

RD SHARMA

Solutions

Class 10 Maths

Chapter 8

Ex 8.1

1. (i) $x^2 - 3x + 2 = 0$, $x = 2$, $x = -1$

Here LHS = $x^2 - 3x + 2$

RHS = 0

Now, substitute $x = 2$ in LHS

We get,

$$(2)^2 - 3(2) + 2 = 4 - 6 + 2 = 6 - 6 = 0 = \text{RHS}$$

Since, LHS = RHS

Therefore, $x = 2$ is a solution of the given equation.

Similarly, substituting $x = -1$ in LHS

We get,

$$(-1)^2 - 3(-1) + 2 = 1 + 3 + 2 = 6 \neq \text{RHS}$$

Since, LHS \neq RHS = $x = -1$ is not the solution of the given equation.

(ii) $x^2 + x + 1 = 0$, $x = 0$, $x = 1$

Here, LHS = $x^2 + x + 1$ and RHS = 0

Now, substituting $x = 0$ and $x = 1$ in LHS

$$= 0^2 + 0 + 1 = (1)^2 + 1 + 1 = 1 \neq 3$$

LHS \neq RHS

Both $x = 0$ and $x = 1$ are not solutions of the given equation.

(iii) $x^2 - 3\sqrt{3}x + 6 = 0$, $x = \sqrt{3}$ and $x = -2\sqrt{3}$

Here,

$$\text{LHS} = x^2 - 3\sqrt{3}x + 6 = 0 \quad \text{and} \quad \text{RHS} = 0$$

Substituting the value of $x = \sqrt{3}$ and $x = -2\sqrt{3}$ in LHS

$$\sqrt{3}^2 - 3\sqrt{3} \times \sqrt{3} + 6 = 3 - 3\sqrt{3} \times \sqrt{3} + 6$$

$$= 3 - 9 + 6$$

$$= 0$$

$$= \text{RHS}$$

$$-2\sqrt{3}^2 - 3\sqrt{3} \times -2\sqrt{3} + 6 - 2\sqrt{3}^2 - 3\sqrt{3} \times -2\sqrt{3} + 6$$

$$= 12 + 18 + 6$$

$$= 36$$

$$\neq \text{RHS}$$

$x = \sqrt{3}$ is a solution of the above mentioned equation

Whereas, $x = -2\sqrt{3}$ is not a solution of the above mentioned equation .

$$\text{(iv) } x + \frac{1}{x} = 136x + \frac{1}{x} = \frac{13}{6}$$

$$\text{where } x = \frac{5}{6} \text{ and } x = \frac{4}{3}$$

$$\text{Here, LHS} = x + \frac{1}{x} = 136x + \frac{1}{x} = \frac{13}{6} \quad \text{and RHS} = 136 \frac{13}{6}$$

Substituting $x = \frac{5}{6}$ and $x = \frac{4}{3}$ in the LHS

$$= 56 + 156 \frac{5}{6} + \frac{1}{\frac{5}{6}}$$

$$= 56 + 65 \frac{5}{6} + \frac{6}{5}$$

$$= 25 + 3630 \frac{25+36}{30}$$

$$= 6130 \frac{61}{30}$$

$$\neq \text{RHS}$$

$$= 43 + 143 \frac{4}{3} + \frac{1}{\frac{4}{3}}$$

$$= 43 + 34 \frac{4}{3} + \frac{3}{4}$$

$$= 16 + 912 \frac{16+9}{12}$$

$$= 2512 \frac{25}{12}$$

$$\neq \text{RHS}$$

$x = \frac{5}{6}$ and $x = \frac{4}{3}$ are not the solutions of the given equation.

$$(v) 2x^2 - x + 9 = x^2 + 4x + 3, x = 2 \text{ and } x = 3$$

$$= 2x^2 - x + 9 - x^2 + 4x + 3$$

$$= x^2 - 5x + 6 = 0$$

$$\text{Here, LHS} = x^2 - 5x + 6 \text{ and RHS} = 0$$

Substituting $x = 2$ and $x = 3$

$$= x^2 - 5x + 6$$

$$= (2)^2 - 5(2) + 6$$

$$= 10 - 10$$

$$= 0$$

$$= \text{RHS}$$

$$= x^2 - 5x + 6$$

$$= (3)^2 - 5(3) + 6$$

$$= 9 - 15 + 6$$

$$= 15 - 15$$

$$= 0$$

$$= \text{RHS}$$

$x = 2$ and $x = 3$ both are the solutions of the given quadratic equation.

$$(vi) x^2 - \sqrt{2}x - 4 = 0 \quad x^2 - \sqrt{2}x - 4 = 0$$

$$x = -\sqrt{2} \text{ and } x = -2\sqrt{2} \quad x = -\sqrt{2} \text{ and } x = -2\sqrt{2}$$

$$\text{Here, LHS} = x^2 - \sqrt{2}x - 4 = 0 \quad x^2 - \sqrt{2}x - 4 = 0$$

$$\text{And RHS} = 0$$

Substituting the value $x = -\sqrt{2}$ and $x = -2\sqrt{2}$ in LHS

$$= (-\sqrt{2})^2 - \sqrt{2} \times \sqrt{2} - 4 \quad (-\sqrt{2})^2 - \sqrt{2} \times \sqrt{2} - 4$$

$$= 2 - 2 - 4$$

$$= -4$$

≠RHS

$$= (-2\sqrt{2})^2 - \sqrt{2} \times 2\sqrt{2} - 4(-2\sqrt{2})^2 - \sqrt{2} \times 2\sqrt{2} - 4$$

$$= 8 - 4 - 4$$

$$= 8 - 8$$

$$= 0$$

= RHS

$x = -2\sqrt{2}$ is the solution of the above mentioned quadratic equation .

(vii) $a^2x^2 - 3abx + 2b^2 = 0$

$$x = ab \text{ and } x = \frac{b}{a}$$

Here, LHS = $a^2x^2 - 3abx + 2b^2$ and RHS = 0

Substituting the $x = ab$ in LHS

$$= a^2(ab)^2 - 3ab(ab) + 2b^2a^2\left(\frac{a}{b}\right)^2 - 3ab\left(\frac{a}{b}\right) + 2b^2$$

$$= a^4b^2 - 3a^2 + 2b^2\frac{a^4}{b^2} - 3a^2 + 2b^2$$

≠ RHS

$$= a^2(ba)^2 - 3ab(ba) + 2b^2a^2\left(\frac{b}{a}\right)^2 - 3ab\left(\frac{b}{a}\right) + 2b^2$$

$$= b^2 - 3b^2 + 2b^2 = 0 = \text{RHS}$$

$x = \frac{b}{a}$ is the solution of the above mentioned quadratic equation .

3.

(i) Given that $23\frac{2}{3}$ is a root of the given equation.

The equation is $7x^2 + kx - 3 = 0$

According to the question $23\frac{2}{3}$ satisfies the equation.

$$= 7(23\frac{2}{3})^2 + k(23\frac{2}{3}) - 37(\frac{2}{3})^2 + k(\frac{2}{3}) - 3$$

$$= 7(49) + 2k3 - 37(\frac{4}{9}) + \frac{2k}{3} - 3$$

$$= 2k^3 = 27 - 289 \frac{2k}{3} = \frac{27 - 28}{9}$$

$$= 2k^3 = -19 \frac{2k}{3} = \frac{-1}{9}$$

$$= k = -16k = \frac{-1}{6}$$

(ii) Given that $x=a$ is a root of the given equation $x^2 - x(a+b) + k = 0$

= $x=a$ satisfies the equation

$$= a^2 - a(a+b) + k = 0$$

$$= a^2 - a^2 - ab + k = 0$$

$$K = ab$$

(iii) Given that $x = \sqrt{2}x = \sqrt{2}$ is a root of the given equation $kx^2 + \sqrt{2}x - 4kx^2 + \sqrt{2}x - 4$

$x = \sqrt{2}x = \sqrt{2}$ satisfies the given quadratic equation.

$$= k\sqrt{2}^2 + \sqrt{2}\sqrt{2} - 4k\sqrt{2}^2 + \sqrt{2}\sqrt{2} - 4$$

$$= 2k + 2 - 4 = 0$$

$$= 2k - 2 = 0$$

$$K = 1$$

(iv) Given that $x = -a$ is the root of the given equation $x^2 + 3ax + k = 0$

Therefore,

$$= (-a)^2 + 3a(-a) + k = 0$$

$$= a^2 + 3a^2 + k = 0$$

$$= k = 4a^2 = -a \text{ satisfies the equation}$$

(v) Given that $x = \sqrt{2}x = \sqrt{2}$ is a root of the given equation $kx^2 + \sqrt{2}x - 4kx^2 + \sqrt{2}x - 4$

$x = \sqrt{2}x = \sqrt{2}$ satisfies the given quadratic equation.

$$= k\sqrt{2}^2 + \sqrt{2}\sqrt{2} - 4k\sqrt{2}^2 + \sqrt{2}\sqrt{2} - 4$$

$$=2k+2-4=0$$

$$=2k-2=0$$

$$K=1$$

4. Given to check whether 3 is a root of the equation $\sqrt{x^2-4x+3}+\sqrt{x^2-9}=\sqrt{4x^2-14x+16}$
 $\sqrt{x^2-4x+3} + \sqrt{x^2-9} = \sqrt{4x^2-14x+16}$

$$\text{LHS} = \sqrt{x^2-4x+3} + \sqrt{x^2-9}$$

$$\text{RHS} = \sqrt{4x^2-14x+16}$$

Substituting $x=3$ in LHS

$$\sqrt{3^2-4 \times 3+3} + \sqrt{3^2-9}$$

$$\sqrt{9-12+3} + \sqrt{9-9}$$

$$\sqrt{12-12} + \sqrt{9-9}$$

$$=0$$

Similarly putting $x=3$ in RHS

Extra open brace or missing close brace

$$\sqrt{4(3)^2-14(3)+16}$$

$$\sqrt{4(3)^2-14(3)+16}$$

\neq RHS

$X=3$ is not the solution the given quadratic equation.