

RD SHARMA
Solutions
Class 10 Maths
Chapter 5
Ex 5.2

Evaluate each of the following:

Q 1 . $\sin 45^\circ 45^\circ \sin 30^\circ 30^\circ + \cos 45^\circ 45^\circ \cos 30^\circ 30^\circ$

Solution:

$$\sin 45^\circ 45^\circ \sin 30^\circ 30^\circ + \cos 45^\circ 45^\circ \cos 30^\circ 30^\circ$$

[1]

We know that by trigonometric ratios we have ,

$$\sin 45^\circ = \frac{1}{\sqrt{2}} \quad \sin 30^\circ = \frac{1}{2}$$

$$\cos 45^\circ = \frac{1}{\sqrt{2}} \quad \cos 30^\circ = \frac{\sqrt{3}}{2}$$

Substituting the values in equation 1 , we get

$$1 \cdot \frac{1}{\sqrt{2}} \cdot \frac{1}{2} + 1 \cdot \frac{1}{\sqrt{2}} \cdot \frac{\sqrt{3}}{2}$$

$$= \frac{1}{\sqrt{2}} \cdot \frac{1}{2} + \frac{\sqrt{3}}{2\sqrt{2}}$$

$$= \frac{1 + \sqrt{3}}{2\sqrt{2}}$$

Q 2 . $\sin 60^\circ 60^\circ \cos 30^\circ 30^\circ + \cos 60^\circ 60^\circ \sin 30^\circ 30^\circ$

Solution:

$$\sin 60^\circ 60^\circ \cos 30^\circ 30^\circ + \cos 60^\circ 60^\circ \sin 30^\circ 30^\circ$$

[1]

By trigonometric ratios we have ,

$$\sin 60^\circ = \frac{\sqrt{3}}{2} \quad \sin 30^\circ = \frac{1}{2}$$

$$\cos 30^\circ = \frac{\sqrt{3}}{2} \quad \cos 60^\circ = \frac{1}{2}$$

Substituting the values in equation 1 , we get

$$= \frac{\sqrt{3}}{2} \cdot \frac{\sqrt{3}}{2} + \frac{1}{2} \cdot \frac{1}{2}$$

$$= \frac{3}{4} + \frac{1}{4} = 1$$

Q 3 . $\cos 60^\circ \cos 45^\circ - \sin 60^\circ \sin 45^\circ$

Solution:

$$\cos 60^\circ \cos 45^\circ - \sin 60^\circ \sin 45^\circ \quad [1]$$

We know that by trigonometric ratios we have ,

$$\cos 60^\circ = \frac{1}{2}$$

$$\cos 45^\circ = \frac{1}{\sqrt{2}}$$

$$\sin 60^\circ = \frac{\sqrt{3}}{2}$$

$$\sin 45^\circ = \frac{1}{\sqrt{2}}$$

Substituting the values in equation 1 , we get

$$\begin{aligned} & 1 \cdot \frac{1}{\sqrt{2}} - \frac{\sqrt{3}}{2} \cdot \frac{1}{\sqrt{2}} - \frac{\sqrt{3}}{2} \cdot \frac{1}{\sqrt{2}} \\ &= 1 - \frac{\sqrt{3}}{\sqrt{2}} - \frac{\sqrt{3}}{\sqrt{2}} \end{aligned}$$

Q.4: $\sin^2 30^\circ + \sin^2 45^\circ + \sin^2 60^\circ + \sin^2 90^\circ$

Solution:

$$\sin^2 30^\circ + \sin^2 45^\circ + \sin^2 60^\circ + \sin^2 90^\circ \quad [1]$$

We know that by trigonometric ratios we have ,

$$\sin 30^\circ = \frac{1}{2}$$

$$\sin 45^\circ = \frac{1}{\sqrt{2}}$$

$$\sin 60^\circ = \frac{\sqrt{3}}{2} \quad \sin 90^\circ = 1$$

Substituting the values in equation 1 , we get

$$\begin{aligned} &= \left[\frac{1}{2}\right]^2 + \left[\frac{1}{\sqrt{2}}\right]^2 + \left[\frac{\sqrt{3}}{2}\right]^2 + 1 \\ &= 14 + 12 + 34 + 1 \frac{1}{4} + \frac{1}{2} + \frac{3}{4} + 1 \\ &= 52 \frac{5}{4} \end{aligned}$$

Q 5. $\cos^2 30^\circ + \cos^2 45^\circ + \cos^2 60^\circ + \cos^2 90^\circ$

Solution:

$$\cos^2 30^\circ + \cos^2 45^\circ + \cos^2 60^\circ + \cos^2 90^\circ \cos^2 30^\circ + \cos^2 45^\circ + \cos^2 60^\circ + \cos^2 90^\circ \quad [1]$$

We know that by trigonometric ratios we have ,

$$\cos 30^\circ = \frac{\sqrt{3}}{2} \cos 30^\circ = \frac{\sqrt{3}}{2} \quad \cos 45^\circ = \frac{1}{\sqrt{2}} \cos 45^\circ = \frac{1}{\sqrt{2}}$$

$$\cos 60^\circ = \frac{1}{2} \cos 60^\circ = \frac{1}{2} \quad \cos 90^\circ \cos 90^\circ = 0$$

Substituting the values in equation 1 , we get

$$[\frac{\sqrt{3}}{2}]^2 + [1 \cdot \frac{1}{\sqrt{2}}]^2 + [1 \cdot \frac{1}{2}]^2 + 0[\frac{\sqrt{3}}{2}]^2 + [\frac{1}{\sqrt{2}}]^2 + [\frac{1}{2}]^2 + 0$$

$$= 34 + 12 + 14 \frac{3}{4} + \frac{1}{2} + \frac{1}{4}$$

$$= 32 \frac{3}{2}$$

Q 6 . $\tan^2 30^\circ + \tan^2 45^\circ + \tan^2 60^\circ \tan^2 30^\circ + \tan^2 45^\circ + \tan^2 60^\circ$

Solution:

$$\tan^2 30^\circ + \tan^2 45^\circ + \tan^2 60^\circ \tan^2 30^\circ + \tan^2 45^\circ + \tan^2 60^\circ \quad [1]$$

We know that by trigonometric ratios we have ,

$$\tan 30^\circ = \frac{1}{\sqrt{3}} \tan 30^\circ = \frac{1}{\sqrt{3}} \quad \tan 60^\circ = \sqrt{3} \tan 60^\circ = \sqrt{3}$$

$$\tan 45^\circ = 1 \tan 45^\circ = 1$$

Substituting the values in equation 1 , we get

$$[1 \cdot \frac{1}{\sqrt{3}}]^2 + [\sqrt{3}]^2 + 1[\frac{1}{\sqrt{3}}]^2 + [1]^2 + 1$$

$$= 13 + 3 + 1 \frac{1}{3} + 3 + 1$$

$$= 133 \frac{13}{3}$$

Q 7 . $2\sin^2 30^\circ - 3\cos^2 45^\circ + \tan^2 60^\circ 2\sin^2 30^\circ - 3\cos^2 45^\circ + \tan^2 60^\circ$

Solution:

$$2\sin^2 30^\circ - 3\cos^2 45^\circ + \tan^2 60^\circ 2\sin^2 30^\circ - 3\cos^2 45^\circ + \tan^2 60^\circ \quad [1]$$

We know that by trigonometric ratios we have ,

$$\sin 30^\circ = \frac{1}{2} \quad \cos 45^\circ = \frac{1}{\sqrt{2}}$$

$$\tan 60^\circ = \sqrt{3}$$

Substituting the values in equation 1 , we get

$$= 2\left(\frac{1}{2}\right)^2 - 3\left(\frac{1}{\sqrt{2}}\right)^2 + (\sqrt{3})^2 2\left(\frac{1}{2}\right)^2 - 3\left(\frac{1}{\sqrt{2}}\right)^2 + (\sqrt{3})^2$$

$$= 2\left(\frac{1}{4}\right) - 3\left(\frac{1}{2}\right) + 3\left(\frac{1}{4}\right) - 3\left(\frac{1}{2}\right) + 3$$

$$= \frac{1-3+6}{2}$$

$$= 2$$

$$\text{Q8: } \sin^2 30^\circ \cos^2 45^\circ + 4\tan^2 30^\circ + 12\sin^2 90^\circ - 2\cos^2 90^\circ + 124\cos^2 0^\circ$$

$$\sin^2 30^\circ \cos^2 45^\circ + 4\tan^2 30^\circ + \frac{1}{2}\sin^2 90^\circ - 2\cos^2 90^\circ + \frac{1}{24}\cos^2 0^\circ$$

Solution:

$$\sin^2 30^\circ \cos^2 45^\circ + 4\tan^2 30^\circ + 12\sin^2 90^\circ - 2\cos^2 90^\circ + 124\cos^2 0^\circ$$

$$\sin^2 30^\circ \cos^2 45^\circ + 4\tan^2 30^\circ + \frac{1}{2}\sin^2 90^\circ - 2\cos^2 90^\circ + \frac{1}{24}\cos^2 0^\circ \quad [1]$$

We know that by trigonometric ratios we have ,

$$\sin 30^\circ = \frac{1}{2} \quad \cos 45^\circ = \frac{1}{\sqrt{2}} \quad \tan 30^\circ = \frac{1}{\sqrt{3}}$$

$$\sin 90^\circ \sin 90^\circ = 1$$

$$\cos 90^\circ \cos 90^\circ = 0$$

$$\cos 0^\circ \cos 0^\circ = 1$$

Substituting the values in equation 1 , we get

$$[12]^2 \cdot [1\sqrt{2}]^2 + 4[1\sqrt{3}]^2 + 12[1]^2 - 2[0]^2 + 124[1]^2 \left[\frac{1}{2}\right]^2 \cdot \left[\frac{1}{\sqrt{2}}\right]^2 + 4\left[\frac{1}{\sqrt{3}}\right]^2 + \frac{1}{2}[1]^2 - 2[0]^2 + \frac{1}{24}[1]^2$$

$$= 18 + 43 + 12 + 124 \frac{1}{8} + \frac{4}{3} + \frac{1}{2} + \frac{1}{24}$$

$$= 4824 \frac{48}{24} = 2$$

$$\text{Q 9. } 4(\sin^4 60^\circ + \cos^4 30^\circ) - 3(\tan^2 60^\circ - \tan^2 45^\circ) + 5\cos^2 45^\circ$$

$$4(\sin^4 60^\circ + \cos^4 30^\circ) - 3(\tan^2 60^\circ - \tan^2 45^\circ) + 5\cos^2 45^\circ$$

Solution:

$$4(\sin^4 60^\circ + \cos^4 30^\circ) - 3(\tan^2 60^\circ - \tan^2 45^\circ) + 5\cos^2 45^\circ$$

$$4(\sin^4 60^\circ + \cos^4 30^\circ) - 3(\tan^2 60^\circ - \tan^2 45^\circ) + 5\cos^2 45^\circ$$

[1]

We know that by trigonometric ratios we have ,

$$\sin 60^\circ = \frac{\sqrt{3}}{2} \Rightarrow \sin^2 60^\circ = \frac{3}{4}$$

$$\cos 45^\circ = \frac{1}{\sqrt{2}} \Rightarrow \cos^2 45^\circ = \frac{1}{2}$$

$$\tan 60^\circ = \sqrt{3} \Rightarrow \tan^2 60^\circ = 3$$

$$\cos 30^\circ = \frac{\sqrt{3}}{2} \Rightarrow \cos^2 30^\circ = \frac{3}{4}$$

Substituting the values in equation 1 , we get

$$4\left(\left[\frac{\sqrt{3}}{2}\right]^4 + \left[\frac{\sqrt{3}}{2}\right]^4\right) - 3(3)^2 - 1^2 + 5\left[\frac{1}{\sqrt{2}}\right]^2 \left(\left[\frac{\sqrt{3}}{2}\right]^4 + \left[\frac{\sqrt{3}}{2}\right]^4\right) - 3(3)^2 - 1^2 + 5\left[\frac{1}{\sqrt{2}}\right]^2$$

$$= 4 \cdot 1816 - 6 + 524 \cdot \frac{18}{16} - 6 + \frac{5}{2}$$

$$= 14 - 6 + 52 \frac{1}{4} - 6 + \frac{5}{2}$$

$$= 142 - 6 \frac{14}{2} - 6 = 7 - 6 = 1$$

$$\text{Q 10. } (\operatorname{cosec}^2 45^\circ \sec^2 30^\circ)(\sin^2 30^\circ + 4\cot^2 45^\circ - \sec^2 60^\circ)$$

$$(\operatorname{cosec}^2 45^\circ \sec^2 30^\circ)(\sin^2 30^\circ + 4\cot^2 45^\circ - \sec^2 60^\circ)$$

Solution:

$$(\operatorname{cosec}^2 45^\circ \sec^2 30^\circ)(\sin^2 30^\circ + 4\cot^2 45^\circ - \sec^2 60^\circ)$$

$$(\operatorname{cosec}^2 45^\circ \sec^2 30^\circ)(\sin^2 30^\circ + 4\cot^2 45^\circ - \sec^2 60^\circ)$$

[1]

We know that by trigonometric ratios we have ,

$$\operatorname{cosec} 45^\circ = \sqrt{2} \Rightarrow \operatorname{cosec}^2 45^\circ = 2$$

$$\sec 30^\circ = 2\sqrt{3} \Rightarrow \sec^2 30^\circ = 12$$

$$\sin 30^\circ = \frac{1}{2} \Rightarrow \sin^2 30^\circ = \frac{1}{4}$$

$$\cot 45^\circ = 1 \Rightarrow \cot^2 45^\circ = 1$$

$$\sec 60^\circ = 2 \Rightarrow \sec^2 60^\circ = 4$$

Substituting the values in equation 1 , we get

$$\begin{aligned}
&([\sqrt{2}]^2 \cdot [2\sqrt{3}]^2)([12]^2 + 4(1)(2)^2)([\sqrt{2}]^2 \cdot [\frac{2}{\sqrt{3}}]^2)([\frac{1}{2}]^2 + 4(1)(2)^2) \\
&= 3 \cdot 43 \cdot 143 \cdot \frac{4}{3} \cdot \frac{1}{4} \\
&= 23 \frac{2}{3}
\end{aligned}$$

Q11. cosec³30° cos60° tan³45° sin²90° sec²45° cot30°
cosec³ 30° cos60° tan³45° sin²90° sec²45° cot30°

Solution:

Given,

$$\begin{aligned}
&= \text{cosec}^3 30^\circ \cos 60^\circ \tan^3 45^\circ \sin^2 90^\circ \sec^2 45^\circ \cot 30^\circ \\
&\text{cosec}^3 30^\circ \cos 60^\circ \tan^3 45^\circ \sin^2 90^\circ \sec^2 45^\circ \cot 30^\circ \\
&= 2^3(12)(1^3)(1^2)(\sqrt{2}^2)(\sqrt{3})2^3(\frac{1}{2})(1^3)(1^2)(\sqrt{2}^2)(\sqrt{3}) \\
&= (2)^3 \times (12) \times (1^3) \times (1^2) \times (\sqrt{2}^2) \times (\sqrt{3})(2)^3 \times (\frac{1}{2}) \times (1^3) \times (1^2) \times (\sqrt{2}^2) \times (\sqrt{3}) \\
&= 8 \times (12) \times (1) \times (1) \times (2) \times (\sqrt{3}) 8 \times (\frac{1}{2}) \times (1) \times (1) \times (2) \times (\sqrt{3}) \\
&= 8\sqrt{3}8\sqrt{3}
\end{aligned}$$

Q12. cot²30° - 2cos²60° - 34sec²45° - 4sec²30° cot²30° - 2cos²60° - $\frac{3}{4}$ sec²45° - 4sec²30°

Solution:

Given,

$$\begin{aligned}
&= \cot^2 30^\circ - 2\cos^2 60^\circ - 34\sec^2 45^\circ - 4\sec^2 30^\circ \cot^2 30^\circ - 2\cos^2 60^\circ - \frac{3}{4}\sec^2 45^\circ - 4\sec^2 30^\circ \\
&= (\sqrt{3}^2) \times 2(12)^2 \times (34 \times \sqrt{2}^2) \times (4 \times (2\sqrt{3})^2)(\sqrt{3}^2) \times 2(\frac{1}{2})^2 \times (\frac{3}{4} \times \sqrt{2}^2) \times (4 \times (\frac{2}{\sqrt{3}})^2) \\
&= 3 - 12 - 32 - 1633 - \frac{1}{2} - \frac{3}{2} - \frac{16}{3} \\
&= -133 \frac{-13}{3}
\end{aligned}$$

Q13. (cos0° + sin45° + sin30°)(sin90° - cos45° + cos60°)
(cos0° + sin45° + sin30°)(sin90° - cos45° + cos60°)

Solution:

Given,

$$\begin{aligned} & (\cos 0^\circ + \sin 45^\circ + \sin 30^\circ)(\sin 90^\circ - \cos 45^\circ + \cos 60^\circ)(1 + \sqrt{2} + \sqrt{2})(1 - \sqrt{2} + \sqrt{2})(32 + \sqrt{2})(32 - \sqrt{2}) \\ & (\cos 0^\circ + \sin 45^\circ + \sin 30^\circ)(\sin 90^\circ - \cos 45^\circ + \cos 60^\circ) \\ & \left(1 + \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}}\right)\left(1 - \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}}\right) \\ & \left(\frac{3}{2} + \frac{1}{\sqrt{2}}\right)\left(\frac{3}{2} - \frac{1}{\sqrt{2}}\right) \\ & ((32)^2 - (\sqrt{2})^2) 94 - 1274 \left(\left(\frac{3}{2}\right)^2 - \left(\frac{1}{\sqrt{2}}\right)^2\right) \frac{9}{4} - \frac{1}{2} \frac{7}{4} \end{aligned}$$

Q14. $\sin 30^\circ - \sin 90^\circ + 2\cos 0^\circ \tan 30^\circ \tan 60^\circ = \frac{\sin 30^\circ - \sin 90^\circ + 2\cos 0^\circ}{\tan 30^\circ \tan 60^\circ}$

Solution:

Given,

$$\frac{\sin 30^\circ - \sin 90^\circ + 2\cos 0^\circ}{\tan 30^\circ \tan 60^\circ} = \frac{\frac{1}{2} - 1 + 2}{\frac{1}{\sqrt{3}} \times \sqrt{3}}$$

$$\sin 30^\circ - \sin 90^\circ + 2\cos 0^\circ \tan 30^\circ \tan 60^\circ = \frac{1}{2} - 1 + 2 \times \frac{1}{\sqrt{3}} \times \sqrt{3} = \frac{3}{2}$$

Q15. $4\cot^2 30^\circ + 1\sin^2 60^\circ - \cos^2 45^\circ = \frac{4}{\cot^2 30^\circ} + \frac{1}{\sin^2 60^\circ} - \cos^2 45^\circ$

Solution:

Given,

$$\begin{aligned} & \frac{4}{\cot^2 30^\circ} + \frac{1}{\sin^2 60^\circ} - \cos^2 45^\circ \\ & = \frac{4}{(\sqrt{3})^2} + \frac{1}{\left(\frac{\sqrt{3}}{2}\right)^2} - \left(\frac{1}{\sqrt{2}}\right)^2 \\ & = \frac{4}{3} + \frac{4}{3} - \frac{1}{2} \\ & = \frac{16-3}{6} \end{aligned}$$

$$4\cot^2 30^\circ + 1\sin^2 60^\circ - \cos^2 45^\circ = 4(\sqrt{3})^2 + 1\left(\frac{2}{\sqrt{3}}\right)^2 - (1\sqrt{2})^2 = 43 + 43 - 12 = 16 - 36 = 136 = \frac{13}{6}$$

Q16. $4(\sin^4 30^\circ + \cos^2 60^\circ) - 3(\cos^2 45^\circ - \sin^2 90^\circ) - \sin^2 60^\circ$

$$4(\sin^4 30^\circ + \cos^2 60^\circ) - 3(\cos^2 45^\circ - \sin^2 90^\circ) - \sin^2 60^\circ$$

Solution:

Given,

$$\begin{aligned} 4(\sin^4 30^\circ + \cos^2 60^\circ) - 3(\cos^2 45^\circ - \sin^2 90^\circ) - \sin^2 60^\circ &= 4\left(\left(\frac{1}{2}\right)^4 + \left(\frac{1}{2}\right)^2\right) - 3\left(\left(\frac{1}{\sqrt{2}}\right)^2 - 1\right) - \left(\frac{\sqrt{3}}{2}\right)^2 \\ &= 4\left(\frac{1}{16} + \frac{1}{4}\right) + \frac{3}{2} - \frac{3}{4} \end{aligned}$$

$$(\sqrt{32})^2 = 4(116 + 14) + 32 - 34 = 84 = 2 = \frac{8}{4} = 2$$

Q17. $\frac{\tan^2 60^\circ + 4\cos^2 45^\circ + 3\sec^2 30^\circ + 5\cos^2 90^\circ \operatorname{cosec} 30^\circ + \sec 60^\circ - \cot^2 30^\circ}{\operatorname{cosec} 30^\circ + \sec 60^\circ - \cot^2 30^\circ}$

Solution:

Given,

$$\begin{aligned} \frac{\tan^2 60^\circ + 4\cos^2 45^\circ + 3\sec^2 30^\circ + 5\cos^2 90^\circ \operatorname{cosec} 30^\circ + \sec 60^\circ - \cot^2 30^\circ}{\operatorname{cosec} 30^\circ + \sec 60^\circ - \cot^2 30^\circ} &= \frac{(\sqrt{3})^2 + 4(1\sqrt{2})^2 + 3(2\sqrt{3})^2 + 5(0)2 + 2 - (\sqrt{3})^2}{2 + 2 - (\sqrt{3})^2} = 3 + 2 + 4 = 9 \\ &= \frac{(\sqrt{3})^2 + 4\left(\frac{1}{\sqrt{2}}\right)^2 + 3\left(\frac{2}{\sqrt{3}}\right)^2 + 5(0)}{2 + 2 - (\sqrt{3})^2} \\ &= 3 + 2 + 4 \\ &= 9 \end{aligned}$$

Q18. $\sin 30^\circ \sin 45^\circ + \tan 45^\circ \sec 60^\circ - \sin 60^\circ \cot 45^\circ - \cos 30^\circ \sin 90^\circ \frac{\sin 30^\circ}{\sin 45^\circ} + \frac{\tan 45^\circ}{\sec 60^\circ} - \frac{\sin 60^\circ}{\cot 45^\circ} - \frac{\cos 30^\circ}{\sin 90^\circ}$

Solution:

Given,

$$\begin{aligned} \sin 30^\circ \sin 45^\circ + \tan 45^\circ \sec 60^\circ - \sin 60^\circ \cot 45^\circ - \cos 30^\circ \sin 90^\circ &= \frac{1}{2} \cdot \frac{1}{\sqrt{2}} + 1 \cdot 2 - \frac{\sqrt{3}}{2} \cdot 1 - \frac{\sqrt{3}}{2} \cdot 1 = \frac{1}{2\sqrt{2}} + 2 - \sqrt{3} - \sqrt{3} = \frac{1}{2\sqrt{2}} + 2 - 2\sqrt{3} \\ \frac{\sin 30^\circ}{\sin 45^\circ} + \frac{\tan 45^\circ}{\sec 60^\circ} - \frac{\sin 60^\circ}{\cot 45^\circ} - \frac{\cos 30^\circ}{\sin 90^\circ} &= \frac{\frac{1}{2}}{\frac{1}{\sqrt{2}}} + \frac{1}{2} - \frac{\frac{\sqrt{3}}{2}}{1} - \frac{\frac{\sqrt{3}}{2}}{1} \\ &= \frac{1}{2} \cdot \frac{\sqrt{2}}{1} + \frac{1}{2} - \frac{\sqrt{3}}{2} - \frac{\sqrt{3}}{2} \\ &= \frac{\sqrt{2}}{2} + \frac{1}{2} - \frac{\sqrt{3}}{2} - \frac{\sqrt{3}}{2} \\ &= \frac{\sqrt{2} + 1 - 2\sqrt{3}}{2} \end{aligned}$$

Q19. $\tan 45^\circ \operatorname{cosec} 30^\circ + \sec 60^\circ \cot 45^\circ + \sin 90^\circ 2 \cos 0^\circ = \frac{\tan 45^\circ}{\operatorname{cosec} 30^\circ} + \frac{\sec 60^\circ}{\cot 45^\circ} + \frac{\sin 90^\circ}{2 \cos 0^\circ}$

Solution:

Given,

$$\begin{aligned} \frac{\tan 45^\circ}{\operatorname{cosec} 30^\circ} + \frac{\sec 60^\circ}{\cot 45^\circ} + \frac{\sin 90^\circ}{2 \cos 0^\circ} &= \frac{1}{2} + \frac{2}{1} - \frac{5(1)}{2(1)} \\ &= \frac{5}{2} - \frac{5}{2} \end{aligned}$$

$$\tan 45^\circ \operatorname{cosec} 30^\circ + \sec 60^\circ \cot 45^\circ + \sin 90^\circ 2 \cos 0^\circ = 1 \cdot 2 + 2 \cdot 1 - 5(1)2(1) = 2 + 2 - 10 = 4 - 10 = -6 \neq 0$$

Q20. $2 \sin 3x = \sqrt{3} \Rightarrow \sin 3x = \frac{\sqrt{3}}{2}$

Solution:

Given,

$$\begin{aligned} 2 \sin 3x &= \sqrt{3} \\ \Rightarrow \sin 3x &= \frac{\sqrt{3}}{2} \\ \Rightarrow \sin 3x &= \sin 60^\circ \\ \Rightarrow 3x &= 60^\circ \end{aligned}$$

$$2 \sin 3x = \sqrt{3} \Rightarrow \sin 3x = \frac{\sqrt{3}}{2} \Rightarrow \sin 3x = \sin 60^\circ \Rightarrow 3x = 60^\circ \Rightarrow x = 20^\circ$$

Q21) $2 \sin x = 1, x = ? \Rightarrow \sin \frac{x}{2} = \frac{1}{2}, x = ?$

Solution:

$$\sin x^2 = 12 \sin \frac{x}{2} = \frac{1}{2} \quad \sin x^2 = \sin 30^0 \sin \frac{x}{2} = \sin 30^0 \quad x^2 = 30^0 \frac{x}{2} = 30^0$$

$$x = 60^0$$

Q22) $\sqrt{3} \sin x = \cos x$ $\sqrt{3} \sin x = \cos x$

Solution:

$$\sqrt{3} \tan x = 1 \quad \sqrt{3} \tan x = 1 \quad \tan x = \frac{1}{\sqrt{3}} \quad \therefore \tan x = \tan 30^0 \therefore \tan x = \tan 30^0$$

$$x = 30^0$$

Q23) $\tan x = \sin 45^0 \cos 45^0 + \sin 30^0$

Solution:

$$\tan x = 1 \cdot \frac{1}{\sqrt{2}} + \frac{1}{2} \quad [\because \sin 45^0 = \frac{1}{\sqrt{2}} \cos 45^0 = \frac{1}{\sqrt{2}} \sin 30^0 = \frac{1}{2}]$$

$$\tan x = \frac{1}{\sqrt{2}} + \frac{1}{2} \quad \tan x = \frac{1}{\sqrt{2}} + \frac{1}{2} \quad \tan x = \frac{1}{\sqrt{2}} + \frac{1}{2}$$

$$\tan x = 1$$

$$\tan x = 45^0$$

$$x = 45^0$$

Q24) $\sqrt{3} \tan 2x = \cos 60^0 + \sin 45^0 \cos 45^0$ $\sqrt{3} \tan 2x = \cos 60^0 + \sin 45^0 \cos 45^0$

Solution:

$$\sqrt{3} \tan 2x = \frac{1}{2} + \frac{1}{\sqrt{2}} \cdot \frac{1}{\sqrt{2}} \quad [\because \cos 60^0 = \frac{1}{2} \sin 45^0 = \cos 45^0 = \frac{1}{\sqrt{2}}]$$

$$\sqrt{3} \tan 2x = \frac{1}{2} + \frac{1}{2} \quad [\because \cos 60^0 = \frac{1}{2} \sin 45^0 = \cos 45^0 = \frac{1}{\sqrt{2}}] \quad \sqrt{3} \tan 2x = 1 \Rightarrow \tan 2x = \tan 30^0$$

$$\sqrt{3} \tan 2x = \frac{1}{\sqrt{3}} \Rightarrow \tan 2x = \tan 30^0$$

$$2x = 30^0$$

$$x = 15^0$$

$$\text{Q25) } \cos 2x = \cos 60^\circ \cos 30^\circ + \sin 60^\circ \sin 30^\circ \cos 2x = \cos 60^\circ \cos 30^\circ + \sin 60^\circ \sin 30^\circ$$

Solution:

$$\cos 2x = 12 \cdot \sqrt{32} + \sqrt{32} \cdot 12 \quad [\because \cos 60^\circ = \sin 30^\circ = 12 \sin 60^\circ = \cos 30^\circ = \sqrt{32}]$$

$$\cos 2x = \frac{1}{2} \cdot \frac{\sqrt{3}}{2} + \frac{\sqrt{3}}{2} \cdot \frac{1}{2} \quad [\because \cos 60^\circ = \sin 30^\circ = \frac{1}{2} \sin 60^\circ = \cos 30^\circ = \frac{\sqrt{3}}{2}] \quad \cos 2x = 2 \cdot \sqrt{34}$$

$$\cos 2x = 2 \cdot \frac{\sqrt{3}}{4} \quad \cos 2x = \sqrt{32} \cos 2x = \frac{\sqrt{3}}{2} \quad \cos 2x = \cos 30^\circ \cos 2x = \cos 30^\circ \quad 2x = 30^\circ \quad 2x = 30^\circ \quad x = 15^\circ$$

Q26)

If $\theta = 30^\circ$, verify

$$\text{If } \theta = 30^\circ, \text{ verify (i) } \tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta} \quad \text{(i) } \tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta}$$

Solution:

$$\tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta} \dots \dots \text{(i) } \tan 2\theta = \frac{2 \tan \theta}{1 - \tan^2 \theta} \dots \dots \text{(i)}$$

Substitute $\theta = 30^\circ$ in equation (i)

$$\text{LHS} = \tan 60^\circ = \sqrt{3}$$

$$\text{RHS} = \frac{2 \tan 30^\circ}{1 - (\tan 30^\circ)^2} = \frac{2 \cdot \frac{1}{\sqrt{3}}}{1 - (\frac{1}{\sqrt{3}})^2} = \frac{2 \cdot \frac{1}{\sqrt{3}}}{1 - \frac{1}{3}} = \frac{2 \cdot \frac{1}{\sqrt{3}}}{\frac{2}{3}} = \sqrt{3}$$

Therefore, LHS = RHS

$$\text{(ii) } \sin 2\theta = \frac{2 \tan \theta}{1 + \tan^2 \theta} \sin \theta = \frac{2 \tan \theta}{1 + \tan^2 \theta} \sin \theta$$

Substitute $\theta = 30^\circ$

$$\sin 60^\circ = \frac{2 \tan 30^\circ \sin 30^\circ}{1 + (\tan 30^\circ)^2} = \frac{2 \tan 30^\circ \sin 30^\circ}{1 + (\tan 30^\circ)^2}$$

$$\Rightarrow \sqrt{32} = \frac{2 \cdot \frac{1}{\sqrt{3}} \cdot \frac{1}{2}}{1 + (\frac{1}{\sqrt{3}})^2} = \frac{2 \cdot \frac{1}{\sqrt{3}} \cdot \frac{1}{2}}{1 + \frac{1}{3}}$$

$$\Rightarrow \frac{\sqrt{3}}{2} = \frac{2}{\sqrt{3}} \cdot \frac{3}{4}$$

$$\sqrt{32} = 2 \sqrt{3} \cdot \frac{3}{4} \Rightarrow \sqrt{32} = \sqrt{32} \Rightarrow \frac{\sqrt{3}}{2} = \frac{\sqrt{3}}{2}$$

Therefore, LHS = RHS.

$$\text{(iii) } \cos 2\theta = \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta} \cos 2\theta = \frac{1 - \tan^2 \theta}{1 + \tan^2 \theta}$$

Substitute $\theta=30^\circ$

$$\text{LHS} = \operatorname{cosec}\theta \operatorname{cosec}\theta$$

$$\text{RHS} = \frac{1-\tan^2\theta}{1+\tan^2\theta}$$

$$= \cos 2(30^\circ)$$

$$= \frac{1-\tan^2 30^\circ}{1+\tan^2 30^\circ}$$

$$\cos 60^\circ = \frac{1}{2} = \frac{1 - (\frac{1}{\sqrt{2}})^2}{1 + (\frac{1}{\sqrt{2}})^2} = \frac{1 - \frac{1}{2}}{1 + \frac{1}{2}} = \frac{\frac{1}{2}}{\frac{3}{2}} = \frac{1}{3}$$

Therefore, LHS = RHS

(iv) $\cos 3\theta = 4\cos^3\theta - 3\cos\theta$

Solution:

$$\text{LHS} = \cos 3\theta$$

Substitute $\theta=30^\circ$

$$= \cos 3(30^\circ) = \cos 90^\circ$$

$$= 0$$

$$\text{RHS} = 4\cos^3\theta - 3\cos\theta$$

$$= 4\cos^3 30^\circ - 3\cos 30^\circ$$

$$= 4\left(\frac{\sqrt{3}}{2}\right)^3 - 3 \cdot \frac{\sqrt{3}}{2}$$

$$= 3 \cdot \frac{\sqrt{3}}{2} - 3 \cdot \frac{\sqrt{3}}{2}$$

$$= 0$$

Therefore, LHS = RHS.

Q27) If $A = B = 60^\circ$. Verify (i) $\cos(A - B) = \cos A \cos B + \sin A \sin B$

Solution:

$$\cos(A - B) = \cos A \cos B + \sin A \sin B \dots\dots (i)$$

Substitute A and B in (i)

$$\Rightarrow \cos(60^\circ - 60^\circ) = \cos 60^\circ \cos 60^\circ + \sin 60^\circ \sin 60^\circ$$

$$\Rightarrow \cos 0^\circ = \left(\frac{1}{2}\right)^2 + \left(\frac{\sqrt{3}}{2}\right)^2$$

$$\Rightarrow 1 = 14 + 34 \frac{1}{4} + \frac{3}{4}$$

$$\Rightarrow 1 = 1$$

Therefore, LHS = RHS

(ii) Substitute A and B in (i)

$$\Rightarrow \sin(60^\circ - 60^\circ) = \sin 60^\circ \cos 60^\circ - \cos 60^\circ \sin 60^\circ$$

$$\Rightarrow \sin 0^\circ = 0$$

$$\Rightarrow 0 = 0$$

Therefore, LHS = RHS

$$\text{(iii) } \tan(A - B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

A = 60°, B = 60° we get,

$$\tan(60^\circ - 60^\circ) = \frac{\tan 60^\circ - \tan 60^\circ}{1 + \tan 60^\circ \tan 60^\circ} = \frac{\tan 60^\circ - \tan 60^\circ}{1 + \tan 60^\circ \tan 60^\circ}$$

$$\tan 0^\circ = 0$$

$$0 = 0$$

Therefore, LHS = RHS

Q28) If A = 30°, B = 60° verify:

(i) Sin (A + B) = Sin A Cos B + Cos A Sin B

Solution:

A = 30°, B = 60° we get

$$\sin(30^\circ + 60^\circ) = \sin 30^\circ \cos 60^\circ + \cos 30^\circ \sin 60^\circ$$

$$\sin(90^\circ) = 1 = \frac{1}{2} \cdot \frac{1}{2} + \frac{\sqrt{3}}{2} \cdot \frac{\sqrt{3}}{2}$$

$$\sin(90^\circ) = 1 \Rightarrow 1 = 1$$

Therefore, LHS = RHS

(ii) Cos (A + B) = Cos A Cos B - Sin A Sin B

$A = 30^\circ$, $B = 60^\circ$ we get

$$\cos(30^\circ + 60^\circ) = \cos 30^\circ \cos 60^\circ - \sin 30^\circ \sin 60^\circ$$

$$\cos(90^\circ) = 12 \cdot \sqrt{3}2 - \sqrt{3}2 \cdot 12 \cdot \frac{1}{2} \cdot \frac{\sqrt{3}}{2} - \frac{\sqrt{3}}{2} \cdot \frac{1}{2}$$

$$0 = 0$$

Therefore, LHS = RHS

Q29. If $\sin(A+B) = 1$ and $\cos(A-B) = 1$, $0^\circ < A+B \leq 90^\circ$, $0^\circ < A + B \leq 90^\circ$, $A \geq B$ find A and B.

Sol:

Given,

$$\sin(A+B) = 1 \text{ this can be written as } \sin(A+B) = \sin(90^\circ)\sin(90^\circ)$$

$$\cos(A-B) = 1 \text{ this can be written as } \cos(A-B) = \cos(0^\circ)\cos(0^\circ)$$

$$\Rightarrow A + B = 90^\circ 90^\circ$$

$$A - B = 0^\circ 0^\circ$$

$$2A = 90^\circ 90^\circ$$

$$A = 90^\circ 2 \frac{90^\circ}{2}$$

$$A = 45^\circ 45^\circ$$

Substitute A value in $A - B = 0^\circ 0^\circ$

$$45^\circ 45^\circ - B = 0^\circ 0^\circ$$

$$B = 45^\circ 45^\circ$$

Hence, the value of $A = 45^\circ 45^\circ$ and $B = 45^\circ 45^\circ$

Q30. If $\tan(A-B) = 1\sqrt{3} \frac{1}{\sqrt{3}}$ and $\tan(A+B) = \sqrt{3}\sqrt{3}$, $0^\circ < A+B \leq 90^\circ$, $0^\circ < A + B \leq 90^\circ$, $A > B$ find A and B

Solution:

Given,

$$\tan(A-B) = 1\sqrt{3} \frac{1}{\sqrt{3}}$$

$$A - B = \tan^{-1}(1\sqrt{3})\tan^{-1}\left(\frac{1}{\sqrt{3}}\right)$$

$$A - B = 30^\circ \quad \text{--- 1}$$

$$\tan(A+B) = \sqrt{3}$$

$$A + B = \tan^{-1} \sqrt{3}$$

$$A + B = 60^\circ \quad \text{--- 2}$$

Solve equations 1 and 2

$$A + B = 60^\circ$$

$$A - B = 30^\circ$$

$$2A = 90^\circ$$

$$A = 90^\circ \div 2 = 45^\circ$$

$$A = 45^\circ$$

Substitute the value of A in equation 1

$$45^\circ + B = 60^\circ$$

$$B = 60^\circ - 45^\circ$$

$$B = 15^\circ$$

The value of $A = 45^\circ$ and $B = 15^\circ$

Q31. If $\sin(A-B) = \frac{1}{2}$ and $\cos(A+B) = \frac{1}{2}$, $0^\circ < A+B \leq 90^\circ$, $0^\circ < A < B$ find A and B.

Solution:

Given,

$$\sin(A-B) = \frac{1}{2}$$

$$A - B = \sin^{-1} \left(\frac{1}{2} \right)$$

$$A - B = 30^\circ \quad \text{--- 1}$$

$$\cos(A+B) = \frac{1}{2}$$

$$A + B = \cos^{-1} \left(\frac{1}{2} \right)$$

$$A + B = 60^\circ \quad \text{--- 2}$$

Solve equations 1 and 2

$$A + B = 60^\circ$$

$$A - B = 30^\circ$$

$$2A = 90^\circ$$

$$A = 90^\circ \div 2 = \frac{90^\circ}{2}$$

$$A = 45^\circ$$

Substitute the value of A in equation 2

$$45^\circ + B = 60^\circ$$

$$B = 60^\circ - 45^\circ$$

$$B = 15^\circ$$

The value of $A = 45^\circ$ and $B = 15^\circ$

Q32. In a ΔABC right angled triangle at B, $\angle A = \angle C$. Find the values of:

1. $\sin A \cos C + \cos A \sin C$

Solution:

since, it is given as $\angle A = \angle C$

the value of A and C is 45° , the value of angle B is 90°

because the sum of angles of triangle is 180°

$$\Rightarrow \sin(45^\circ) \cos(45^\circ) + \cos(45^\circ) \sin(45^\circ)$$

$$\Rightarrow (1 \times \frac{1}{\sqrt{2}}) (\frac{1}{\sqrt{2}}) + (\frac{1}{\sqrt{2}}) (1 \times \frac{1}{\sqrt{2}})$$

$$\Rightarrow 1 \times \frac{1}{2} + 1 \times \frac{1}{2}$$

$$\Rightarrow 1$$

The value of $\sin A \cos C + \cos A \sin C$ is 1

2. $\sin A \sin B + \cos A \cos B$

Solution:

since, it is given as $\angle A = \angle C = \angle A = \angle C$

the value of A and C is 45° , the value of angle B is 90°

because the sum of angles of triangle is 180°

$$\Rightarrow \sin(45^\circ)\sin(90^\circ) + \cos(45^\circ)\cos(90^\circ)$$

$$\Rightarrow 1\sqrt{2} \cdot \frac{1}{\sqrt{2}}(1) + 1\sqrt{2} \cdot \frac{1}{\sqrt{2}}(0)$$

$$\Rightarrow 1\sqrt{2} \cdot \frac{1}{\sqrt{2}} + 0$$

$$\Rightarrow 1\sqrt{2} \cdot \frac{1}{\sqrt{2}}$$

The value of $\sin A \sin B + \cos A \cos B$ is $1\sqrt{2} \cdot \frac{1}{\sqrt{2}}$

Q33. Find the acute angle A and B, if $\sin(A+2B) = \frac{\sqrt{3}}{2}$ and $\cos(A+4B) = 0$, $A > B$.

Solution:

Given,

$$\sin(A+2B) = \frac{\sqrt{3}}{2}$$

$$A + 2B = \sin^{-1}\left(\frac{\sqrt{3}}{2}\right)$$

$$A + 2B = 60^\circ \quad \text{--- 1}$$

$$\cos(A+4B) = 0$$

$$A + 4B = \sin^{-1}(0)$$

$$A + 4B = 90^\circ \quad \text{--- 2}$$

Solve equations 1 and 2

$$A + 2B = 60^\circ$$

$$A + 4B = 90^\circ$$

$$(-) \quad (-) \quad (-)$$

$$-2B = -30^\circ$$

$$2B = 30^\circ$$

$$B = 30^\circ - \frac{30^\circ}{2}$$

$$B = 15^\circ$$

Substitute B value in eq 2

$$A + 4B = 90^\circ$$

$$A + 4(15^\circ) = 90^\circ$$

$$A + 60^\circ = 90^\circ$$

$$A = 90^\circ - 60^\circ$$

$$A = 30^\circ$$

The value of $A = 30^\circ$ and $B = 15^\circ$

Q 34. In ΔPQR , right angled at Q, PQ = 3 cm and PR = 6 cm. Determine $\angle P$ and $\angle R$.

Solution:

Given,

In ΔPQR , right angled at Q, PQ = 3 cm and PR = 6 cm

By Pythagoras theorem,

$$PR^2 = PQ^2 + QR^2$$

$$\Rightarrow 6^2 = 3^2 + QR^2$$

$$\Rightarrow QR^2 = 36 - 9$$

$$\Rightarrow QR = \sqrt{27}$$

$$PR^2 = PQ^2 + QR^2 \Rightarrow 6^2 = 3^2 + QR^2 \Rightarrow QR^2 = 36 - 9 \Rightarrow QR = \sqrt{27} \Rightarrow QR = 3\sqrt{3}$$

$$\sin R = \frac{PQ}{PR} = \frac{3}{6} = \frac{1}{2} = \sin 30^\circ$$

$$\angle R = 30^\circ$$

As we know, Sum of angles in a triangle = 180

$$\angle P + \angle Q + \angle R = 180^\circ \Rightarrow \angle P + 90^\circ + 30^\circ = 180^\circ \Rightarrow \angle P = 180^\circ - 120^\circ \Rightarrow \angle P = 60^\circ$$

$$\angle P + \angle Q + \angle R = 180^\circ$$

$$\Rightarrow \angle P + 90^\circ + 30^\circ = 180^\circ$$

$$\Rightarrow \angle P = 180^\circ - 120^\circ$$

$$\Rightarrow \angle P = 60^\circ$$

$$\text{Therefore, } \angle R = 30^\circ \angle R = 30^\circ$$

$$\text{And, } \angle P = 60^\circ \angle P = 60^\circ$$

Q35. If $\sin(A - B) = \sin A \cos B - \cos A \sin B$ and $\cos(A - B) = \cos A \cos B + \sin A \sin B$, find the values of $\sin 15$ and $\cos 15$.

Solution:

Given,

$$\sin(A - B) = \sin A \cos B - \cos A \sin B$$

$$\text{And, } \cos(A - B) = \cos A \cos B + \sin A \sin B$$

We need to find, $\sin 15$ and $\cos 15$.

$$\text{Let } A = 45 \text{ and } B = 30$$

$$\sin 15 = \sin(45 - 30) = \sin 45 \cos 30 - \cos 45 \sin 30$$

$$= \left(\frac{1}{\sqrt{2}} \times \frac{\sqrt{3}}{2}\right) - \left(\frac{1}{\sqrt{2}} \times \frac{1}{2}\right)$$

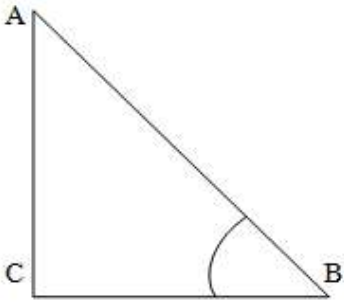
$$= (1\sqrt{2} \times \sqrt{32}) - (1\sqrt{2} \times 12) = \sqrt{3} - 12\sqrt{2} = \frac{\sqrt{3}-1}{2\sqrt{2}}$$

$$\cos 15 = \cos(45 - 30) = \cos 45 \cos 30 + \sin 45 \sin 30$$

$$= \left(\frac{1}{\sqrt{2}} \times \frac{\sqrt{3}}{2}\right) + \left(\frac{1}{\sqrt{2}} \times \frac{1}{2}\right)$$

$$= (1\sqrt{2} \times \sqrt{32}) + (1\sqrt{2} \times 12) = \sqrt{3} + 12\sqrt{2} = \frac{\sqrt{3}+1}{2\sqrt{2}}$$

Q36. In a right triangle ABC, right angled at C, if $\angle B = 60^\circ$ and $AB = 15$ units. Find the remaining angles and sides.



Solution:

$$\sin 60^\circ = \frac{x}{15}$$

$$\frac{\sqrt{3}}{2} = \frac{x}{15}$$

$$x = \frac{15\sqrt{3}}{2} \text{ units}$$

$$\cos 60^\circ = \frac{x}{15}$$

$$\frac{1}{2} = \frac{x}{15}$$

$$x = \frac{15}{2}$$

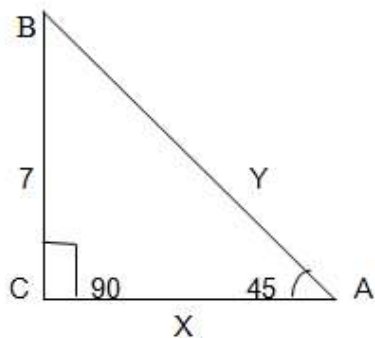
$$x = 7.5 \text{ units}$$

$$\sin 60^\circ = \frac{x}{15} \Rightarrow x = 15 \sin 60^\circ = 15 \cdot \frac{\sqrt{3}}{2} = 7.5\sqrt{3} \text{ units}$$

$$\cos 60^\circ = \frac{x}{15} \Rightarrow x = 15 \cos 60^\circ = 15 \cdot \frac{1}{2} = 7.5 \text{ units}$$

Q37. In ΔABC is a right triangle such that $\angle C = 90^\circ$, $\angle A = 45^\circ$ and $BC = 7$ units. Find the remaining angles and sides.

Solution:



Here, $\angle C = 90^\circ$ and $\angle A = 45^\circ$

We know that,

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\Rightarrow 45^\circ + 90^\circ + \angle C = 180^\circ$$

$$\Rightarrow 135^\circ + \angle C = 180^\circ$$

$$\Rightarrow \angle C = 180^\circ - 135^\circ$$

$$\Rightarrow \angle C = 45^\circ$$

The value of the remaining angle C is 45°

Now, we need to find the sides x and y

here,

$$\cos(45) = \frac{BC}{AB}$$

$$1\sqrt{2} \frac{1}{\sqrt{2}} = 7y \frac{7}{y}$$

$$y = 7\sqrt{2}$$

$$\sin(45) = \frac{AC}{AB}$$

$$1\sqrt{2} \frac{1}{\sqrt{2}} = xy \frac{x}{y}$$

$$1\sqrt{2} \frac{1}{\sqrt{2}} = x7\sqrt{2} \frac{x}{7\sqrt{2}}$$

$$x = 7\sqrt{2}$$

$$x = 7 \text{ units}$$

the value of x = 7 units and y = $7\sqrt{2}$ units

Q 38 . In a rectangle ABCD , AB = 20 cm , $\angle BAC = 60^\circ$, calculate side BC and diagonals AC and BD .

Solution:

Let AC = x cm and CB = y cm

$$\text{Since , } \cos\theta = \frac{\text{base}}{\text{hypotenuse}}$$

$$\text{Therefore , } \cos 60^\circ = \frac{20}{x}$$

$$\Rightarrow 12 = 20x \Rightarrow \frac{1}{2} = \frac{20}{x} \quad [\text{since, } \cos 60^\circ = \frac{1}{2}]$$

$$\Rightarrow x = 40 \text{ cm} = AC$$

Similarly $BD = 40 \text{ cm}$

Now ,

Since , $\sin\theta = \frac{\text{perpendicular}}{\text{hypotenuse}}$

$$\text{Therefore , } \sin 60^\circ = \frac{BC}{AC} \Rightarrow \frac{\sqrt{3}}{2} = \frac{y}{40}$$

$$\Rightarrow \sqrt{3} = \frac{y}{40} \Rightarrow y = 40\sqrt{3} \Rightarrow y = \frac{40\sqrt{3}}{2}$$

$$\Rightarrow y = 20\sqrt{3} \Rightarrow y = 20\sqrt{3} \text{ cm .}$$

Q39: If A & B are acute angles such that $\tan A = \frac{1}{2}$ $\tan B = \frac{1}{3}$ and $\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$, find $A+B$.

Solution:

$$\tan(A+B) = \frac{\frac{1}{2} + \frac{1}{3}}{1 - \frac{1}{2} \cdot \frac{1}{3}} = \frac{\frac{3+2}{6}}{1 - \frac{1}{6}} = \frac{\frac{5}{6}}{\frac{5}{6}} = 1 \Rightarrow \tan(A+B) = 1$$

$$\tan(A+B) = 1 \Rightarrow (A+B) = \tan^{-1}(1) \Rightarrow (A+B) = 45^\circ$$

$$(A+B) = 45^\circ$$

Q 40: Prove that : $(\sqrt{3}-1)(3-\cot 30^\circ) = \tan^3 60^\circ - 2\sin 60^\circ$

$$(\sqrt{3}-1)(3-\cot 30^\circ) = \tan^3 60^\circ - 2\sin 60^\circ$$

Ans:

$$\text{L.H.S} \Rightarrow (\sqrt{3}-1)(3-\cot 30^\circ)$$

$$= (\sqrt{3}-1)(3-\sqrt{3}) \because \cot 30^\circ = \sqrt{3}$$

$$= (\sqrt{3}-1)(\sqrt{3}-1)\sqrt{3} = (\sqrt{3}-1)^2 \sqrt{3}$$

$$= ((\sqrt{3})^2 - 2\sqrt{3} + 1)\sqrt{3}$$

$$= (3 - 2\sqrt{3} + 1)\sqrt{3}$$

$$\text{R.H.S} \Rightarrow \tan^3 60^\circ - 2\sin 60^\circ$$

$$= (\sqrt{3})^3 - 2 \times \frac{\sqrt{3}}{2}$$

$$= 3\sqrt{3} - \sqrt{3}$$

$$= 2\sqrt{3}$$

L.H.S = R.H.S

Hence Proved