

**RD SHARMA**  
**Solutions**  
**Class 10 Maths**  
**Chapter 16**  
**16.3**

**Q1. A bucket has top and bottom diameters of 40 cm and 20 cm respectively. Find the volume of the bucket if its depth is 12 cm. Also find the cost of tin sheet for making the bucket at the rate of Rs 1.20 per  $\text{dm}^2$**

**Soln:**

Given

Diameter to top of bucket = 40 cm

$$\text{Radius } (r_1) = \frac{40}{2} = 20\text{cm}$$

Diameter of bottom part of the bucket = 20 cm

$$\text{Radius } (r_2) = \frac{20}{2} = 10\text{cm}$$

Depth of the bucket (h) = 12 cm

$$\text{Volume of the bucket} = \pi (r_1^2 + r_2^2 + r_1 r_2) h$$

$$= \pi (20^2 + 10^2 + 20 \times 10) \times 12$$

$$= 8800\text{cm}^3$$

Let 'L' be slant height of the bucket

$$\Rightarrow L = \sqrt{(r_1 - r_2)^2 + h^2}$$

$$\Rightarrow L = \sqrt{(20 - 10)^2 + 12^2}$$

$$\Rightarrow L = 15.620\text{cm}$$

$$\text{Total surface area of bucket} = \pi (r_1 + r_2) \times L + \pi r_2^2$$

$$= \pi (20 + 10) \times 15.620 + \pi \times 10^2$$

$$= 1320\sqrt{61} + 2200\pi$$

$$= 17.87\text{dm}^2$$

Given that cost of tin sheet used for making bucket per  $\text{dm}^2$  = Rs 1.20

$$\text{So total cost for } 17.87\text{dm}^2 = 1.20 \times 17.87$$

$$= \text{Rs } 21.40.$$

∴

$$\text{Cost for } 17.87\text{dm}^2 \times 17.87 \text{ dm}^2 = \text{Rs } 21.40$$

**Q2. A frustum of a right circular cone has a diameter of base 20cm, of top 12 cm and height 3 cm. find the area of its whole surface and volume.**

**Sol:**

$$\text{Given base diameter of cone } (d_1)(d_1) = 20\text{cm}$$

$$\text{Radius } (r_1)(r_1) = \frac{20}{2}\text{cm} = 10\text{cm}$$

$$\text{Top diameter of Cone } (d_2)(d_2) = 12 \text{ cm}$$

$$\text{Radius } (r_2)(r_2) = \frac{12}{2}\text{cm} = 6\text{cm}$$

$$\text{Height of the cone } (h) = 3\text{cm}$$

$$\text{Volume of the frustum right circular cone} = \frac{\pi}{3}(r_1^2 + r_2^2 + r_1 r_2)h$$

$$= \frac{\pi}{3}(10^2 + 6^2 + 10 \times 6) \times 3$$

$$= 616 \text{ cm}^3$$

Let 'L' be the slant height of cone

$$\Rightarrow L = \sqrt{(r_1 - r_2)^2 + h^2}$$

$$\Rightarrow L = \sqrt{(10 - 6)^2 + 3^2}$$

$$\Rightarrow L = \sqrt{25}$$

$$\Rightarrow L = 5 \text{ cm}$$

∴ Slant height of cone (L) = 5 cm

$$\text{Total surface area of the cone} = \pi(r_1 + r_2)L + \pi r_1^2 + \pi r_2^2$$

$$= \pi(10 + 6) \times 5 + \pi \times 10^2 + \pi \times 6^2$$

$$= \pi(80 + 100 + 36)$$

$$= \pi(216)$$

$$= 678.85 \text{ cm}^2$$

$$= 678.85 \text{ cm}^2$$

∴

Total surface area of the cone =  $678.85 \text{ cm}^2$

**Q 3. The slant height of the frustum of a cone is 4 cm and perimeters of its circular ends are 18 cm and 6 cm. Find the curved surface of the frustum.**

**Soln:**

Given slant height of frustum of cone ( $l$ ) = 4 cm

Let ratio of the top and bottom circles be  $r_1$  and  $r_2$

Given perimeters of its ends as 18 cm and 6 cm

$$\Rightarrow 2\pi r_1 = 18 \text{ cm} \quad ; \quad 2\pi r_2 = 6 \text{ cm}$$

$$\Rightarrow \pi r_1 = 9 \text{ cm} \text{ --- (a)} \quad ; \quad \pi r_2 = 3 \text{ cm --- (b)}$$

$$\text{Curved surface area of frustum cone} = \pi(r_1 + r_2)l$$

$$= \pi(r_1 + r_2)l$$

$$= (\pi r_1 + \pi r_2)l$$

$$= (9 + 3) \times 4$$

$$= 12 \times 4$$

$$= 48 \text{ cm}^2$$

$$\therefore \text{Curved surface area of the frustum cone} = 48 \text{ cm}^2$$

**Q4. The perimeters of the ends of a frustum of a right circular cone are 44 cm and 33 cm. If the height of the frustum be 16 cm, find its volume, the slant surface and the total surface.**

**Soln:**

Given:

Perimeters of ends of frustum right circular cone are 44 cm and 33 cm

Height of the frustum cone = 16 cm

$$\text{Perimeter} = 2\pi r$$

$$2\pi r_1 h = 44 \quad ; \quad 2\pi r_2 h = 33$$

$$r_1 h = 7 \text{ cm} \quad ; \quad r_2 h = 5.25 \text{ cm}$$

Let the slant height of frustum right circular cone be L

$$L = \sqrt{(r_1 - r_2)^2 + h^2}$$

$$L = \sqrt{(7 - 5.25)^2 + 16^2}$$

$$L = 16.1 \text{ cm}$$

∴ Slant height of the frustum cone = 16.1 cm

$$\text{Curved surface area of the frustum cone} = \pi(r_1 + r_2)L$$

$$= \pi(7 + 5.25)16.1$$

$$\text{Curved surface area of the frustum cone} = 619.65 \text{ cm}^2$$

$$\text{Volume of the frustum cone} = \frac{1}{3}\pi(r_1^2 + r_2^2 + r_1 r_2)h$$

$$= \frac{1}{3}\pi(7^2 + 5.25^2 + 7 \times 5.25) \times 16$$

$$= 1898.56 \text{ cm}^3$$

∴ volume of the cone = 1898.56 cm<sup>3</sup>

$$\text{Total surface area of the frustum cone} = \pi(r_1 + r_2)L + \pi r_1^2 + \pi r_2^2$$

$$= \pi(7 + 5.25) \times 16.1 + \pi 7^2 + \pi 5.25^2$$

$$= \pi(7 + 5.25) \times 16.1 + \pi(7^2 + 5.25^2)$$

$$= 860.27 \text{ cm}^2$$

∴ total surface area of the frustum cone = 860.27 cm<sup>2</sup>

**Q.5: If the radius of circular ends of a conical bucket which is 45 cm high be 28 cm and 7 cm. Find the capacity of the bucket.**

**Soln:**

Given

Height of the conical bucket = 45 cm

Radii of the 2 circular ends of the conical bucket is 28 cm and 7 cm

$$r_1 = 28 \text{ cm}$$

$$r_2 = 7 \text{ cm}$$

$$\text{Volume of the conical bucket} = \frac{1}{3} \pi (r_1^2 + r_2^2 + r_1 r_2) h$$

$$= \frac{1}{3} \pi (28^2 + 7^2 + 28 \times 7) \times 45$$

$$= 15435 \pi$$

$$\text{Volume} = 48510 \text{ cm}^3$$

**Q7. If the radii of circular end of a bucket 24 cm high are 5 and 15 cm. Find surface area of the bucket.**

**Soln:**

Given height of the bucket (h) = 24 cm

Radius of the circular ends of the bucket 5 cm and 15 cm

$$r_1 = 5 \text{ cm} \quad ; \quad r_2 = 15 \text{ cm}$$

Let 'L' be the slant height of the bucket

$$L = \sqrt{(r_1 - r_2)^2 + h^2}$$

$$\Rightarrow L = \sqrt{(5 - 15)^2 + 24^2}$$

$$\Rightarrow L = \sqrt{100 + 576}$$

$$\Rightarrow L = 26 \text{ cm}$$

$$\text{Curved surface area of the bucket} = \pi (r_1 + r_2) L + \pi r_2^2$$

$$= \pi (5 + 15) 26 + \pi 15^2$$

$$= \pi (520 + 225)$$

$$= 745 \pi \text{ cm}^2$$

$$\text{Curved surface area of the bucket} = 745 \pi \text{ cm}^2$$

**Q8. The radii of circular bases of a frustum of a right circular cone are 12 cm and 3 cm and the height is 15 cm. Find the total surface area and volume of frustum.**

**Soln:**

Let slant height of the frustum cone be 'L'

Given height of frustum cone = 15 cm

Radii of a frustum cone are 12 cm and 3 cm

$$r_1 = 12 \text{ cm} \quad ; \quad r_2 = 3 \text{ cm}$$

$$L = \sqrt{(r_1 - r_2)^2 + h^2} = \sqrt{(12 - 3)^2 + 15^2}$$

L = Extra close brace or missing open brace

$$L = \sqrt{81 + 225} = \sqrt{306} = 17.63 \text{ cm}$$

$$L = 17.63 \text{ cm}$$

$$\text{Total surface area of cone} = \pi(r_1 + r_2)L + \pi r_1^2 + \pi r_2^2$$

$$= \pi(12 + 3)17.63 + \pi(12)^2 + \pi(3)^2$$

$$\text{Total surface area} = 378 \text{ cm}^2$$

$$\text{Volume of frustum cone} = \frac{1}{3}\pi(r_1^2 + r_1r_2 + r_2^2)h$$

$$= \frac{1}{3}\pi(12^2 + 12 \times 3 + 3^2) \times 15 = 756\pi \text{ cm}^3$$

$$\text{Volume of the frustum cone} = 756\pi \text{ cm}^3$$

**Q9. A tent consists of a frustum of a cone capped by a cone. If radii of ends of frustum be 13 m and 7 m the height of frustum be 8 m and the slant height of the conical cap be 12 m. Find canvas required for the tent.**

**Soln:**

Given height of frustum (h) = 8 m

Radii of the frustum cone are 13 cm and 7 cm

$$r_1 = 13 \text{ m} \quad ; \quad r_2 = 7 \text{ m}$$

Let 'L' be slant height of the frustum cone

$$\Rightarrow L = \sqrt{(r_1 - r_2)^2 + h^2} = \sqrt{(13 - 7)^2 + 8^2}$$

$$\Rightarrow L = \sqrt{36 + 64} = \sqrt{100}$$

$$\Rightarrow L = 10 \text{ m}$$

$$\Rightarrow L = 10 \text{ m}$$

Curved surface area of frustum ( $s_1$ ) =  $\pi(r_1 + r_2) \times L$

$$= \pi(13 + 7) \times 10 = 200\pi \text{ m}^2$$

$$= 200\pi \text{ m}^2$$

Curved surface area of frustum ( $s_1$ ) =  $200\pi \text{ m}^2$

Given slant height of conical cap = 12 m

Base radius of upper cap cone = 7 m

Curved surface area of upper cap cone ( $s_2$ ) =  $\pi r L$

$$= \pi \times 7 \times 12 = 84\pi \text{ m}^2$$

$$= 84\pi \text{ m}^2$$

Total canvas required for tent ( $S$ ) =  $s_1 + s_2$

$$S = 200\pi + 84\pi = 284\pi \approx 892.57 \text{ m}^2$$

$$\therefore \text{total canvas} = 892.57 \text{ m}^2$$

**Q10. A bucket is in the form of a frustum of a cone with a capacity of  $12308.8 \text{ cm}^3$  of water. Radii of the top and bottom circular ends are 20 cm and 12 cm respectively. Find the height of the bucket and the area of the metal sheet used in its making.**

**Soln:**

Radii of top circular ends ( $r_1$ ) = 20 cm

Radii of bottom circular end of bucket ( $r_2$ ) = 12 cm

Let height of bucket be 'h'



$$\begin{aligned} \text{Volume of frustum cone} &= \frac{1}{3}\pi(r_1^2 + r_2^2 + r_1 r_2)h \\ &= \frac{1}{3}\pi(20^2 + 12^2 + 20 \times 12)h \\ &= \frac{784}{3}\pi h \text{ cm}^3 \text{ ---(a)} \end{aligned}$$

$$\text{Given capacity/ volume of the bucket} = 12308.8 \text{ cm}^3 \text{ ---(b)}$$

Equating (a) and (b)

$$\Rightarrow \frac{784}{3}\pi h \text{ cm}^3 = 12308.8$$

$$\Rightarrow h = \frac{12308.8 \times 3}{784 \times \pi}$$

$$\Rightarrow h = 15 \text{ cm}$$

∴ height of the bucket (h) = 15 cm

Let 'L' be slant height of bucket

$$\Rightarrow L^2 = (r_1 - r_2)^2 + h^2$$

$$\Rightarrow L = \sqrt{(r_1 - r_2)^2 + h^2}$$

$$\Rightarrow L = 17 \text{ cm}$$

∴ length of the bucket/ slant height of the bucket (L) = 17 cm

$$\text{Curved surface area of bucket} = \pi(r_1 + r_2)L + \pi r_2^2$$

$$= \pi(20 + 12)17 + \pi \times 12^2$$

$$= \pi(9248 + 144)$$

$$= 2160.32 \text{ cm}^2$$

∴ curved surface area = 2160.32 cm<sup>2</sup>

**Q11. A bucket made of aluminum sheet is of height 20 cm and its upper and lower ends are of radius 25 cm and 10 cm. Find cost of making if the aluminum sheet costs Rs 70 per 100 cm<sup>2</sup> cm<sup>2</sup>.**

**Soln:**

Given height of bucket (h) = 20 cm

Upper radius of bucket ( $r_1$ ) ( $r_1$ ) = 25 cm

Lower radius of the bucket ( $r_2$ ) ( $r_2$ ) = 10 cm

Let 'L' be slant height of the bucket

$$\begin{aligned} L &= \sqrt{(r_1 - r_2)^2 + h^2} \sqrt{(r_1 - r_2)^2 + h^2} \\ &= \sqrt{(25 - 10)^2 + 20^2} \sqrt{(25 - 10)^2 + 20^2} \\ &= 25 \text{ cm} \end{aligned}$$

∴ slant height of bucket (L) = 25 cm

$$\begin{aligned} \text{Curved surface area of bucket} &= \Pi(r_1 + r_2) \times L + \Pi r_2^2 \\ &= \Pi(25 + 10) \times 25 + \Pi \times 10^2 \\ &= 3061.5 \text{ cm}^2 \end{aligned}$$

∴ curved surface area = 3061.5 cm<sup>2</sup>

Cost of making bucket per 100 cm<sup>2</sup> = Rs 70

$$\begin{aligned} \text{Cost of making bucket per } 3061.5 \text{ cm}^2 &= 3061.5 \times \frac{70}{100} \\ &= \text{Rs } 2143.05 \end{aligned}$$

Total cost for 3061.5 cm<sup>2</sup> = Rs 2143.05

**Q12. Radii of circular ends of a solid frustum of a cone are 33 cm and 27 cm and its slant height is 10 cm. Find its total surface area.**

**Soln:**

Given slant height of frustum cone = 10 cm

Radii of circular ends of frustum cone are 33 cm and 27 cm

$$r_1 = 33 \text{ cm} \quad ; \quad r_2 = 27 \text{ cm}$$

Total surface area of a solid frustum of cone

$$= \Pi(r_1 + r_2) \times L + \Pi r_1^2 + \Pi r_2^2$$

$$= \pi(33+27) \times 10 + \pi 33^2 + \pi 27^2 \pi(33 + 27) \times 10 + \pi 33^2 + \pi 27^2$$

$$= \pi(60) \times 10 + \pi 33^2 + \pi 27^2 \pi(60) \times 10 + \pi 33^2 + \pi 27^2$$

$$= \pi(600 + 1089 + 729) \pi(600 + 1089 + 729)$$

$$= 2418 \pi \text{cm}^2 \pi \text{cm}^2$$

$$\therefore \text{Total surface area} = 7599.42 \text{ cm}^2 \text{cm}^2$$

**Q13. A bucket made up of a metal sheet is in form of a frustum of cone of height 16 cm with diameters of its lower and upper ends as 16 cm and 40 cm. Find the volume of the bucket. Also find the cost of the bucket if the cost of metal sheet used is Rs 20 per 100 cm<sup>2</sup>cm<sup>2</sup>.**

**Soln:**

Given height of frustum cone = 16 cm

Diameter of the lower end of the bucket  $d_1 = 16 \text{ cm}$   $d_1 = 16 \text{ cm}$

Lower end radius  $r_1 = \frac{16}{2} = 8 \text{ cm}$   $r_1 = \frac{16}{2} = 8 \text{ cm}$

Upper end radius  $r_2 = \frac{40}{2} = 20 \text{ cm}$   $r_2 = \frac{40}{2} = 20 \text{ cm}$

Let 'L' be slant height of frustum of cone

$$L = \sqrt{(r_1 - r_2)^2 + h^2} \sqrt{(r_1 - r_2)^2 + h^2}$$

$$L = \sqrt{(20 - 8)^2 + 16^2} \sqrt{(20 - 8)^2 + 16^2}$$

$$L = \sqrt{(114 + 256)} \sqrt{(114 + 256)}$$

$$L = 20 \text{ cm}$$

$\therefore$  slant height of the frustum cone  $L = 20 \text{ cm}$

Volume of the frustum cone =  $\frac{1}{3} \pi (r_1^2 + r_2^2 + r_1 \times r_2) \times h$   $\frac{1}{3} \pi (r_1^2 + r_2^2 + r_1 \times r_2) \times h$

$$= \frac{1}{3} \pi (8^2 + 20^2 + 8 \times 20) \times 16 \frac{1}{3} \pi (8^2 + 20^2 + 8 \times 20) \times 16$$

Volume of the frustum cone = 10449.92 cm<sup>3</sup>cm<sup>3</sup>

Curved surface area of the frustum cone =  $\pi(r_1 + r_2) \times L + \pi r_1^2 \pi(r_1 + r_2) \times L + \pi r_1^2$   $\pi(r_1 + r_2) \times L + \pi r_1^2$

$$= \pi(20 + 8) \times 20 + \pi 8^2 \pi(20 + 8) \times 20 + \pi 8^2$$

$$= \pi(560+64)\pi(560 + 64)$$

$$= 624 \pi \text{cm}^2 \pi \text{cm}^2$$

$$\text{Cost of the metal sheet per } 100 \text{ cm}^2 \text{cm}^2 = \text{Rs } 20$$

$$\text{Cost of the metal sheet per } 624 \pi \text{cm}^2 \pi \text{cm}^2 = 624 \pi 100 \times 20 \frac{624 \pi}{100} \times 20$$

$$\therefore \text{Cost of the metal sheet} = 391.9$$

**Q14. A solid is in the shape of a frustum of a cone. The diameters of two circular ends are 60 cm and 36 cm and height is 9 cm. find area of its whole surface and volume.**

**Soln:**

given height of the frustum cone = 9 cm

$$\text{Lower end radius } r_1 = \frac{60}{2} = 30 \text{ cm}$$

$$\text{Upper end radius } r_2 = \frac{36}{2} = 18 \text{ cm}$$

Let slant height of the frustum cone be L

$$L = \sqrt{(r_1 - r_2)^2 + h^2} = \sqrt{(30 - 18)^2 + 9^2}$$

$$L = \sqrt{(18 - 30)^2 + 9^2} = \sqrt{144 + 81}$$

$$L = \sqrt{144 + 81} = \sqrt{225}$$

$$L = 15 \text{ cm}$$

$$\text{Volume of the frustum cone} = \frac{1}{3} \pi (r_1^2 + r_2^2 + r_1 \times r_2) \times h$$

$$= \frac{1}{3} \pi (30^2 + 18^2 + 30 \times 18) \times 9$$

$$= 5292 \pi \text{cm}^3$$

$$\text{Volume} = 5292 \pi \text{cm}^3$$

$$\text{Total surface area of frustum cone} = \pi(r_1 + r_2) \times L + \pi r_1^2 + \pi r_2^2$$

$$= \pi(30 + 18) \times 15 + \pi 30^2 + \pi 18^2$$

$$= \pi(720 + 900 + 324)$$

$$= 1944\pi \text{ cm}^2 + 1944\pi \text{ cm}^2$$

$$\therefore \text{ total surface area} = 1944\pi \text{ cm}^2 + 1944\pi \text{ cm}^2$$

**Q15. A milk container is made of metal sheet in the shape of frustum cone whose volume is  $10459 \text{ cm}^3$ . The radii of its lower and upper circular ends are 8 cm and 20 cm. Find the cost of metal sheet used in making container at a rate of Rs 1.40 per  $\text{cm}^2$ .**

**Soln:**

Given,

$$\text{Lower end radius } r_1 = 8 \text{ cm}$$

$$\text{upper end radius } r_2 = 20 \text{ cm}$$

Let the height of the container be 'h'

$$V_1 = \frac{1}{3} \pi (8^2 + 20^2 + 8(20)) h \text{ cm}^3 \quad \text{--- (1)}$$

$$\text{Volume of the milk container} = 10459 \text{ cm}^3$$

$$V_2 = \frac{73216}{7} \text{ cm}^3$$

$$V_1 - V_2$$

$$\frac{1}{3} \pi (8^2 + 20^2 + 8(20)) h \text{ cm}^3 - \frac{73216}{7} \text{ cm}^3$$

$$\Rightarrow h = \frac{10459.4265345 \times 3}{\frac{1}{3} \pi (8^2 + 20^2 + 8(20)) - \frac{73216}{7}}$$

$$\Rightarrow h = 16 \text{ cm}$$

$\therefore$  Height of frustum cone (h) = 16 cm

Let slant height of frustum cone be 'L'

$$L = \sqrt{(r_1 - r_2)^2 + h^2} = \sqrt{(8 - 20)^2 + 16^2}$$

$$L = \sqrt{(20 - 8)^2 + 16^2} = \sqrt{16^2 + 16^2}$$

$$L = 20 \text{ cm}$$

$\therefore$  Slant height of frustum cone (L) = 20 cm

Total surface area of the frustum cone

$$\begin{aligned}
&= \pi(r_1+r_2) \times L + \pi r_1^2 + \pi r_2^2 \\
&= \pi(20+8) \times 20 + \pi 20^2 + \pi 8^2 \\
&= \pi(560+400+64) \\
&= 1024\pi \\
&= 3216.99 \text{ cm}^2
\end{aligned}$$

Total surface area of the frustum =  $3216.99 \text{ cm}^2$

**Q.16: A reservoir in form of frustum of a right circular cone contains  $44 \times 10^7$  liters of water which fills it completely. The radii of bottom and top of the reservoir are 50 m and 100 m. Find the depth of water and lateral surface area of the reservoir.**

**Soln:**

Let depth of frustum cone be h

$$\text{Volume of first cone (V)} = \frac{1}{3} \pi (r_1^2 + r_2^2 + r_1 \times r_2) \times h$$

$$r_1 = 50 \text{ m} \quad ; \quad r_2 = 100$$

$$V = \frac{1}{3} \pi (50^2 + 100^2 + 50 \times 100) h$$

$$V = \frac{1}{3} \pi (2500 + 10000 + 5000) h \text{ --- (a)}$$

$$\text{Volume of the reservoir} = 44 \times 10^7 \text{ liters --- (b)}$$

Equating (a) and (b)

$$\frac{1}{3} \pi (8500) h = 44 \times 10^7$$

$$h = 24$$

**Q.17: A metallic right circular cone 20 cm high and whose vertical angle is  $90^\circ$  is cut into two parts at the middle point of its axis by a plane parallel to the base. If frustum so obtained be drawn into a wire of diameter  $\frac{1}{16}$  cm. Find the length of the wire.**

**Soln:**

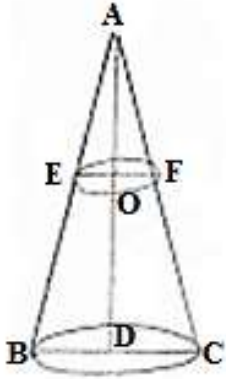
Let ABC be the cone. Height of metallic cone

AO = 20 cm

-> Cone is cut into two parts at the middle point of its axis

Hence height of frustum cone AD = 10 cm

Since angle A is right angles. So each angles B and C = 45° 45°



Angles E and F = 45° 45°

Let radii of top and bottom circle of frustum

Cone be  $r_1$  and  $r_2$

From  $\triangle ADE$   $\Rightarrow \cot 45^\circ = \frac{DE}{AD} = \cot 45^\circ$

$$\Rightarrow r_1 = 10 = 1 \frac{r_1}{10} = 1$$

$$\Rightarrow r_1 = 10 \text{ cm}$$

From  $\triangle AOB$

$\Rightarrow \cot 45^\circ = \frac{OE}{OA} = \cot 45^\circ$

$$\Rightarrow r_2 = 20 = 1 \frac{r_2}{20} = 1$$

$$\Rightarrow r_2 = 20 \text{ cm}$$