

RD Sharma
Solutions
Class 11 Maths
Chapter 2
Ex 2.3

RD Sharma Class 11 Solutions Chapter 2 Relations Ex 2.3 Q1

(i) We have,

$$A = \{1, 2, 3\} \text{ and } B = \{4, 5, 6\}$$

$\{(1, 6), (3, 4), (5, 2)\}$ is not a relation from A to B as it is not a subset of $A \times B$.

(ii) We have,

$$A = \{1, 2, 3\} \text{ and } B = \{4, 5, 6\}$$

$\{(1, 5), (2, 6), (3, 4), (3, 6)\}$ is a subset of $A \times B$, so it is a relation from A to B .

(iii) We have,

$$A = \{1, 2, 3\} \text{ and } B = \{4, 5, 6\}$$

$\{(4, 2), (4, 3), (5, 1)\}$ is not a relation from A to B as it is not a subset of $A \times B$.

(iv) We have,

$$A = \{1, 2, 3\} \text{ and } B = \{4, 5, 6\}$$

$A \times B$ is a relation from A to B .

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q2

We have,

$$A = \{2, 3, 4, 5\} \text{ and } B = \{3, 6, 7, 10\}$$

It is given that $(x, y) \in R \Leftrightarrow x$ is relatively prime to y

$$\therefore (2, 3) \in R, (2, 7) \in R, (3, 7) \in R, (3, 10) \in R, (4, 3) \in R, (4, 7) \in R, (5, 3) \in R, \text{ and } (5, 7) \in R$$

Thus,

$$R = \{(2, 3), (2, 7), (3, 7), (3, 10), (4, 3), (4, 7), (5, 3), (5, 7)\}$$

Clearly, Domain $(R) = \{2, 3, 4, 5\}$ and Range $= \{3, 7, 10\}$.

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q3

We have,

$$A = \{1, 2, 3, 4, 5\} \quad [\because A \text{ is the set of first five natural number}]$$

It is given that R be a relation on A defined as $(x, y) \in R \Leftrightarrow x \leq y$

For the elements of the given sets A and A , we find that

$$1 = 1, 1 < 2, 1 < 3, 1 < 4, 1 < 5, 2 = 2, 2 < 3, 2 < 4, 2 < 5, 3 = 3, 3 < 4, 3 < 5, 4 = 4, 4 < 5, \text{ and } 5 = 5$$

$$\therefore (1, 1) \in R, (1, 2) \in R, (1, 3) \in R, (1, 4) \in R, (1, 5) \in R, (2, 2) \in R, (2, 3) \in R, (2, 4) \in R, (2, 5) \in R, \\ (3, 3) \in R, (3, 4) \in R, (3, 5) \in R, (4, 4) \in R, (4, 5) \in R, \text{ and } (5, 5) \in R$$

Thus,

$$R = \left\{ (1, 1), (1, 2), (1, 3), (1, 4), (1, 5), (2, 2), (2, 3), (2, 4), (2, 5), (3, 3), (3, 4), (3, 5), (4, 4), (4, 5), (5, 5) \right\}$$

Also,

$$R^{-1} = \left\{ (1, 1), (2, 1), (3, 1), (4, 1), (5, 1), (2, 2), (3, 2), (4, 2), (5, 2), (3, 3), (4, 3), (5, 3), (4, 4), (5, 4), (5, 5) \right\}$$

$$(i) \text{ Domain}(R^{-1}) = \{1, 2, 3, 4, 5\}$$

$$(ii) \text{ Range}(R) = \{1, 2, 3, 4, 5\}$$

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q4

(i) We have,

$$R = \{(1, 2), (1, 3), (2, 3), (3, 2), (5, 6)\}$$

$$\Rightarrow R^{-1} = \{(2, 1), (3, 1), (3, 2), (2, 3), (6, 5)\}$$

(ii) We have,

$$R = \{(x, y) : x, y \in N, x + 2y = 8\}$$

Now,

$$x + 2y = 8$$

$$\Rightarrow x = 8 - 2y$$

Putting $y = 1, 2, 3$ we get $x = 6, 4, 2$ respectively.

For $y = 4$, we get $x = 0 \notin N$. Also for $y > 4$, $x \notin N$

$$\therefore R = \{(6, 1), (4, 2), (2, 3)\}$$

Thus,

$$R^{-1} = \{(1, 6), (2, 4), (3, 2)\}$$

$$\Rightarrow R^{-1} = \{(3, 2), (2, 4), (1, 6)\}$$

(iii) We have,

$$R \text{ is a relation from } \{11, 12, 13\} \text{ to } \{8, 10, 12\} \text{ defined by } y = x - 3$$

Now,

$$y = x - 3$$

Putting $x = 11, 12, 13$ we get $y = 8, 9, 10$ respectively

$$\Rightarrow (11, 8) \in R, (12, 9) \in R \text{ and } (13, 10) \in R$$

Thus,

$$R = \{(11, 8), (13, 10)\}$$

$$\Rightarrow R^{-1} = \{(8, 11), (10, 13)\}$$

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q5

(i) We have,
 $x = 2y$

Putting $y = 1, 2, 3$ we get $x = 2, 4, 6$ respectively.

$$\therefore R = \{(2,1), (4,2), (6,3)\}$$

(ii) We have,

It is given that relation R on the set $\{1, 2, 3, 4, 5, 6, 7\}$ defined by $(x, y) \in R \Leftrightarrow x$ is relatively prime to y .

$$\therefore \begin{aligned} & \{(2,3) \in R, (2,5) \in R, (2,7) \in R, (3,2) \in R, (3,4) \in R, (3,5) \in R, (3,7) \in R, (4,3) \in R, (4,5) \in R, \\ & (4,7) \in R, (5,2) \in R, (5,3) \in R, (5,4) \in R, (5,6) \in R, (5,7) \in R, (6,5) \in R, (6,7) \in R, (7,2) \in R, \\ & (7,3) \in R, (7,4) \in R, (7,5) \in R \text{ and } (7,6) \in R. \end{aligned}$$

Thus,

$$R = \{(2,3), (2,5), (2,7), (3,2), (3,4), (3,5), (3,7), (4,3), (4,5), (4,7), (5,2), (5,3), (5,4), (5,6), (5,7), (6,5), (6,7), (7,2), (7,3), (7,4), (7,5), (7,6)\}$$

(iii) We have,

$$\begin{aligned} & 2x + 3y = 12 \\ \Rightarrow & 2x = 12 - 3y \\ \Rightarrow & x = \frac{12 - 3y}{2} \end{aligned}$$

Putting $y = 0, 2, 4$ we get $x = 6, 3, 0$ respectively.

For $y = 1, 3, 5, 6, 7, 8, 9, 10$, $x \notin$ given set

$$\begin{aligned} \therefore R &= \{(6,0), (3,2), (0,4)\} \\ &= \{(0,4), (3,2), (6,0)\} \end{aligned}$$

(iv) We have,

$$A = \{5, 6, 7, 8\} \text{ and } B = \{10, 12, 15, 16, 18\}$$

Now,

a/b stands for 'a divides b'. For the elements of the given set A and B , we find that $5/10, 5/15, 6/12, 6/18$ and $8/16$

$$\therefore \{(5,10) \in R, (5,15) \in R, (6,12) \in R, (6,18) \in R, \text{ and } (8,16) \in R\}$$

Thus,

$$R = \{(5,10), (5,15), (6,12), (6,18), (8,16)\}$$

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q6

We have,

$$(x, y) \in R \Leftrightarrow x + 2y = 8$$

Now,

$$\begin{aligned} & x + 2y = 8 \\ \Rightarrow & x = 8 - 2y \end{aligned}$$

Putting $y = 1, 2, 3$, we get $x = 6, 4, 2$ respectively

For $y = 4$, we get $x = 0 \notin N$

Also, for $y > 4$, $x \notin N$

$$\therefore R = \{(6,1), (4,2), (2,3)\}$$

Thus,

$$\begin{aligned} & R^{-1} = \{(1,6), (2,4), (3,2)\} \\ \Rightarrow & R^{-1} = \{(3,2), (2,4), (1,6)\} \end{aligned}$$

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q7

We have,

$$A = \{3, 5\}, \quad B = \{7, 11\}$$

and, $R = \{(a, b) : a \in A, b \in B, a - b \text{ is odd}\}$

For the elements of the given sets A and B , we find that

$$3 - 7 = -4, \quad 3 - 11 = -8, \quad 5 - 7 = -2 \text{ and } 5 - 11 = -6$$

$$\therefore (3,7) \notin R, (3,11) \notin R, (5,7) \notin R \text{ and } (5,11) \notin R,$$

Thus, R is an empty relation from A into B .

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q8

We have,

$$A = \{1, 2\} \text{ and } B = \{3, 4\}$$

$$\therefore n(A) = 2 \text{ and } n(B) = 2$$

$$\Rightarrow n(A) \times n(B) = 2 \times 2 = 4$$

$$\Rightarrow n(A \times B) = 4$$

$$[\because n(A \times B) = n(A) \times n(B)]$$

So, there are $2^4 = 16$ relations from A to B .

$$\left[\begin{array}{l} \because n(x) = a, n(y) = b \\ \Rightarrow \text{Total number of relations} = 2^{ab} \end{array} \right]$$

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q9

(i) We have,

$$R = \{(x, x+5) : x \in \{0, 1, 2, 3, 4, 5\}\}$$

For the elements of the given sets, we find that

$$R = \{(0, 5), (1, 6), (2, 7), (3, 8), (4, 9), (5, 10)\}$$

Clearly, $\text{Domain}(R) = \{0, 1, 2, 3, 4, 5\}$ and $\text{Range}(R) = \{5, 6, 7, 8, 9, 10\}$

(ii) We have,

$$R = \{(x, x^3) : x \text{ is a prime number less than } 10\}$$

For the elements of the given sets, we find that

$$x = 2, 3, 5, 7$$

$$\therefore (2, 8) \in R, (3, 27) \in R, (5, 125) \in R \text{ and } (7, 343) \in R$$

$$\Rightarrow R = \{(2, 8), (3, 27), (5, 125), (7, 343)\}$$

Clearly, $\text{Domain}(R) = \{2, 3, 5, 7\}$ and $\text{Range}(R) = \{8, 27, 125, 343\}$

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q10

(i) We have,

$$R = \{(a, b) : a \in N, a < 5, b = 4\}$$

$$\Rightarrow a = 1, 2, 3, 4 \text{ and } b = 4$$

$$\text{Thus, } R = \{(1, 4), (2, 4), (3, 4), (4, 4)\}$$

Clearly, $\text{Domain}(R) = \{1, 2, 3, 4\}$ and $\text{Range}(R) = \{4\}$

(ii) We have,

$$S = \{(a, b) : b = |a - 1|, a \in Z \text{ and } |a| \leq 3\}$$

$$\Rightarrow a = -3, -2, -1, 0, 1, 2, 3$$

For $a = -3, -2, -1, 0, 1, 2, 3$ we get

$$b = 4, 3, 2, 1, 0, 1, 2 \text{ respectively}$$

$$\text{Thus, } S = \{(-3, 4), (-2, 3), (-1, 2), (0, 1), (1, 0), (2, 1), (3, 2)\}$$

$\text{Domain}(S) = \{-3, -2, -1, 0, 1, 2, 3\}$ and

$$\text{Range}(S) = \{0, 1, 2, 3, 4\}$$

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q11

Here, $A = \{a, b\}$

we know that,

$$\text{Number of relations} = 2^{n \times n}$$

$$= 2^{2 \times 2}$$

$$= 2^4$$

$$= 16$$

Number of relations on $A = 16$

Relations on A are given by

$$R = \{a, a\}, \{a, b\}, \{b, a\}, \{b, b\}$$

$$\{(a, a), (a, b)\}, \{(a, a), (b, a)\}, \{(a, a), (b, b)\},$$

$$\{(a, b), (b, a)\}, \{(a, b), (b, b)\}, \{(b, a), (b, b)\},$$

$$\{(a, a), (a, b), (b, a)\}, \{(a, b), (b, a), (b, b)\},$$

$$\{(b, a), (b, b), (a, a)\}, \{(b, b), (a, a), (a, b)\},$$

$$\{(a, a), (b, a), (b, b)\}, \{(a, a), (b, a), (b, b)\}$$

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q12

We have,

$$A = \{x, y, z\} \text{ and } B = \{a, b\}$$

$$\Rightarrow n(A) = 3 \text{ and } n(B) = 2$$

$$\Rightarrow n(A) \times n(B) = 3 \times 2 = 6$$

$$\Rightarrow n(A \times B) = 6$$

$$[\because n(A \times B) = n(A) \times n(B)]$$

So, there are $2^6 = 64$ relations from A to B .

$$\left[\begin{array}{l} \because n(x) = a, n(y) = b \\ \Rightarrow \text{Total number of relations} = 2^{ab} \end{array} \right]$$

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q13

We have,

$$R = \{a, b\} : a, b \in \mathbb{N} \text{ and } a = b^2$$

(i) This statement is not true because $(5, 5) \notin R$.

(ii) This statement is not true because $(25, 5) \in R$ but $(5, 25) \notin R$.

(iii) This statement is not true because $(36, 6) \in R$ and $(25, 5) \in R$ but $(36, 5) \notin R$.

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q14

We have,

$$3x - y = 0$$

$$\Rightarrow 3x = y$$

$$\Rightarrow y = 3x$$

Putting $x = 1, 2, 3, 4$ we get, $y = 3, 6, 9, 12$ respectively

For $x > 4$, we get $y > 14$ which does not belong to set A .

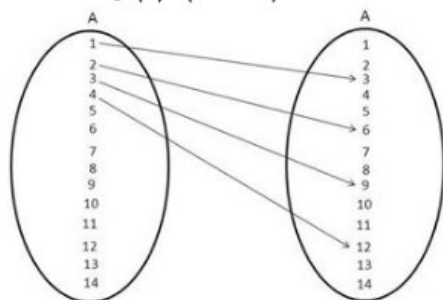
$$\therefore R = \{(1, 3), (2, 6), (3, 9), (4, 12)\}$$

The arrow diagram representing R is as follows:

Clearly, $\text{Domain}(R) = \{1, 2, 3, 4\}$,

$\text{Co-domain}(R) = \{1, 2, 3, 4, \dots, 14\}$ and

$\text{Range}(R) = \{3, 6, 9, 12\}$



Class 11 Solutions Chapter 2 Relations Ex 2.3 Q15

We have,

$$R = \{(x, y) : y = x + 5, x \text{ is a natural number less than } 4, x, y \in \mathbb{N}\}$$

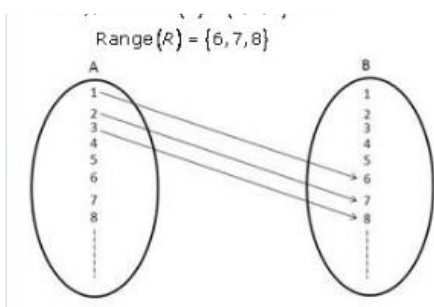
(i) Putting $x = 1, 2, 3$ we get, $y = 6, 7, 8$ respectively

\therefore Relation R in roster form is

$$R = \{(1, 6), (2, 7), (3, 8)\}$$

(ii) The arrow diagram representing R is as follows:

Clearly, $\text{Domain}(R) = \{1, 2, 3\}$ and



Class 11 Solutions Chapter 2 Relations Ex 2.3 Q16

We have,

$$A = \{1, 2, 3, 5\} \text{ and } B = \{4, 6, 9\}$$

It is given that,

$$R = \{(x, y) : \text{the difference between } x \text{ and } y \text{ is odd, } x \in A, y \in B\}$$

For the elements of the given sets A and B , we find that

$$(1, 4) \in R, (1, 6) \in R, (2, 9) \in R, (3, 4) \in R, (3, 6) \in R, (5, 4) \in R \text{ and } (5, 6) \in R$$

$$\therefore R = \{(1, 4), (1, 6), (2, 9), (3, 4), (3, 6), (5, 4), (5, 6)\}$$

Hence, relation R in roster form is $\{(1, 4), (1, 6), (2, 9), (3, 4), (3, 6), (5, 4), (5, 6)\}$

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q17

We have,

$$R = \{(x, x^3) : x \text{ is a prime number less than } 10\}$$

For the elements of the given sets, we find that

$$x = 2, 3, 5, 7$$

$$\therefore (2, 8) \in R, (3, 27) \in R, (5, 125) \in R \text{ and } (7, 343) \in R$$

$$\therefore \text{Relation } R \text{ in roster form is } = \{(2, 8), (3, 27), (5, 125), (7, 343)\}$$

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q18

We have,

$$A = \{1, 2, 3, 4, 5, 6\}$$

and, $R = \{(a, b) : a, b \in A, b \text{ is exactly divisible by } a\}$

(i) Now, a/b stands for 'a divides b'. For the elements of the given sets A and A , we find that

$$1/1, 1/2, 1/3, 1/4, 1/5, 1/6, 2/2, 2/4, 2/6, 3/3, 3/6, 4/4, 5/5, 6/6$$

\therefore Relation R in roster form is

$$R = \{(1, 1), (1, 2), (1, 3), (1, 4), (1, 5), (1, 6), (2, 2), (2, 4), (2, 6), (3, 3), (3, 6), (4, 4), (5, 5), (6, 6)\}$$

(ii) Domain $\{R\} = \{1, 2, 3, 4, 5, 6\}$

(iii) Range $\{R\} = \{1, 2, 3, 4, 5, 6\}$

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q19

(i) Set builder form of the relation from P to Q is

$$R = \{(x, y) : y = x - 2, x \in P, y \in Q\}$$

(ii) Roster form of the relation from P to Q is

$$R = \{(5, 3), (6, 4), (7, 5)\}$$

$$\text{Domain}\{R\} = \{5, 6, 7\}$$

$$\text{Range}\{R\} = \{3, 4, 5\}$$

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q20

We have,

$$R = \{(a, b) : a, b \in Z, a - b \text{ is an integer}\}$$

Clearly, Domain $\{R\} = Z$

$$\text{Range}(R) = z.$$

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q21

$$\text{Let } \left(1, \frac{-1}{2}\right) \in R_1 \text{ and } \left(\frac{-1}{2}, -4\right) \in R_1$$

$$\Rightarrow 1 + 1 \times \frac{-1}{2} > 0 \text{ and } 1 + \left(\frac{-1}{2}\right) - 4 > 0$$

$$\text{But, } 1 + 1 \times (-4) = 1 - 4 \\ = -3 < 0$$

$$\text{So, } (1, -4) \notin R_1$$

Class 11 Solutions Chapter 2 Relations Ex 2.3 Q22

We have,

$$(a, b)R(c, d) \Leftrightarrow a + d = b + c \text{ for all } (a, b), (c, d) \in N \times N$$

(i) We have,

$$a + b = b + a \text{ for all } a, b \in N$$

$$\therefore (a, b)R(a, b) \text{ for all } a, b \in N$$

(ii) Now,

$$(a, b)R(c, d)$$

$$\Rightarrow a + d = b + c$$

$$\Rightarrow c + b = d + a$$

$$\Rightarrow (c, d)R(a, b)$$

(iii) Now,

$$(a, b)R(c, d) \text{ and } (c, d)R(e, f)$$

$$\Rightarrow a + d = b + c \text{ and } c + f = d + e$$

$$\Rightarrow a + d + c + f = b + c + d + e$$

[Adding]

$$\Rightarrow a + f = b + e$$

$$\Rightarrow (a, b)R(e, f)$$