dx}{dt}$$

$$\frac{dy}{dt} = \frac{4}{11}(1.1)$$

$$\frac{dy}{dt} = 0.4 \text{ m/sec}$$

Rate of increasing of shadow = 0.4 m/sec.

Let *AB* be the height of source of light. Suppose at time t, the man *CD* is at a distance of x meters from the lamp-post and y meters be the length of his shadow *CE*, then

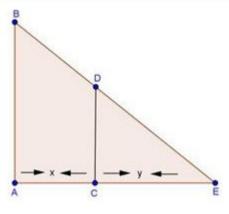
$$\frac{dx}{dt} = 2 \text{ m/sec}$$

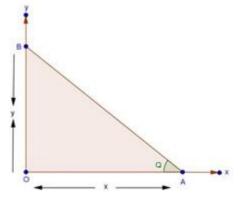
 $\triangle ABE$ is similar to $\triangle CDE$,

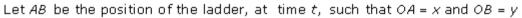
 $\frac{AB}{CD} = \frac{AE}{CE}$ $\frac{900}{180} = \frac{x+y}{y}$ 5y = x + y4y = x $4\frac{dy}{dt} = \frac{dx}{dt}$ $\frac{dy}{dt} = \frac{2}{4}$ $=\frac{1}{2}$ $\frac{dy}{dt} = 0.5 \text{ m/sec}$

So, rate of increase of shadow is 0.5 m/sec.

The diagram of the problem is shown below







Here,

$$OA^{2} + OB^{2} = AB^{2}$$

 $x^{2} + y^{2} = (13)^{2}$
 $x^{2} + y^{2} = 169$ ----(i)

And
$$\frac{dx}{dt} = 1.5 \text{ m/sec}$$

From figure, $\tan \theta = \frac{y}{x}$

Differentiating equation (i) with respect to t,

$$2x \frac{dx}{dt} + 2y \frac{dy}{dt} = 0$$
$$2(1.5)x + 2y \frac{dy}{dt} = 0$$
$$3x + 2y \frac{dy}{dt} = 0$$
$$\frac{dy}{dt} = -\frac{3x}{2y}$$

Differentiating equation (ii) with respect to t,

$$\sec^{2}\theta \frac{d\theta}{dt} = \frac{d \frac{dy}{dt} - y \frac{dx}{dt}}{x^{2}}$$

$$= \frac{x \times \left(-\frac{3x}{2y}\right) - y (1.5)}{x^{2}}$$

$$= \frac{-1.5x^{2} - 1.5y^{2}}{yx^{2}}$$

$$\frac{d\theta}{dt} = \frac{-1.5\left(x^{2} + y^{2}\right)}{x^{2}y \sec^{2}\theta}$$

$$= \frac{-1.5\left(x^{2} + y^{2}\right)}{x^{2}y\left(1 + \tan^{2}\theta\right)}$$

$$\frac{d\theta}{dt} = \frac{-1.5\left(x^{2} + y^{2}\right)}{x^{2}y\left(1 + \frac{y^{2}}{x^{2}}\right)}$$

$$= \frac{-1.5\left(x^{2} + y^{2}\right)}{x^{2}y\left(x^{2} + y^{2}\right)}$$

$$= \frac{-1.5}{y}$$

$$= \frac{-1.5}{\sqrt{169 - x^{2}}}$$

$$= \frac{-1.5}{5}$$

$$= -0.3 \text{ radian/sec}$$

So, angle between ladder and ground is decreasing at the rate of 0.3 radian/sec.

Here, curve is

$$y = x^2 + 2x$$

And
$$\frac{dy}{dt} = \frac{dx}{dt}$$

 $y = x^2 + 2x$
 $\Rightarrow \qquad \frac{dy}{dt} = 2x \frac{dx}{dt} + 2 \frac{dx}{dt}$
 $\Rightarrow \qquad \frac{dy}{dt} = \frac{dx}{dt}(2x + 2)$

----(i)

Using equation (i),

$$2x + 2 = 1$$
$$2x = -1$$
$$x = -\frac{1}{2}$$
So,
$$y = x^{2} + 2x$$
$$= \left(-\frac{1}{2}\right)^{2} + 2\left(-\frac{1}{2}\right)$$
$$= \frac{1}{4} - 1$$
$$y = -\frac{3}{4}$$

So, required points is $\left(-\frac{1}{2},-\frac{3}{4}\right)$.

Derivatives as a Rate Measurer Ex 13.2 Q14

Here,

$$\frac{dx}{dt} = 4$$
 units/sec, and $x = 2$

And, $y = 7x - x^3$

Slope of the curve(S) =
$$\frac{dy}{dx}$$

 $S = 7 - 3x^2$
 $\frac{ds}{dt} = -6x \frac{dx}{dt}$
 $= -6(2)(4)$
 $= -48 \text{ units/sec}$

So, slope is decreasing at the rate of 48 units/sec.

Here,

Derivatives as a Rate Measurer Ex 13.2 Q16(i)

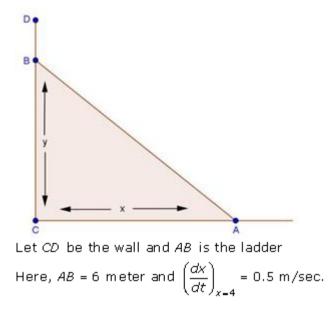
Here,

$$2 \frac{d(\sin \theta)}{dt} = \frac{d\theta}{dt}$$
$$2 \times \cos \theta \frac{d\theta}{dt} = \frac{d\theta}{dt}$$
$$2 \cos \theta = 1$$
$$\cos \theta = \frac{1}{2}$$

$$\theta = \frac{\pi}{3}$$
.

Derivatives as a Rate Measurer Ex 13.2 Q16(ii)

$$\frac{d\theta}{dt} = -2\frac{d}{dt}(\cos\theta)$$
$$\frac{d\theta}{dt} = -2(-\sin\theta)\frac{d\theta}{dt}$$
$$1 = 2\sin\theta$$
$$\sin\theta = \frac{1}{2}$$
$$\theta = \frac{\pi}{6}$$



From figure,

$$AB^{2} = x^{2} + y^{2}$$

(6)² = x² + y²
36 = x² + y²

Differentiating it with respect to t,

$$0 = 2x \frac{dx}{dt} + 2y \frac{dy}{dt}$$

$$\frac{dy}{dt} = -\frac{x}{y} \frac{dx}{dt}$$
 ----(i)

$$\left(\frac{dy}{dt}\right)_{x=4} = \frac{4(0.5)}{\sqrt{36 - x^2}}$$

$$= -\frac{2}{\sqrt{36 - 16}}$$

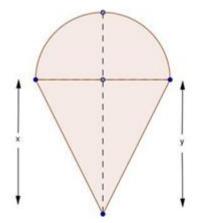
$$= -\frac{2}{2\sqrt{5}}$$

$$= -\frac{1}{\sqrt{5}} \text{ m/sec.}$$

So, ladder top is sliding at the rate of $\frac{1}{\sqrt{5}}$ m/sec.

Now, to find x when $\frac{dx}{dt} = -\frac{dy}{dt}$ From equation (i), $\frac{dy}{dt} = -\frac{x}{y}\frac{dx}{dt}$ $-\frac{dx}{dt} = -\frac{x}{v}\frac{dx}{dt}$ X = YNow, $36 = x^2 + y^2$ $36 = x^2 + x^2$ $2x^2 = 36$ $x^2 = 18$ $x = 3\sqrt{2}$ m

When foot and top are moving at the same rate, foot of wall is $3\sqrt{2}$ meters away from the wall



Let height of the cone is x cm. and radius of sphere is r cm.

Here given,

$$x = 2r$$
 ----(i)
 $h = x + r$
 $h = 2r + r$
 $h = 3r$ ----(ii)

v = volume of cone + volume of hemisphere

$$= \frac{1}{3} \pi r^{2} \times + \frac{2}{3} \pi r^{3}$$

$$= \frac{1}{3} \pi r^{2} (2r) + \frac{2}{3} \pi r^{3}$$
[Using equation (ii)]
$$v = \frac{2}{3} \pi r^{3} + \frac{2}{3} \pi r^{3}$$

$$= \frac{4}{3} \pi r^{3}$$

$$= \frac{4}{3} \pi \left(\frac{h}{3}\right)^{3}$$

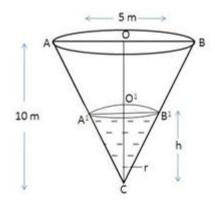
$$v = \frac{4}{81} \pi h^{3}$$

$$\frac{dv}{dh} = \frac{4}{81} \pi \times 3h^{2}$$

$$\left(\frac{dv}{dh}\right)_{h=9} = \frac{12}{81} \pi (9)^{2}$$

$$\left(\frac{dv}{dh}\right)_{h=9} = 12\pi \text{ cm}^{2}$$

Volume is changing at the rate 12π cm² with respect to total height.



Let α be the semi vertical angle of the cone CAB whose height CO is 10 m and radius OB = 5 m.

Now,

$$\tan \alpha = \frac{OB}{CO}$$
$$= \frac{5}{10}$$
$$\tan \alpha = \frac{1}{2}$$

Let ${\boldsymbol{\mathcal{V}}}$ be the volume of the water in the cone, then

$$v = \frac{1}{3}\pi \left(O'B'\right)^{2} (CO')$$

$$= \frac{1}{3}\pi \left(h \tan \alpha\right)^{2} (h)$$

$$v = \frac{1}{3}\pi h^{3} \tan^{2} \alpha$$

$$v = \frac{\pi}{12} h^{2} \qquad \left[\because \tan \alpha = \frac{1}{2}\right]$$

$$\frac{dv}{dt} = \frac{\pi}{12} 3h^{2} \frac{dh}{dt}$$

$$\pi = \frac{\pi}{4}h^{2} \frac{dh}{dt} \qquad \left[\because \frac{dV}{dt} = m^{3}/\text{min}\right]$$

$$\frac{dh}{dt} = \frac{4}{h^{2}}$$

$$\left(\frac{dh}{dt}\right)_{2.5} = \frac{4}{(2.5)^{2}} \qquad \left[\because h = 10 - 7.5 = 2.5 \text{ m}\right]$$

$$= \frac{4}{6.25}$$

$$= 0.64 \text{ m/min}$$

So, water level is rising at the rate of 0.64 m/min.

Let AB be the lamp-post. Suppose at time t, the man CD is at a distance x m. from the lamp-post and y m be the length of the shadow CE.

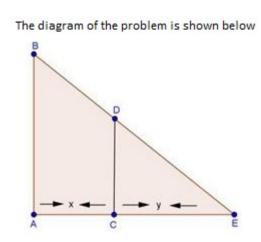
Here,
$$\frac{dx}{dt} = 6 \text{ km/hr}$$

 $CD = 2 \text{ m}, AB = 6 \text{ m}$

Here, *ABE* and *ACDE* are similar

So,
$$\frac{AB}{CD} = \frac{AE}{CE}$$
$$\frac{6}{2} = \frac{x+y}{y}$$
$$3y = x + y$$
$$2y = x$$
$$2\frac{dy}{dt} = \frac{dx}{dt}$$
$$2\frac{dy}{dt} = 6$$
$$\frac{dy}{dt} = 3 \text{ km/hr}$$

So, length of his shadow increases at the rate of 3 km/hr.



Here,
$$rac{dA}{dt}$$
= 2 cm²/sec

To find
$$\frac{dV}{dt}$$
 at $r = 6$ cm
 $A = 4\pi r^2$
 $\frac{dA}{dt} = 8\pi r \frac{dr}{dt}$
 $2 = 8\pi r \frac{dr}{dt}$
 $\frac{dr}{dt} = \frac{1}{4\pi r}$ cm/sec

Now,
$$V = \frac{4}{3}\pi r^3$$

$$\frac{dV}{dt} = 4\pi r^2 \frac{dr}{dt}$$
$$= 4\pi r^2 \left(\frac{1}{4\pi r}\right)$$
$$= r$$
$$\frac{dV}{dt} = 6 \text{ cm}^3/\text{sec}$$

So, volume of bubble is increasing at the rate of 6 $\,\rm cm^{\,3}/sec.$

Derivatives as a Rate Measurer Ex 13.2 Q22

Here,
$$\frac{dr}{dt} = 2 \text{ cm/sec}, \frac{dh}{dt} = -3 \text{ cm/sec}$$

To find
$$\frac{dV}{dt}$$
 when $r = 3 \text{ cm}$, $h = 5 \text{ cm}$

Now,
$$V = \text{volume of cylinder}$$

 $V = \pi r^2 h$
 $\frac{dV}{dt} = \pi \left[2r \frac{dr}{dt} \times h + r^2 \frac{dh}{dt} \right]$
 $= \pi \left[2(3)(2)(5) + (3)^2 (-3)^2 \right]$
 $= \pi \left[60 - 27 \right]$
 $\frac{dV}{dt} = 33\pi \text{ cm}^3/\text{sec}$

So, volume of cylinder is increasing at the rate of 33 π cm $^3/sec.$

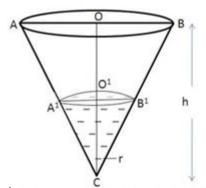
Let V be volume of sphere with miner radius r and onter radius R, then

$$V = \frac{4}{3}\pi \left(R^3 - r^3\right)$$
$$\frac{dV}{dt} = \frac{4}{3}\pi \left(3R^2 \frac{dR}{dt} - 3r^2 \frac{dr}{dt}\right)$$
$$0 = \frac{4\pi}{3}3 \left(R^2 \frac{dR}{dt} - r^2 \frac{dr}{dt}\right)$$
$$R^2 \frac{dR}{dt} = r^2 \frac{dr}{dt}$$
$$\left(8\right)^2 \frac{dR}{dt} = \left(4\right)^2 \left(1\right)$$
$$\frac{dR}{dt} = \frac{16}{64}$$
$$\frac{dR}{dt} = \frac{1}{4} \text{ cm/sec}$$

Rate of increasing of onter radius = $\frac{1}{4}$ cm/sec.

Derivatives as a Rate Measurer Ex 13.2 Q24

[Since volume V is constant]



Let α be the semi vertical angle of the cone CAB whose height CO is half of radius OB.

ſ

r

Now,

$$\tan \alpha = \frac{OB}{CO}$$
$$= \frac{OB}{2OB}$$
$$[\because CO = 2OB]$$
$$\tan \alpha = \frac{1}{2}$$

Let V be the volume of the sand in the cone

 $V = \frac{1}{3}\pi r^2 h$

1

$$= \frac{1}{3} \pi \left(\frac{h}{2}\right)^2 h$$

$$= \frac{\pi}{12} h^3$$

$$\frac{dV}{dt} = \frac{3\pi}{12} h^2 \frac{dh}{dt}$$

$$50 = \frac{3\pi}{12} h^2 \frac{dh}{dt}$$

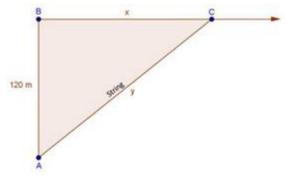
$$\left[\because \frac{dV}{dt} = 50 \text{ cm}^3/\text{min} \right]$$

$$\frac{dh}{dt} = \frac{200}{\pi h^2}$$

$$= \frac{200}{\pi (5)^2}$$

$$\frac{dh}{dt} = \frac{8}{3.14} \text{ cm}/\text{min}$$

Rate of increasing of height = $\frac{8}{\pi}$ cm/min



Let C be the position of kite and AC be the string.

Here,
$$y^2 = x^2 + (120)^2$$
 ----(i)
 $2y \frac{dy}{dt} = 2x \frac{dx}{dt}$
 $y \frac{dy}{dt} = x \frac{dx}{dt}$
 $\frac{dy}{dt} = \frac{x}{y} (52)$ ----(ii) $\left[\because \frac{dx}{dt} = 52 \text{ m/sec} \right]$

From equation (i),

$$y^2 = x^2 + (120)^2$$

 $(130)^2 = x^2 + (120)^2$
 $x^2 = 16900 - 14400$
 $x^2 = 2500$
 $x = 50$

Using equation (ii),

$$\frac{dy}{dt} = \frac{x}{y} (52) \\ = \frac{50}{130} (52) \\ = 20 \text{ m/sec}$$

So, string is being paid out at the rate of 20 m/sec.

Here,

Put
$$x = 1$$
, $y = \frac{2}{3} + 1 = \frac{5}{3}$
Put $x = -1$, $y = \frac{2}{3}(-1) + 1 = \frac{1}{3}$

So, required point
$$\left(1,\frac{5}{3}\right)$$
 and $\left(-1,\frac{1}{3}\right)$.

Derivatives as a Rate Measurer Ex 13.2 Q27

Here,

 $\frac{dx}{dt} = \frac{dy}{dt} \qquad ---(i)$ and curve is $y^2 = 8x$ $2y \frac{dy}{dt} = 8 \frac{dx}{dt}$ $2y = 8 \qquad [using equation (i)]$ y = 4 $\Rightarrow \qquad (4)^2 = 8x$ $\Rightarrow \qquad x = 2$

So, required point = (2,4).

Let edge of cube be x cm Here,

To find $\frac{dA}{dt}$ when x = 10 cm

We know that

$$V = x^{3}$$
$$\frac{dV}{dt} = 3x^{2} \left(\frac{dx}{dt}\right)$$
$$9 = 3(10)^{2} \frac{dx}{dt}$$
$$\frac{dx}{dt} = \frac{3}{100} \text{ cm/sec}$$

Now,
$$A = 6x^2$$

$$\frac{dA}{dt} = 12x \frac{dx}{dt}$$

$$= 12 (10) \left(\frac{3}{100}\right)$$

$$\frac{dA}{dt} = 3.6 \text{ cm}^2/\text{sec.}$$

Derivatives as a Rate Measurer Ex 13.2 Q29

Given,
$$\frac{dV}{dt}$$
 = 25 cm³/sec

To find
$$\frac{dA}{dt}$$
 when $r = 5$ cm

We know that,

$$V = \frac{4}{3}\pi r^{3}$$
$$\frac{dV}{dt} = \frac{4}{3}\pi \left(3r^{2}\right)\frac{dr}{dt}$$
$$25 = 4\pi \left(5\right)^{2}\frac{dr}{dt}$$
$$\frac{dr}{dt} = \frac{1}{4\pi} \text{ cm/sec}$$

Now,
$$A = 4\pi r^2$$

 $\frac{dA}{dt} = 8\pi r \frac{dr}{dt}$
 $= 8\pi (5) \left(\frac{1}{4\pi}\right)$

$$\frac{dA}{dt} = 10 \text{ cm}^2/\text{sec}.$$

Given,

$$\frac{dx}{dt} = -5 \text{ cm/min}$$

$$\frac{dy}{dt} = 4 \text{ cm/min}$$
(i) To find $\frac{dP}{dt}$ when $x = 8 \text{ cm}, y = 6 \text{ cm}$

$$P = 2(x + y)$$

$$\frac{dP}{dt} = 2\left(\frac{dx}{dt} + \frac{dy}{dt}\right)$$

$$= 2(-5 + 4)$$

$$\frac{dP}{dt} = -2 \text{ cm/min}$$

(ii) To find
$$\frac{dA}{dt}$$
 when x = 8 cm and y = 6 cm

$$A = xy
\frac{dA}{dt} = x \frac{dy}{dt} + y \frac{dx}{dt}
= (8)(4) + (6)(-5)
= 32 - 30$$

$$\frac{dA}{dt} = 2 \text{ cm}^2/\text{min}.$$

Derivatives as a Rate Measurer Ex 13.2 Q31

Let r be the radius of the given disc and A be its area.

Then,
$$A = \pi r^2$$

$$\therefore \frac{dA}{dt} = 2\pi r \frac{dr}{dt}$$
[by chain rule]

Now, the approximate increase of radius = $dr = \frac{dr}{dt} \Delta t = 0.05 \text{ cm}/\text{sec}$

 $\boldsymbol{\pi}$ the approximate rate of increase in areais given by

$$dA = \frac{dA}{dt} (\Delta t) = 2\pi r \left(\frac{dr}{dt} \Delta t\right) = 2\pi (3.2) (0.05) = 0.320\pi \text{ cm}^3 / \text{s}$$