

RD Sharma
Solutions Class
12 Maths
Chapter 31
Ex 31.3

Probability Ex 31.3 Q1

Given,

$$P(A) = \frac{7}{13}, P(B) = \frac{9}{13} \text{ and } P(A \cap B) = \frac{4}{13}$$

We know that,

$$\begin{aligned} P\left(\frac{A}{B}\right) &= \frac{P(A \cap B)}{P(B)} \\ &= \frac{\frac{4}{13}}{\frac{9}{13}} \\ &= \frac{4}{9} \end{aligned}$$

$$P\left(\frac{A}{B}\right) = \frac{4}{9}$$

Probability Ex 31.3 Q2

Given,

$$P(A) = 0.6, P(B) = 0.3 \text{ and } P(A \cap B) = 0.2$$

We know that,

$$P\left(\frac{A}{B}\right) = \frac{P(A \cap B)}{P(B)}$$
$$= \frac{0.2}{0.3}$$

$$P\left(\frac{A}{B}\right) = \frac{2}{3}$$

and, $P\left(\frac{B}{A}\right) = \frac{P(A \cap B)}{P(A)}$

$$= \frac{0.2}{0.6}$$

$$P\left(\frac{B}{A}\right) = \frac{1}{3}$$

$$P\left(\frac{A}{B}\right) = \frac{2}{3}, P\left(\frac{B}{A}\right) = \frac{1}{3}$$

Probability Ex 31.3 Q3

Given,

$$P(A \cap B) = 0.32 \text{ and } P(B) = 0.5$$

We know that,

$$P\left(\frac{A}{B}\right) = \frac{P(A \cap B)}{P(B)}$$
$$= \frac{0.32}{0.5}$$
$$= \frac{16}{25}$$
$$= 0.64$$

$$P\left(\frac{A}{B}\right) = 0.64$$

Probability Ex 31.3 Q4

Given,

$$P(A) = 0.4, P(B) = 0.8, P\left(\frac{B}{A}\right) = 0.6$$

We know that,

$$P\left(\frac{B}{A}\right) = \frac{P(A \cap B)}{P(A)}$$

$$0.6 = \frac{P(A \cap B)}{0.4}$$

$$P(A \cap B) = 0.6 \times 0.4$$

$$P(A \cap B) = 0.24$$

Now,
$$P\left(\frac{A}{B}\right) = \frac{P(A \cap B)}{P(B)}$$

$$= \frac{0.24}{0.8}$$

$$P\left(\frac{A}{B}\right) = 0.3$$

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$= 0.4 + 0.8 - 0.24$$

$$P(A \cup B) = 0.96$$

$$P\left(\frac{A}{B}\right) = 0.3, P(A \cup B) = 0.96$$

Probability Ex 31.3 Q5(i)

Given,

$$P(A) = \frac{1}{3}, P(B) = \frac{1}{4}, P(A \cup B) = \frac{5}{12}$$

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$\frac{5}{12} = \frac{1}{3} + \frac{1}{4} - P(A \cap B)$$

$$\begin{aligned} P(A \cap B) &= \frac{1}{3} + \frac{1}{4} - \frac{5}{12} \\ &= \frac{4+3-5}{12} \end{aligned}$$

$$P(A \cap B) = \frac{2}{12}$$

$$P\left(\frac{A}{B}\right) = \frac{P(A \cap B)}{P(B)}$$

$$= \frac{\frac{2}{12}}{\frac{1}{4}}$$

$$= \frac{2}{12} \times \frac{4}{1}$$

$$P\left(\frac{A}{B}\right) = \frac{2}{3}$$

$$P\left(\frac{B}{A}\right) = \frac{P(A \cap B)}{P(A)}$$

$$= \frac{\frac{2}{12}}{\frac{1}{3}}$$

$$= \frac{2}{12} \times \frac{3}{1}$$

$$P\left(\frac{B}{A}\right) = \frac{1}{2}$$

Hence,

$$P\left(\frac{A}{B}\right) = \frac{2}{3}$$

$$P\left(\frac{B}{A}\right) = \frac{1}{2}$$

Given,

$$P(A) = \frac{6}{11}, P(B) = \frac{5}{11} \text{ and } P(A \cup B) = \frac{7}{11}$$

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$P(A \cap B) = P(A) + P(B) - P(A \cup B)$$

$$= \frac{6}{11} + \frac{5}{11} - \frac{7}{11}$$

$$P(A \cap B) = \frac{4}{11}$$

We know that,

$$P\left(\frac{A}{B}\right) = \frac{P(A \cap B)}{P(B)}$$

$$= \frac{\frac{4}{11}}{\frac{5}{11}}$$

$$= \frac{4}{5}$$

$$P\left(\frac{B}{A}\right) = \frac{P(A \cap B)}{P(A)}$$

$$= \frac{\frac{4}{11}}{\frac{6}{11}}$$

$$= \frac{2}{3}$$

Hence,

$$P\left(\frac{A}{B}\right) = \frac{4}{5}, P\left(\frac{B}{A}\right) = \frac{2}{3}$$

Probability Ex 31.3 Q5(iii)

Given,

$$P(A) = \frac{7}{13}, P(B) = \frac{9}{13}, P(A \cap B) = \frac{4}{13}$$

Since, $P(A' \cap B) = P(B) - P(A \cap B)$

$$= \frac{9}{13} - \frac{4}{13}$$

$$P(A' \cap B) = \frac{5}{13}$$

$$P\left(\frac{A'}{B}\right) = \frac{P(A' \cap B)}{P(B)}$$

$$= \frac{\frac{5}{13}}{\frac{9}{13}}$$

$$= \frac{5}{9}$$

$$P\left(\frac{A'}{B}\right) = \frac{5}{9}$$

Probability Ex 31.3 Q5(iv)

$$P(A) = \frac{1}{2}, P(B) = \frac{1}{3} \text{ and } P(A \cap B) = \frac{1}{4},$$

$$P(A/B) = \frac{P(A \cap B)}{P(B)} = \frac{\frac{1}{4}}{\frac{1}{3}} = \frac{3}{4}$$

$$P(B/A) = \frac{P(B \cap A)}{P(A)} = \frac{\frac{1}{4}}{\frac{1}{2}} = \frac{1}{2}$$

$$P(\bar{A}/B) = \frac{P(B) - P(A \cap B)}{P(B)} = \frac{\frac{1}{3} - \frac{1}{4}}{\frac{1}{3}} = \frac{1}{4}$$

$$P(\bar{A}/\bar{B}) = \frac{P(\bar{A} \cap \bar{B})}{P(\bar{B})} = \frac{1 - P(A \cup B)}{P(A) - P(A \cap B)} = \frac{1 - P(A) - P(B) + P(A \cap B)}{P(A) - P(A \cap B)} = \frac{1 - \frac{1}{2} - \frac{1}{3} + \frac{1}{4}}{\frac{1}{2} - \frac{1}{4}} = \frac{5}{4}$$

Probability Ex 31.3 Q6

Given,

$$2P(A) = P(B) = \frac{5}{13}$$

$$2P(A) = \frac{5}{13}$$

$$\Rightarrow P(A) = \frac{5}{26}$$

$$P\left(\frac{A}{B}\right) = \frac{P(A \cap B)}{P(B)}$$

$$\frac{2}{5} = \frac{P(A \cap B)}{\frac{5}{13}}$$

$$P(A \cap B) = \frac{2}{5} \times \frac{5}{13}$$

$$P(A \cap B) = \frac{2}{13}$$

We know that,

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$= \frac{5}{26} + \frac{5}{13} - \frac{2}{13}$$

$$= \frac{5 + 10 - 4}{26}$$

$$= \frac{11}{26}$$

$$P(A \cup B) = \frac{11}{26}$$

Probability Ex 31.3 Q7

Given,

$$P(A) = \frac{6}{11}, P(B) = \frac{5}{11}, P(A \cup B) = \frac{7}{11}$$

(i)

$$\begin{aligned} \text{Since, } P(A \cap B) &= P(A) + P(B) - P(A \cup B) \\ &= \frac{6}{11} + \frac{5}{11} - \frac{7}{11} \end{aligned}$$

$$P(A \cap B) = \frac{4}{11}$$

(ii)

$$\begin{aligned} P\left(\frac{A}{B}\right) &= \frac{P(A \cap B)}{P(B)} \\ &= \frac{\frac{4}{11}}{\frac{5}{11}} \end{aligned}$$

$$P\left(\frac{A}{B}\right) = \frac{4}{5}$$

(iii)

$$\begin{aligned} P\left(\frac{B}{A}\right) &= \frac{P(A \cap B)}{P(A)} \\ &= \frac{\frac{4}{11}}{\frac{6}{11}} \end{aligned}$$

$$P\left(\frac{B}{A}\right) = \frac{2}{3}$$

Sample space for three coins is given by

$$\{HHH, HTH, THH, TTH, HHT, HTT, THT, TTT\}$$

(i)

A = Head on third toss

$$A = \{HHH, HTH, THH, TTH\}$$

B = Head on first two toss

$$B = \{HHH, HHT\}$$

$$(A \cap B) = \{HHH\}$$

$$P\left(\frac{A}{B}\right) = \frac{n(A \cap B)}{n(B)}$$

$$P\left(\frac{A}{B}\right) = \frac{1}{2}$$

Hence, $P\left(\frac{A}{B}\right) = \frac{1}{2}$

(ii)

A = At least two heads

$$A = \{HHH, HHT, HTH, THH\}$$

B = At most two heads

$$B = \{HHT, HTT, THT, TTT, HTH, THH, TTH\}$$

$$(A \cap B) = \{HHT, HTH, THH\}$$

$$P\left(\frac{A}{B}\right) = \frac{P(A \cap B)}{P(B)}$$

$$P\left(\frac{A}{B}\right) = \frac{3}{7}$$

Hence, $P\left(\frac{A}{B}\right) = \frac{3}{7}$

(iii)

A = At most two tails

$$A = \{HHH, HTH, THT, TTH, HHT, THT, HTT\}$$

B = At least one tail

$$B = \{HTH, THH, TTH, HHT, HTT, THT, TTT\}$$

$$(A \cap B) = \{HTH, THT, TTH, HHT, THT, HTT\}$$

$$\begin{aligned} P\left(\frac{A}{B}\right) &= \frac{P(A \cap B)}{P(B)} \\ &= \frac{6}{7} \end{aligned}$$

Hence, $P\left(\frac{A}{B}\right) = \frac{6}{7}$

Probability Ex 31.3 Q9

Sample space of two coins

$$\{HH, HT, TH, TT\}$$

(i)

A = Tail appears on one coin

$$A = \{HT, TH\}$$

B = One coin shows head

$$B = \{HT, TH\}$$

$$(A \cap B) = \{HT, TH\}$$

$$P\left(\frac{A}{B}\right) = \frac{P(A \cap B)}{P(B)}$$
$$= \frac{2}{2}$$

$$P\left(\frac{A}{B}\right) = 1$$

Hence, $P\left(\frac{A}{B}\right) = 1$

(ii)

A = No tail appears

$$A = \{HH\}$$

B = No head appears

$$B = \{TT\}$$

$$(A \cap B) = \{ \}$$

$$P\left(\frac{A}{B}\right) = \frac{P(A \cap B)}{P(B)}$$
$$= \frac{0}{1}$$
$$= 0$$

$$P\left(\frac{A}{B}\right) = 0$$

Die is thrown three times.

$A = 4$ appears on the third toss

$$A = \{(1, 1, 4), (1, 2, 4), (1, 3, 4), (1, 4, 4), (1, 5, 4), (1, 6, 4) \\ (2, 1, 4), (2, 2, 4), (2, 3, 4), (2, 4, 4), (2, 5, 4), (2, 6, 4) \\ (3, 1, 4), (3, 2, 4), (3, 3, 4), (3, 4, 4), (3, 5, 4), (3, 6, 4) \\ (4, 1, 4), (4, 2, 4), (4, 3, 4), (4, 4, 4), (4, 5, 4), (4, 6, 4) \\ (5, 1, 4), (5, 2, 4), (5, 3, 4), (5, 4, 4), (5, 5, 4), (5, 6, 4) \\ (6, 1, 4), (6, 2, 4), (6, 3, 4), (6, 4, 4), (6, 5, 4), (6, 6, 4)\}$$

$B = 6$ and 5 appear respectively on first two tosses

$$B = \{(6, 5, 1), (6, 5, 5), (6, 5, 3), (6, 5, 4), (6, 5, 5), (6, 5, 6)\}$$

$$(A \cap B) = \{(6, 5, 4)\}$$

$$P\left(\frac{A}{B}\right) = \frac{P(A \cap B)}{P(B)} \\ = \frac{1}{6}$$

$$P\left(\frac{B}{A}\right) = \frac{P(A \cap B)}{P(A)} \\ = \frac{1}{36}$$

Hence, $P\left(\frac{A}{B}\right) = \frac{1}{6}$, $P\left(\frac{B}{A}\right) = \frac{1}{36}$

Probability Ex 31.3 Q11

There are three person for photograph father (F), mother (M), son (S).

Sample space = $\{FMS, FSM, MFS, MSF, SFM, SMF\}$

A = Son on one end

$A = \{SFM, SMF, MFS, FMS\}$

B = Father in the middle

$B = \{MFS, SFM\}$

$(A \cap B) = \{MFS, SFM\}$

$$P\left(\frac{A}{B}\right) = \frac{P(A \cap B)}{P(B)}$$
$$= \frac{2}{2}$$

$$P\left(\frac{A}{B}\right) = 1$$

$$P\left(\frac{B}{A}\right) = \frac{P(A \cap B)}{P(A)}$$
$$= \frac{2}{4}$$

$$P\left(\frac{B}{A}\right) = \frac{1}{2}$$

Hence, $P\left(\frac{A}{B}\right) = 1$, $P\left(\frac{B}{A}\right) = \frac{1}{2}$

Probability Ex 31.3 Q12

The sample space of the experiment is $\{(1,1)(1,2)(1,3)\dots(6,6)\}$ consisting of 36 outcomes.

$$P(A) = P(\text{Sum} = 6) = \frac{5}{36}$$

$$P(B) = P(4 \text{ appears at least once}) = \frac{11}{36}$$

Now,
$$P\left(\frac{B}{A}\right) = \frac{P(A \text{ and } B)}{P(A)}$$
$$= \frac{P(\text{sum is 6 and 4 has appeared at least once})}{P(A)}$$
$$= \frac{2}{36}$$
$$= \frac{5}{36}$$
$$= \frac{2}{5}$$

Probability Ex 31.3 Q13

Two dice are thrown.

A = Sum on the dice is 8

$$A = \{(2, 6), (3, 5), (4, 4), (5, 3), (6, 2)\}$$

B = Second die always exhibits 4

$$B = \{(1, 4), (2, 4), (3, 4), (4, 4), (5, 4), (6, 4)\}$$

$$(A \cap B) = \{(4, 4)\}$$

$$\begin{aligned}P\left(\frac{A}{B}\right) &= \frac{n(A \cap B)}{n(B)} \\ &= \frac{1}{6}\end{aligned}$$

$$\text{Required probability} = \frac{1}{6}$$

Probability Ex 31.3 Q14

Here two dice are thrown

A = Getting 7 as sum on two dice

$$A = \{(1, 6), (2, 5), (3, 4), (4, 3), (5, 2), (6, 1)\}$$

B = Second die exhibits an odd number

$$\begin{aligned}B = \{(1, 1), (2, 1), (3, 1), (4, 1), (5, 1), (6, 1) \\ (1, 3), (2, 3), (3, 3), (4, 3), (5, 3), (6, 3) \\ (1, 5), (2, 5), (3, 5), (4, 5), (5, 5), (6, 5)\}\end{aligned}$$

$$(A \cap B) = \{(2, 5), (4, 3), (6, 1)\}$$

$$\begin{aligned}P\left(\frac{A}{B}\right) &= \frac{n(A \cap B)}{n(B)} \\ &= \frac{3}{18} \\ &= \frac{1}{6}\end{aligned}$$

$$\text{Hence, Required probability} = \frac{1}{6}$$

Probability Ex 31.3 Q15

A pair of dice is thrown.

A = Getting 7 as sum number on 2 dice.

$$A = \{(1, 6), (2, 5), (3, 4), (4, 3), (5, 2), (6, 1)\}$$

B = Second die always exhibits prime number

$$B = \{(1, 2), (2, 2), (3, 2), (4, 2), (5, 2), (6, 2)$$

$$(1, 3), (2, 3), (3, 3), (4, 3), (5, 3), (6, 3)$$

$$(1, 5), (2, 5), (3, 5), (4, 5), (5, 5), (6, 5)\}$$

[Since, there are 2, 3, 5 prime number on a die]

$$(A \cap B) = \{(2, 5), (4, 3), (5, 2)\}$$

$$\begin{aligned}P\left(\frac{A}{B}\right) &= \frac{n(A \cap B)}{n(B)} \\ &= \frac{3}{18} \\ &= \frac{1}{6}\end{aligned}$$

Hence, Required probability = $\frac{1}{6}$

Probability Ex 31.3 Q16

A die is rolled.

A = A prime number on die

$$A = \{2, 3, 5\}$$

B = An odd number on die

$$B = \{1, 3, 5\}$$

$$(A \cap B) = \{3, 5\}$$

$$\begin{aligned}P\left(\frac{A}{B}\right) &= \frac{n(A \cap B)}{n(B)} \\ &= \frac{2}{3}\end{aligned}$$

Required probability = $\frac{2}{3}$

Probability Ex 31.3 Q17

A pair of dice is thrown

A = Getting sum 8 or more

= Getting sum 8,9,10,11 or 12 on the pair of dice

$$A = \{(2, 6), (3, 5), (4, 4), (5, 3), (6, 2), (3, 6), \\ (4, 5), (5, 4), (6, 3), (4, 6), (5, 5), (6, 4), \\ (5, 6), (6, 5), (6, 6)\}$$

B = 4 on first die

$$B = \{(4, 1), (4, 2), (4, 3), (4, 4), (4, 5), (4, 6)\}$$

$$(A \cap B) = \{(4, 4), (4, 5), (4, 6)\}$$

$$P\left(\frac{A}{B}\right) = \frac{n(A \cap B)}{n(B)} \\ = \frac{3}{6} \\ = \frac{1}{2}$$

$$\text{Required probability} = \frac{1}{2}$$

Probability Ex 31.3 Q18

Two dice are thrown

A = Sum of the numbers on dice is 8

$$A = \{(2, 6), (3, 5), (4, 4), (5, 3), (6, 2)\}$$

B = At least one die does not show five

$$B = \{(1, 1), (1, 2), (1, 3), (1, 4), (1, 6), (2, 1), (2, 2), \\ (2, 3), (2, 4), (2, 6), (3, 1), (3, 2), (3, 3), (3, 4), \\ (3, 6), (4, 1), (4, 2), (4, 3), (4, 4), (4, 6), (6, 1), \\ (6, 2), (6, 3), (6, 4), (6, 6)\}$$

$$(A \cap B) = \{(2, 6), (4, 6), (6, 2)\}$$

$$P\left(\frac{A}{B}\right) = \frac{n(A \cap B)}{n(B)} \\ = \frac{3}{25}$$

$$\text{Required probability} = \frac{3}{25}$$

Probability Ex 31.3 Q19

Two numbers are selected at random from integers 1 through 9.

A = Both numbers are odd

$$A = \{(3, 1), (5, 1), (7, 1), (9, 1), (3, 5), (3, 7), (9, 3), (5, 3), (5, 7), (5, 9), (7, 3), (7, 5), (7, 9), (9, 3), (9, 5), (9, 7)\}$$

B = Sum of both numbers is even

= Sum of both numbers is 2, 4, 6, 8, 10, 12, 14, 16 or 18

$$= \{(1, 3), (1, 5), (2, 4), (1, 7), (2, 6), (3, 5), (1, 9), (2, 8), (3, 7), (4, 6), (7, 5), (8, 4), (9, 3), (8, 6), (9, 5), (9, 7)\}$$

$$(A \cap B) = \{(1, 3), (1, 5), (1, 7), (3, 5), (1, 9), (3, 7), (7, 5), (9, 3), (9, 5), (9, 7)\}$$

$$P\left(\frac{A}{B}\right) = \frac{n(A \cap B)}{n(B)}$$
$$= \frac{10}{16}$$

$$\text{Required probability} = \frac{5}{8}$$

Probability Ex 31.3 Q20

A die is thrown twice

A = The number 5 has appeared at least once

$$A = \{(1, 5), (2, 5), (3, 5), (4, 5), (5, 5), (6, 5), (5, 1), (5, 2), (5, 3), (5, 4), (5, 6)\}$$

B = Sum of the numbers is 8

$$= \{(2, 6), (3, 5), (4, 4), (5, 3), (6, 2)\}$$

$$(A \cap B) = \{(3, 5), (5, 3)\}$$

$$P\left(\frac{A}{B}\right) = \frac{n(A \cap B)}{n(B)}$$
$$= \frac{2}{5}$$

$$\text{Required probability} = \frac{2}{5}$$

Probability Ex 31.3 Q21

Two dice are thrown

A = Sum of the numbers showing on the dice is 7

$$A = \{(1, 6), (2, 5), (3, 4), (4, 3), (5, 2), (6, 1)\}$$

B = First die shows a 6

$$= \{(6, 1), (6, 2), (6, 3), (6, 4), (6, 5), (6, 6)\}$$

$$(A \cap B) = \{(6, 1)\}$$

$$\begin{aligned}P\left(\frac{A}{B}\right) &= \frac{n(A \cap B)}{n(B)} \\ &= \frac{1}{6}\end{aligned}$$

$$\text{Required probability} = \frac{1}{6}$$

Probability Ex 31.3 Q22

A pair of die is thrown

E = Sum is greater than or equal to 10

$$= \{(4, 6), (5, 5), (6, 4), (5, 6), (6, 5), (6, 6)\}$$

Case I:

F = 5 appears on first die

$$= \{(5, 1), (5, 2), (5, 3), (5, 4), (5, 5), (5, 6)\}$$

$$E \cap F = \{(5, 5), (5, 6)\}$$

$$\begin{aligned}P\left(\frac{E}{F}\right) &= \frac{n(E \cap F)}{n(F)} \\ &= \frac{2}{6}\end{aligned}$$

$$P\left(\frac{E}{F}\right) = \frac{1}{3}$$

Case II:

F = 5 appears on at least one die

$$= \{(1, 5), (2, 5), (3, 5), (4, 5), (6, 5), (5, 1), (5, 2), (5, 3), (5, 4), (5, 5), (5, 6)\}$$

$$E \cap F = \{(5, 5), (5, 6), (6, 5)\}$$

$$\begin{aligned}P\left(\frac{E}{F}\right) &= \frac{n(E \cap F)}{n(F)} \\ &= \frac{3}{11}\end{aligned}$$

$$P\left(\frac{E}{F}\right) = \frac{3}{11}$$

Probability Ex 31.3 Q23

Given,

Probability to pass mathematics (M)

$$P(M) = \frac{4}{5}$$

Probability to pass in mathematics (M) and computer Science (C)

$$P(M \cap C) = \frac{1}{2}$$

To find, $P\left(\frac{C}{M}\right)$

We know that,

$$\begin{aligned} P\left(\frac{C}{M}\right) &= \frac{P(M \cap C)}{P(M)} \\ &= \frac{\frac{1}{2}}{\frac{4}{5}} \\ &= \frac{1}{2} \times \frac{5}{4} \\ &= \frac{5}{8} \end{aligned}$$

Required probability = $\frac{5}{8}$

Given,

$$\text{Probability that a person buys a shirt } (S) = P(S) = 0.2$$

$$\text{Probability that he buys a trouser } (T) = P(T) = 0.3$$

$$P\left(\frac{S}{T}\right) = 0.4$$

We know that,

$$P\left(\frac{S}{T}\right) = \frac{P(S \cap T)}{P(T)}$$

$$0.4 = \frac{P(S \cap T)}{0.3}$$

$$P(S \cap T) = 0.4 \times 0.3$$

$$P(S \cap T) = 0.12$$

Probability that he buys a shirt and a trouser both = 0.12

$$P\left(\frac{T}{S}\right) = \frac{P(S \cap T)}{P(S)}$$

$$= \frac{0.12}{0.2}$$

$$P\left(\frac{T}{S}\right) = \frac{12}{20}$$

$$= \frac{3}{5}$$

$$= 0.6$$

Probability that he buys a trouser given that he buys a shirt = 0.6

Probability Ex 31.3 Q25

Total students = 1000

Number of girls = 430

% of girls in class XII = 10%

Let A = Student chosen studies in class XII

B = Student chosen is a girl

$$\text{Then } P(B) = \frac{430}{1000}$$

$$P(A \cap B) = \frac{43}{1000}$$

$$\therefore P\left(\frac{A}{B}\right) = \frac{P(A \cap B)}{P(B)} = \frac{43}{430} = \frac{1}{10}$$

Probability Ex 31.3 Q26

Total no. of cards = 10

Let A = drawn number is more than 3

B = drawn number is even

$$P\left(\frac{B}{A}\right) = \frac{P(B \cap A)}{P(A)}$$

Now $P(A) = \frac{7}{10}$

$$P(A \cap B) = \frac{4}{10}$$

$$\therefore P\left(\frac{B}{A}\right) = \frac{4}{7}$$

Probability Ex 31.3 Q27

(i) Let 'A' be the event that both the children born are girls.

Let 'B' be the event that the youngest is a girl.

We have to find conditional probability $P(A/B)$.

$$P(A/B) = \frac{P(A \cap B)}{P(B)}$$

$$A \subset B \Rightarrow A \cap B = A$$

$$\Rightarrow P(A \cap B) = P(A) = P(GG) = \frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$$

$$P(B) = P(BG) + P(GG) = \frac{1}{2} \times \frac{1}{2} + \frac{1}{2} \times \frac{1}{2} = \frac{1}{4} + \frac{1}{4} = \frac{1}{2}$$

$$\text{Hence, } P(A/B) = \frac{1/4}{1/2} = \frac{1}{2}$$

(ii) Let 'A' be the event that both the children born are girls.

Let 'B' be the event that at least one is a girl.

We have to find the conditional probability $P(A/B)$.

$$P(A/B) = \frac{P(A \cap B)}{P(B)}$$

$$A \subset B \Rightarrow A \cap B = A$$

$$\Rightarrow P(A \cap B) = P(A) = P(GG) = \frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$$

$$P(B) = 1 - P(BB) = 1 - \frac{1}{2} \times \frac{1}{2} = 1 - \frac{1}{4} = \frac{3}{4}$$

$$\text{Hence, } P(A/B) = \frac{1/4}{3/4} = \frac{1}{3}$$