

RD SHARMA

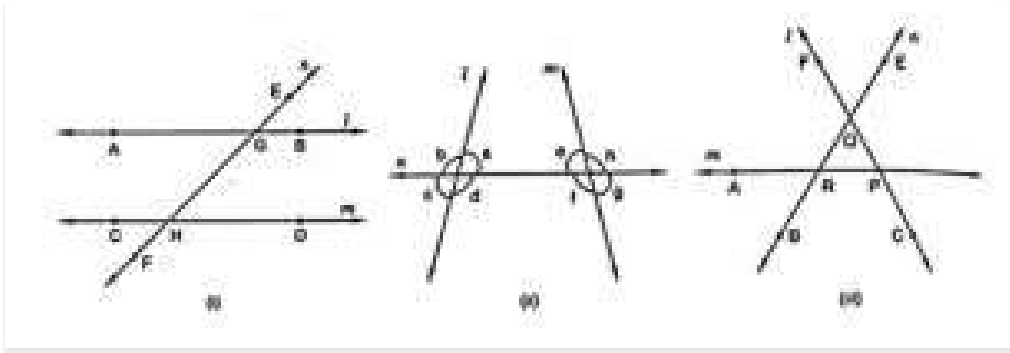
Solutions

Class 7 Maths

Chapter 14

Ex 14.2

Q1. In Figure, line n is a transversal to line l and m. Identify the following:



(i) Alternate and corresponding angles in Fig. 58 (i)

(ii) Angles alternate to $\angle d$ and $\angle g$ and angles corresponding to $\angle RQF$ and angle alternate to $\angle PQE$ in Fig. 58 (ii)

(iii) Angle alternate to $\angle PQR$, angle corresponding to $\angle RQF$ and angle alternate to $\angle PQE$ in Fig. 58 (iii)

(iv) Pairs of interior and exterior angles on the same side of the transversal in Fig. 58 (iii)

Sol:

(i) Figure (i)

Corresponding angles :

$\angle EGB$ and $\angle GHD$

$\angle HGB$ and $\angle FHD$

$\angle EGA$ and $\angle GHC$

$\angle AGH$ and $\angle CHF$

The alternate angles are :

$\angle EGB$ and $\angle CHF$

$\angle HGB$ and $\angle CHG$

$\angle EGA$ and $\angle FHD$

$\angle AGH$ and $\angle GHD$

(ii) Figure (ii)

The alternate angle to $\angle d$ is $\angle e$.

The alternate angle to $\angle g$ is $\angle b$.

The corresponding angle to $\angle f$ is $\angle c$.

The corresponding angle to $\angle h$ is $\angle a$.

(iii) Figure (iii)

Angle alternate to $\angle PQR$ is $\angle QRA$.

Angle corresponding to $\angle RQF$ is $\angle ARB$.

Angle alternate to $\angle POE$ is $\angle ARB$.

(iv) Figure (ii)

Pair of interior angles are

$\angle a$ is $\angle e$.

$\angle d$ is $\angle f$.

Pair of exterior angles are

$\angle b$ is $\angle h$.

$\angle c$ is $\angle g$.

Q2. In Figure, AB and CD are parallel lines intersected by a transversal PQ at L and M respectively, If $\angle CMQ = 60^\circ$, find all other angles in the figure.

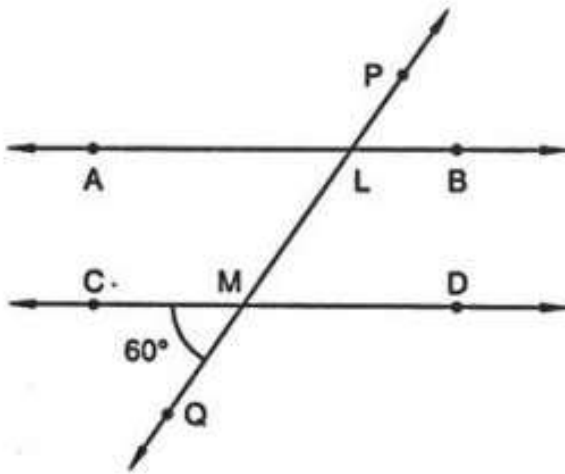


Fig. 59

Sol:

Corresponding angles :

$$\angle ALM = \angle CMQ = 60^\circ$$

Vertically opposite angles :

$$\angle LMD = \angle CMQ = 60^\circ$$

Vertically opposite angles :

$$\angle ALM = \angle PLB = 60^\circ$$

Here,

$$\angle CMQ + \angle QMD = 180^\circ \text{ are the linear pair}$$

$$\Rightarrow \angle QMD = 180^\circ - 60^\circ$$

$$= 120^\circ$$

Corresponding angles :

$$\angle QMD = \angle MLB = 120^\circ$$

Vertically opposite angles

$$\angle QMD = \angle CML = 120^\circ$$

Vertically opposite angles

$$\angle MLB = \angle ALP = 120^\circ$$

Q3. In Fig. 60, AB and CD are parallel lines intersected by a transversal PQ at L and M respectively. If $\angle LMD = 35^\circ$ find $\angle ALM$ and $\angle PLA$.

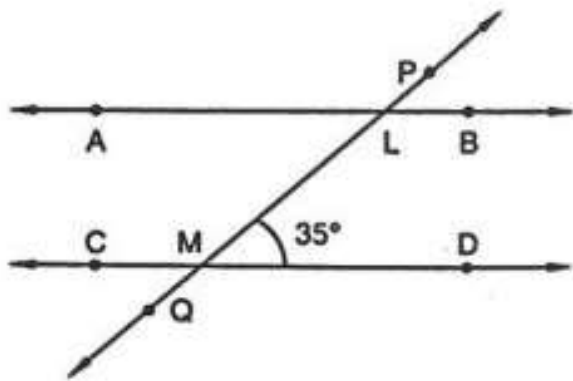


Fig. 60

Sol:

Given that,

$$\angle LMD = 35^\circ$$

$\angle LMD$ and $\angle LMC$ is a linear pair

$$\angle LMD + \angle LMC = 180^\circ$$

$$\Rightarrow \angle LMC = 180^\circ - 35^\circ$$

$$= 145^\circ$$

$$\text{So, } \angle LMC = \angle PLA = 145^\circ$$

$$\text{And, } \angle LMC = \angle MLB = 145^\circ$$

$\angle MLB$ and $\angle ALM$ is a linear pair

$$\angle MLB + \angle ALM = 180^\circ$$

$$\Rightarrow \angle ALM = 180^\circ - 145^\circ$$

$$\Rightarrow \angle ALM = 35^\circ$$

Therefore, $\angle ALM = 35^\circ$, $\angle PLA = 145^\circ$.

Q4. The line n is transversal to line l and m in Fig. 61. Identify the angle alternate to $\angle 13$, angle corresponding to $\angle 15$, and angle alternate to $\angle 15$.

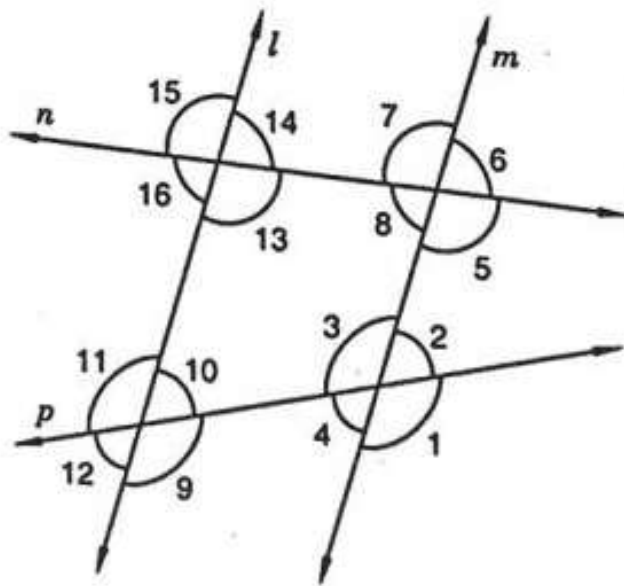


Fig. 61

Sol:

Given that, $l \parallel m$

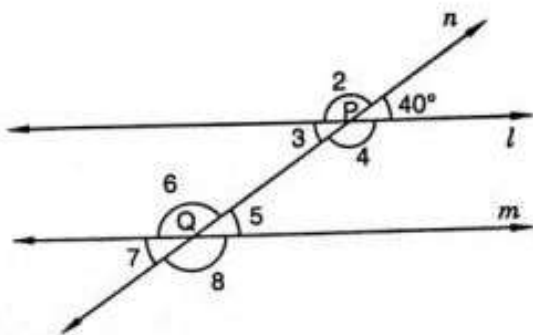
So,

The angle alternate to $\angle 13$ is $\angle 7$

The angle corresponding to $\angle 15$ is $\angle 7$

The angle alternate to $\angle 15$ is $\angle 5$

Q5. In Fig. 62, line $l \parallel m$ and n is transversal. If $\angle 1 = 40^\circ$, find all the angles and check that all corresponding angles and alternate angles are equal.



Sol:

Given that,

$$\angle 1 = 40^\circ$$

$\angle 1$ and $\angle 2$ is a linear pair

$$\Rightarrow \angle 1 + \angle 2 = 180^\circ$$

$$\Rightarrow \angle 2 = 180^\circ - 40^\circ$$

$$\Rightarrow \angle 2 = 140^\circ$$

$\angle 2$ and $\angle 6$ is a corresponding angle pair

So, $\angle 6 = 140^\circ$

$\angle 6$ and $\angle 5$ is a linear pair

$$\Rightarrow \angle 6 + \angle 5 = 180^\circ$$

$$\Rightarrow \angle 5 = 180^\circ - 140^\circ$$

$$\Rightarrow \angle 5 = 40^\circ$$

$\angle 3$ and $\angle 5$ are alternative interior angles

$$\text{So, } \angle 5 = \angle 3 = 40^\circ$$

$\angle 3$ and $\angle 4$ is a linear pair

$$\Rightarrow \angle 3 + \angle 4 = 180^\circ$$

$$\Rightarrow \angle 4 = 180^\circ - 40^\circ$$

$$\Rightarrow \angle 4 = 140^\circ$$

$\angle 4$ and $\angle 6$ are a pair interior angles

$$\text{So, } \angle 4 = \angle 6 = 140^\circ$$

$\angle 3$ and $\angle 7$ are pair of corresponding angles

$$\text{So, } \angle 3 = \angle 7 = 40^\circ$$

Therefore, $\angle 7 = 40^\circ$

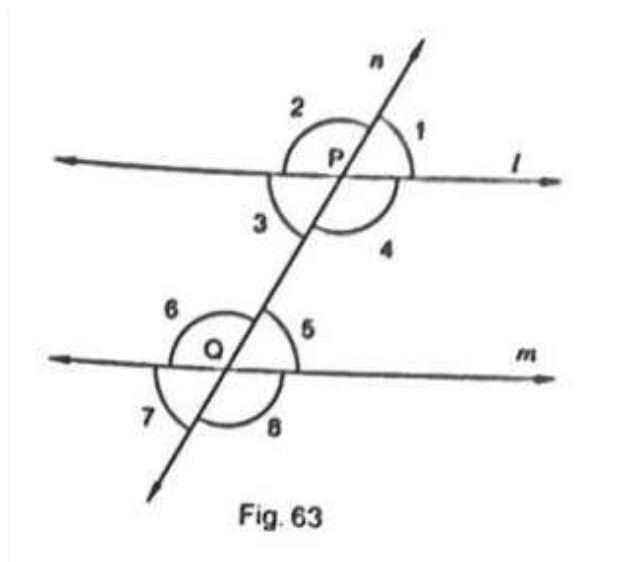
$\angle 4$ and $\angle 8$ are a pair corresponding angles

$$\text{So, } \angle 4 = \angle 8 = 140^\circ$$

Therefore, $\angle 8 = 140^\circ$

$$\text{So, } \angle 1 = 40^\circ, \angle 2 = 140^\circ, \angle 3 = 40^\circ, \angle 4 = 140^\circ, \angle 5 = 40^\circ, \angle 6 = 140^\circ, \angle 7 = 40^\circ, \angle 8 = 140^\circ$$

Q6. In Fig. 63, line $l \parallel m$ and a transversal n cuts them P and Q respectively. If $\angle 1 = 75^\circ$, find all other angles.



Sol:

Given that, $l \parallel m$ and $\angle 1 = 75^\circ$

We know that,

$$\angle 1 + \angle 2 = 180^\circ \text{ — (linear pair)}$$

$$\Rightarrow \angle 2 = 180^\circ - 75^\circ$$

$$\Rightarrow \angle 2 = 105^\circ$$

here, $\angle 1 = \angle 5 = 75^\circ$ are corresponding angles

$\angle 5 = \angle 7 = 75^\circ$ are vertically opposite angles.

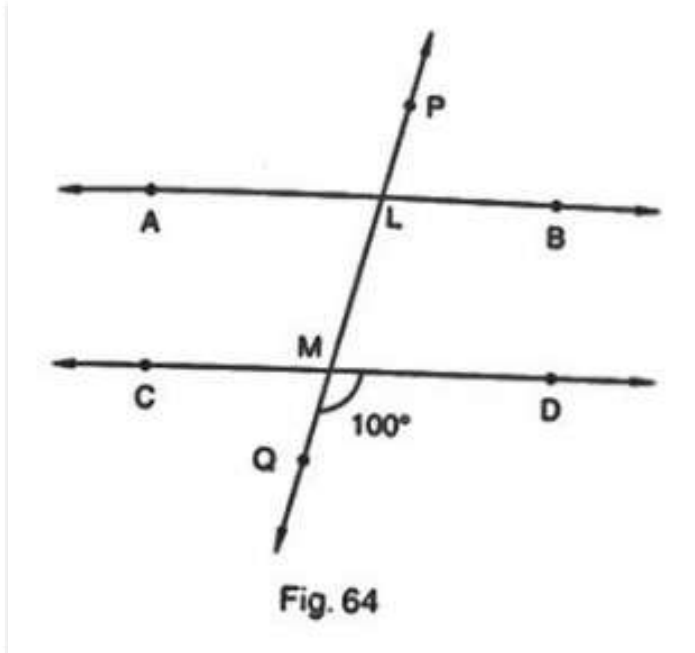
$\angle 2 = \angle 6 = 105^\circ$ are corresponding angles

$\angle 6 = \angle 8 = 105^\circ$ are vertically opposite angles

$\angle 2 = \angle 4 = 105^\circ$ are vertically opposite angles

So, $\angle 1 = 75^\circ, \angle 2 = 105^\circ, \angle 3 = 75^\circ, \angle 4 = 105^\circ, \angle 5 = 75^\circ, \angle 6 = 105^\circ, \angle 7 = 75^\circ, \angle 8 = 105^\circ$

Q7. In Fig. 64, $AB \parallel CD$ and a transversal PQ cuts at L and M respectively. If $\angle QMD = 100^\circ$, find all the other angles.



Sol:

Given that, $AB \parallel CD$ and $\angle QMD = 100^\circ$

We know that,

Linear pair,

$$\angle QMD + \angle QMC = 180^\circ$$

$$\Rightarrow \angle QMC = 180^\circ - \angle QMD$$

$$\Rightarrow \angle QMC = 180^\circ - 100^\circ$$

$$\Rightarrow \angle QMC = 80^\circ$$

Corresponding angles,

$$\angle DMQ = \angle BLM = 100^\circ$$

$$\angle CMQ = \angle ALM = 80^\circ$$

Vertically Opposite angles,

$$\angle DMQ = \angle CML = 100^\circ$$

$$\angle BLM = \angle PLA = 100^\circ$$

$$\angle CMQ = \angle DML = 80^\circ$$

$$\angle ALM = \angle PLB = 80^\circ$$

Q8. In Fig. 65, $l \parallel m$ and $p \parallel q$. Find the values of x, y, z, t .

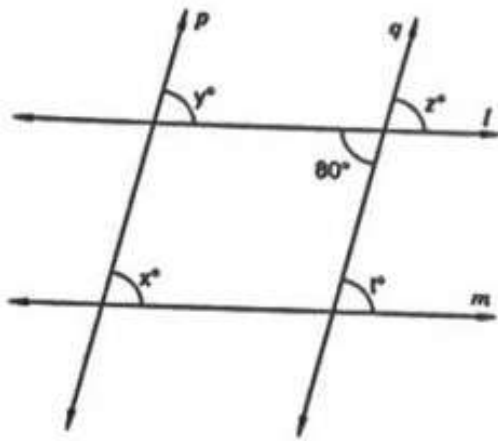


Fig. 65

Sol:

Given that, angle is 80°

$\angle Z$ and 80° are vertically opposite angles

$$\Rightarrow \angle Z = 80^\circ$$

$\angle Z$ and $\angle t$ are corresponding angles

$$\Rightarrow \angle Z = \angle t$$

Therefore, $\angle t = 80^\circ$

$\angle Z$ and $\angle y$ are corresponding angles

$$\Rightarrow \angle Z = \angle y$$

Therefore, $\angle y = 80^\circ$

$\angle X$ and $\angle y$ are corresponding angles

$$\Rightarrow \angle y = \angle X$$

Therefore, $\angle X = 80^\circ$

Q9. In Fig. 66, line $l \parallel m$, $\angle 1 = 120^\circ$ and $\angle 2 = 100^\circ$, find out $\angle 3$ and $\angle 4$.

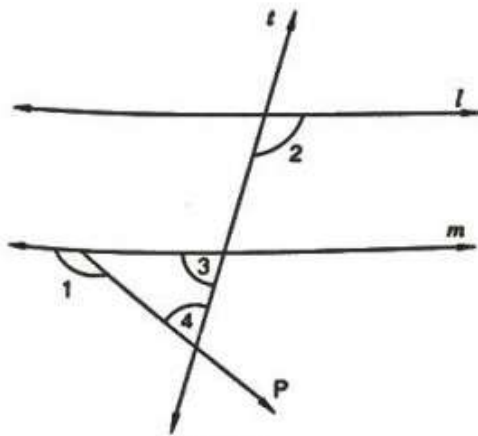


Fig. 66

Sol:

Given that, $\angle 1 = 120^\circ$ and $\angle 2 = 100^\circ$

$\angle 1$ and $\angle 5$ a linear pair

$$\Rightarrow \angle 1 + \angle 5 = 180^\circ$$

$$\Rightarrow \angle 5 = 180^\circ - 120^\circ$$

$$\Rightarrow \angle 5 = 60^\circ$$

Therefore, $\angle 5 = 60^\circ$

$\angle 2$ and $\angle 6$ are corresponding angles

$$\Rightarrow \angle 2 = \angle 6 = 100^\circ$$

Therefore, $\angle 6 = 100^\circ$

$\angle 6$ and $\angle 3$ a linear pair

$$\Rightarrow \angle 6 + \angle 3 = 180^\circ$$

$$\Rightarrow \angle 3 = 180^\circ - 100^\circ$$

$$\Rightarrow \angle 3 = 80^\circ$$

Therefore, $\angle 3 = 80^\circ$

By, angles of sum property

$$\Rightarrow \angle 3 + \angle 5 + \angle 4 = 180^\circ$$

$$\Rightarrow \angle 4 = 180^\circ - 80^\circ - 60^\circ$$

$$\Rightarrow \angle 4 = 40^\circ$$

Therefore, $\angle 4 = 40^\circ$

Q10. In Fig. 67, $l \parallel m$. Find the values of a,b,c,d. Give reasons.

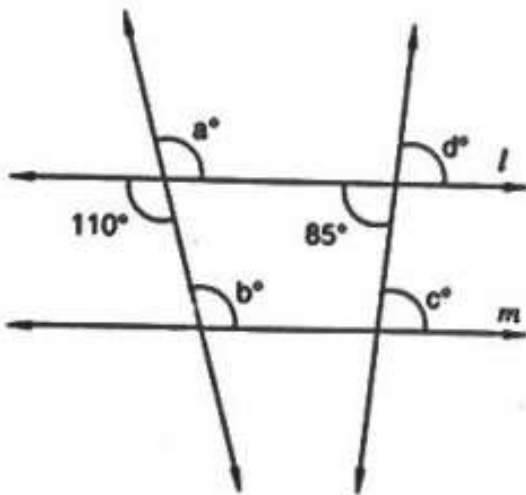


Fig. 67

Sol:

Given that, $l \parallel m$

Vertically opposite angles,

$$\angle a = 110^\circ$$

Corresponding angles,

$$\angle a = \angle b$$

Therefore, $\angle b = 110^\circ$

Vertically opposite angle,

$$\angle d = 85^\circ$$

Corresponding angles,

$$\angle d = \angle c$$

Therefore, $\angle c = 85^\circ$

Hence, $\angle a = 110^\circ$, $\angle b = 110^\circ$, $\angle c = 85^\circ$, $\angle d = 85^\circ$

Q11. In Fig. 68, $AB \parallel CD$ and $\angle 1$ and $\angle 2$ are in the ratio of 3 : 2. Determine all angles from 1 to 8.

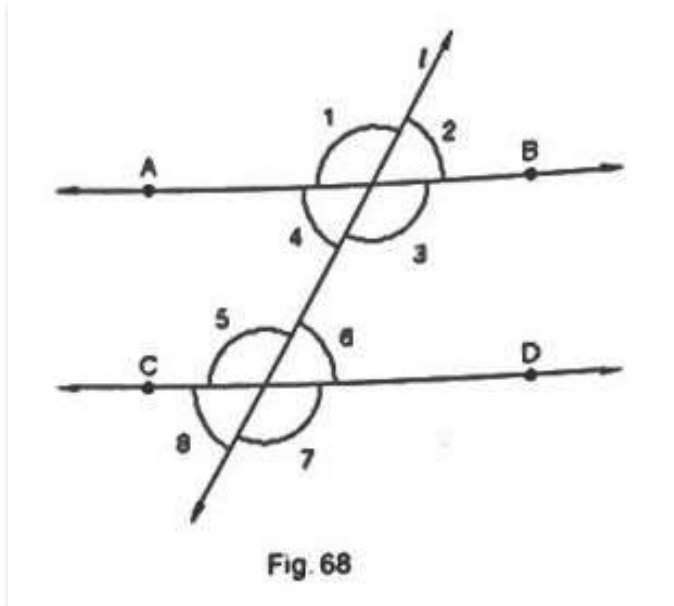


Fig. 68

Sol:

Given that,

$\angle 1$ and $\angle 2$ are 3 : 2

Let us take the angles as $3x$, $2x$

$\angle 1$ and $\angle 2$ are linear pair

$$\Rightarrow 3x + 2x = 180^\circ$$

$$\Rightarrow 5x = 180^\circ$$

$$\Rightarrow x = \frac{180^\circ}{5}$$

$$\Rightarrow x = 36^\circ$$

Therefore, $\angle 1 = 3x = 3(36) = 108^\circ$

$\angle 2 = 2x = 2(36) = 72^\circ$

$\angle 1$ and $\angle 5$ are corresponding angles

$$\Rightarrow \angle 1 = \angle 5$$

Therefore, $\angle 5 = 108^\circ$

$\angle 2$ and $\angle 6$ are corresponding angles

$$\Rightarrow \angle 2 = \angle 6$$

Therefore, $\angle 6 = 72^\circ$

$\angle 4$ and $\angle 6$ are alternate pair of angles

$$\Rightarrow \angle 4 = \angle 6 = 72^\circ$$

Therefore, $\angle 4 = 72^\circ$

$\angle 3$ and $\angle 5$ are alternate pair of angles

$$\Rightarrow \angle 3 = \angle 5 = 108^\circ$$

Therefore, $\angle 5 = 108^\circ$

$\angle 2$ and $\angle 8$ are alternate exterior of angles

$$\Rightarrow \angle 2 = \angle 8 = 72^\circ$$

Therefore, $\angle 8 = 72^\circ$

$\angle 1$ and $\angle 7$ are alternate exterior of angles

$$\Rightarrow \angle 1 = \angle 7 = 108^\circ$$

Therefore, $\angle 7 = 108^\circ$

Hence, $\angle 1 = 108^\circ$, $\angle 2 = 72^\circ$, $\angle 3 = 108^\circ$, $\angle 4 = 72^\circ$, $\angle 5 = 108^\circ$, $\angle 6 = 72^\circ$, $\angle 7 = 108^\circ$, $\angle 8 = 72^\circ$

Q12. In Fig. 69 l, m and n are parallel lines intersected by transversal p at X, Y and Z respectively. Find $\angle 1$, $\angle 2$ and $\angle 3$.

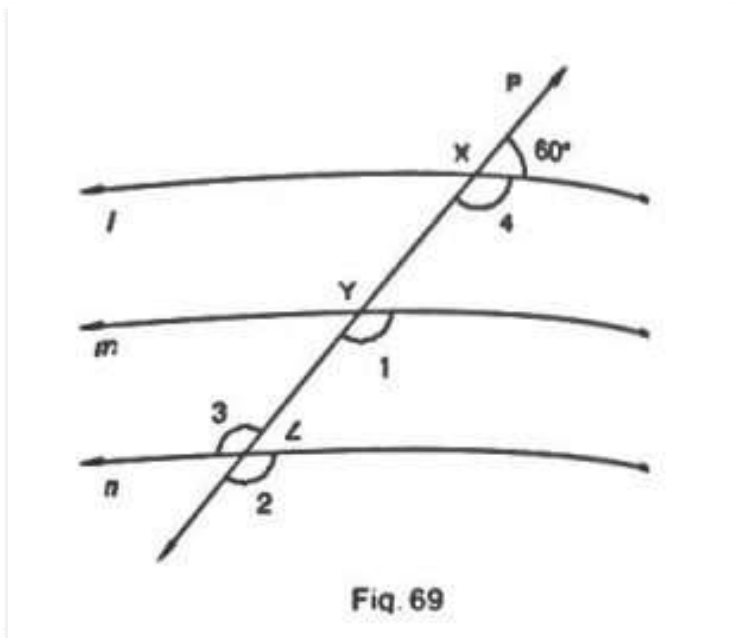


Fig. 69

Sol:

Linear pair,

$$\Rightarrow \angle 4 + 60^\circ = 180^\circ$$

$$\Rightarrow \angle 4 = 180^\circ - 60^\circ$$

$$\Rightarrow \angle 4 = 120^\circ$$

$\angle 4$ and $\angle 1$ are corresponding angles

$$\Rightarrow \angle 4 = \angle 1$$

Therefore, $\angle 1 = 120^\circ$

$\angle 1$ and $\angle 2$ are corresponding angles

$$\Rightarrow \angle 2 = \angle 1$$

Therefore, $\angle 2 = 120^\circ$

$\angle 2$ and $\angle 3$ are vertically opposite angles

$$\Rightarrow \angle 2 = \angle 3$$

Therefore, $\angle 3 = 120^\circ$

Q13. In Fig. 70, if $l \parallel m \parallel n$ and $\angle 1 = 60^\circ$, find $\angle 2$

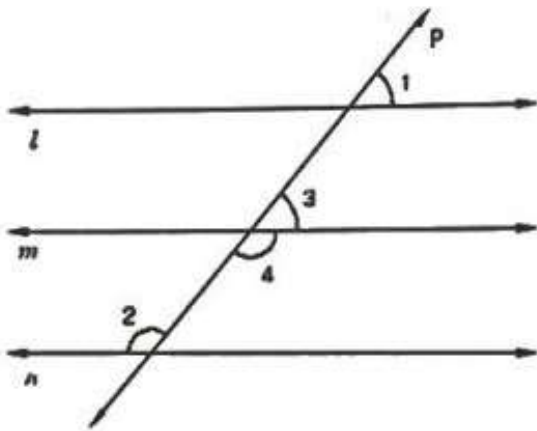


Fig. 70

Sol:

Given that,

Corresponding angles :

$$\angle 1 = \angle 3$$

$$\Rightarrow \angle 1 = 60^\circ$$

Therefore, $\angle 3 = 60^\circ$

$\angle 3$ and $\angle 4$ are linear pair

$$\Rightarrow \angle 3 + \angle 4 = 180^\circ$$

$$\Rightarrow \angle 4 = 180^\circ - 60^\circ$$

$$\Rightarrow \angle 4 = 120^\circ$$

$\angle 3$ and $\angle 4$ are alternative interior angles

$$\Rightarrow \angle 4 = \angle 2$$

Therefore, $\angle 2 = 120^\circ$

Q14. In Fig. 71, if $AB \parallel CD$ and $CD \parallel EF$, find $\angle ACE$.

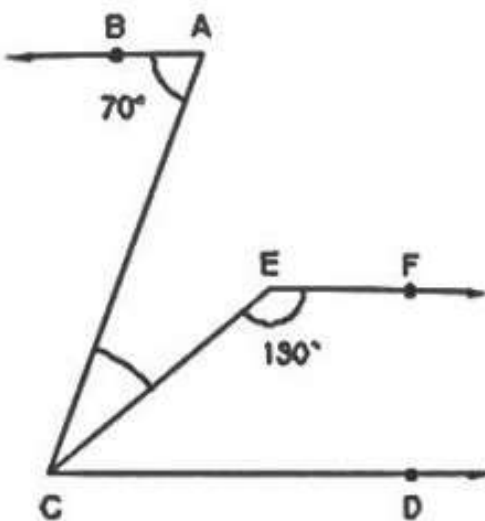


Fig. 71

Sol :

Given that,

Sum of the interior angles,

$$\Rightarrow \angle CEF + \angle ECD = 180^\circ$$

$$\Rightarrow 130^\circ + \angle ECD = 180^\circ$$

$$\Rightarrow \angle ECD = 180^\circ - 130^\circ$$

$$\Rightarrow \angle ECD = 50^\circ$$

We know that alternate angles are equal

$$\Rightarrow \angle BAC = \angle ACD$$

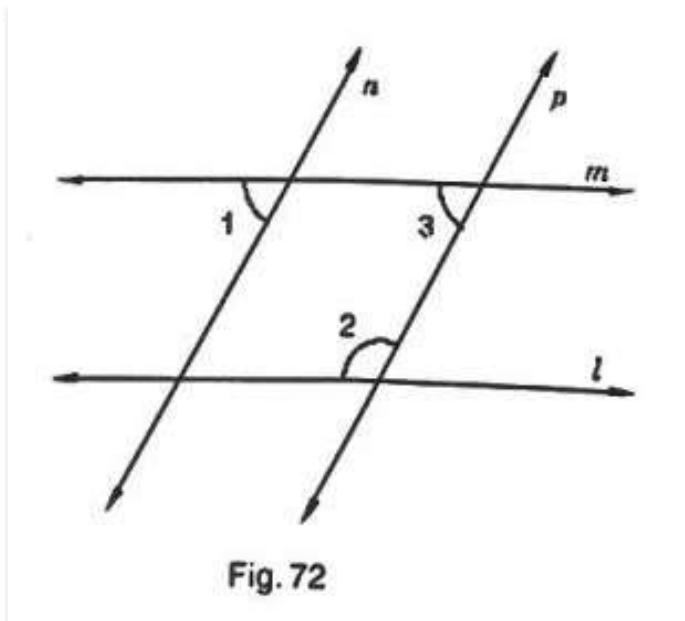
$$\Rightarrow \angle BAC = \angle ECD + \angle ACE$$

$$\Rightarrow \angle ACE = 70^\circ - 50^\circ$$

$$\Rightarrow \angle ACE = 20^\circ$$

Therefore, $\angle ACE = 20^\circ$

Q15. In Fig. 72, if $l \parallel m$, $n \parallel p$ and $\angle 1 = 85^\circ$, find $\angle 2$.



Sol:

Given that, $\angle 1 = 85^\circ$

$\angle 1$ and $\angle 3$ are corresponding angles

So, $\angle 1 = \angle 3$

$$\Rightarrow \angle 3 = 85^\circ$$

Sum of the interior angles

$$\Rightarrow \angle 3 + \angle 2 = 180^\circ$$

$$\Rightarrow \angle 2 = 180^\circ - 85^\circ$$

$$\Rightarrow \angle 2 = 95^\circ$$

Q16. In Fig. 73, a transversal n cuts two lines l and m . If $\angle 1 = 70^\circ$ and $\angle 7 = 80^\circ$, is $l \parallel m$?

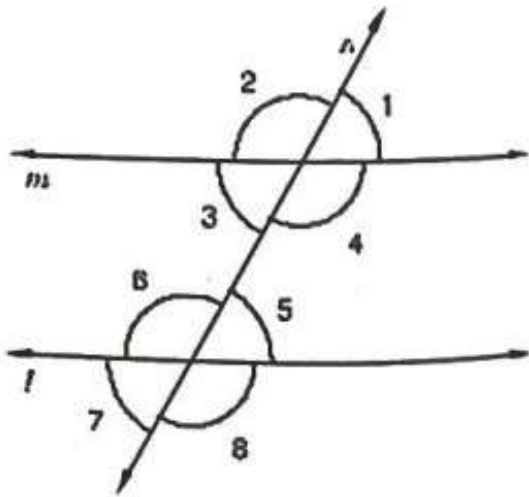


Fig. 73

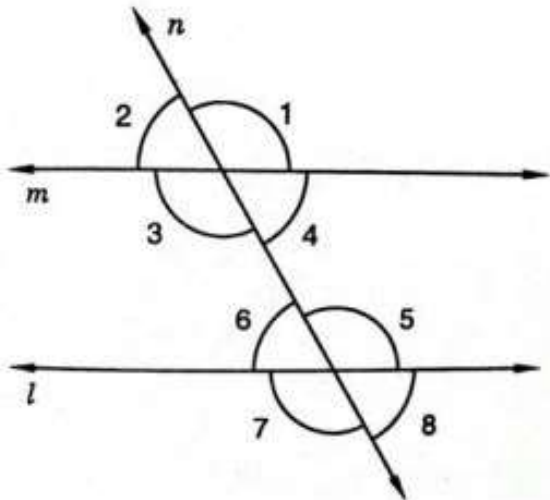
Sol:

We know that if the alternate exterior angles of the two lines are equal, then the lines are parallel.

Here, $\angle 1$ and $\angle 7$ are alternate exterior angles, but they are not equal

$\Rightarrow \angle 1 \neq \angle 7 \neq 80^\circ$

Q17. In Fig. 74, a transversal n cuts two lines l and m such that $\angle 2 = 65^\circ$ and $\angle 8 = 65^\circ$. Are the lines parallel?



Sol:

vertically opposite angles,

$$\angle 2 = \angle 3 = 65^\circ$$

$$\angle 8 = \angle 6 = 65^\circ$$

Therefore, $\angle 3 = \angle 6$

Hence, $l \parallel m$

Q18. In Fig. 75, Show that $AB \parallel EF$.

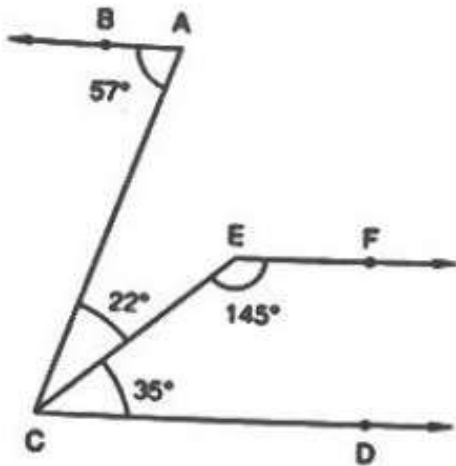


Fig. 75

Sol:

We know that,

$$\angle ACD = \angle ACE + \angle ECD$$

$$\Rightarrow \angle ACD = 35^\circ + 22^\circ$$

$$\Rightarrow \angle ACD = 57^\circ = \angle BAC$$

Thus, lines BA and CD are intersected by the line AC such that, $\angle ACD = \angle BAC$

So, the alternate angles are equal

Therefore, $AB \parallel CD$ ——— 1

Now,

$$\angle ECD + \angle CEF = 35^\circ + 45^\circ = 180^\circ$$

This, shows that sum of the angles of the interior angles on the same side of the transversal CE is 180 degrees

So, they are supplementary angles

Therefore, $EF \parallel CD$ ——— 2

From eq 1 and 2

We can say that, $AB \parallel EF$

Q19. In Fig. 76, $AB \parallel CD$. Find the values of x,y,z.

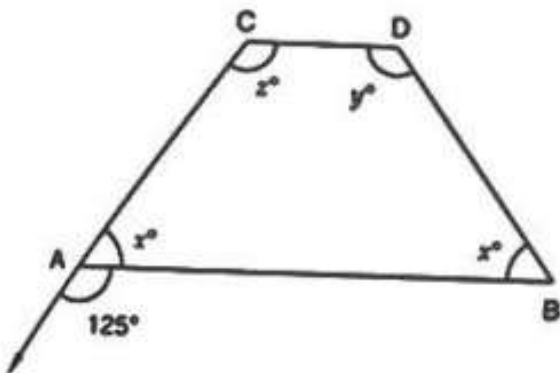


Fig. 76

Sol:

Linear pair,

$$\Rightarrow \angle X + 125^\circ = 180^\circ$$

$$\Rightarrow \angle X = 180^\circ - 125^\circ$$

$$\Rightarrow \angle X = 55^\circ$$

Corresponding angles

$$\Rightarrow \angle Z = 125^\circ$$

Adjacent interior angles

$$\Rightarrow \angle X + \angle Z = 180^\circ$$

$$\Rightarrow \angle X + 125^\circ = 180^\circ$$

$$\Rightarrow \angle X = 180^\circ - 125^\circ$$

$$\Rightarrow \angle X = 55^\circ$$

Adjacent interior angles

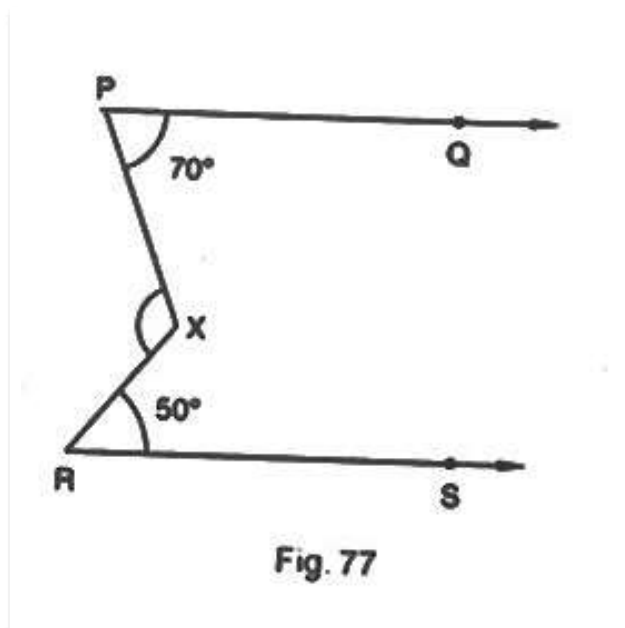
$$\Rightarrow \angle X + \angle y = 180^\circ$$

$$\Rightarrow \angle y + 55^\circ = 180^\circ$$

$$\Rightarrow \angle y = 180^\circ - 55^\circ$$

$$\Rightarrow \angle y = 125^\circ$$

Q20. In Fig. 77, find out $\angle PXR$, if $PQ \parallel RS$.



Sol:

We need to find $\angle PXR$

$$\angle XRS = 50^\circ$$

$$\angle XPR = 70^\circ$$

Given, that $PQ \parallel RS$

$$\angle PXR = \angle XRS + \angle XPR$$

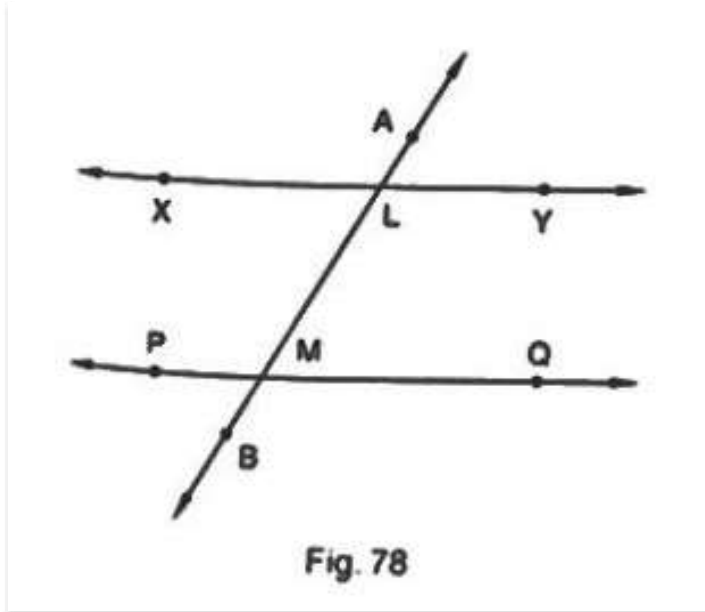
$$\angle PXR = 50^\circ + 70^\circ$$

$$\angle PXR = 120^\circ$$

Therefore, $\angle PXR = 120^\circ$

Q21. In Fig. 78, we have

(i) $\angle MLY = 2\angle LMQ$



Sol:

$\angle MLY$ and $\angle LMQ$ are interior angles

$$\Rightarrow \angle MLY + \angle LMQ = 180^\circ$$

$$\Rightarrow 2\angle LMQ + \angle LMQ = 180^\circ$$

$$\Rightarrow 3\angle LMQ = 180^\circ$$

$$\Rightarrow \angle LMQ = \frac{180^\circ}{3}$$

$$\Rightarrow \angle LMQ = 60^\circ$$

(ii) $\angle XLM = (2x - 10)^\circ$ and $\angle LMQ = (x + 30)^\circ$, find x .

Sol:

$$\angle XLM = (2x - 10)^\circ \text{ and } \angle LMQ = (x + 30)^\circ$$

$\angle XLM$ and $\angle LMQ$ are alternate interior angles

$$\Rightarrow \angle XLM = \angle LMQ$$

$$\Rightarrow (2x - 10)^\circ = (x + 30)^\circ$$

$$\Rightarrow 2x - x = 30^\circ + 10^\circ$$

$$\Rightarrow x = 40^\circ$$

Therefore, $x = 40^\circ$

(iii) $\angle XLM = \angle PML$, find $\angle ALY$

Sol:

$$\angle XLM = \angle PML$$

Sum of interior angles is 180 degrees

$$\Rightarrow \angle XLM + \angle PML = 180^\circ$$

$$\Rightarrow \angle XLM + \angle XLM = 180^\circ$$

$$\Rightarrow 2\angle XLM = 180^\circ$$

$$\Rightarrow \angle XLM = \frac{180^\circ}{2}$$

$$\Rightarrow \angle XLM = 90^\circ$$

$\angle XLM$ and $\angle ALY$ are vertically opposite angles

Therefore, $\angle ALY = 90^\circ$

(iv) $\angle ALY = (2x - 15)^\circ$, $\angle LMQ = (x + 40)^\circ$, find x .

Sol:

$\angle ALY$ and $\angle LMQ$ are corresponding angles

$$\Rightarrow \angle ALY = \angle LMQ$$

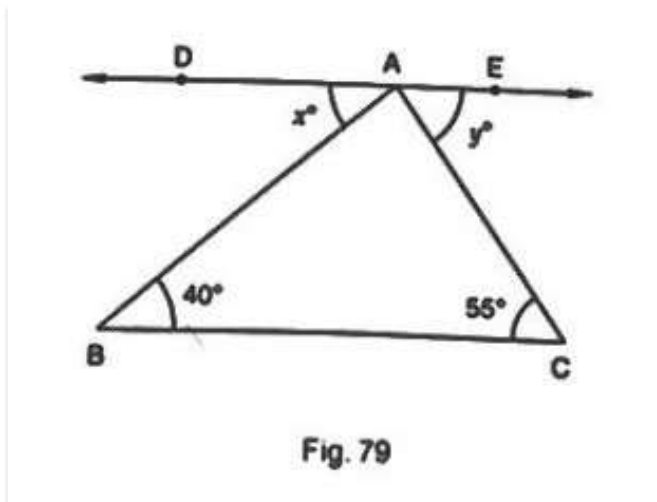
$$\Rightarrow (2x - 15)^\circ = (x + 40)^\circ$$

$$\Rightarrow 2x - x = 40^\circ + 15^\circ$$

$$\Rightarrow x = 55^\circ$$

Therefore, $x = 55^\circ$

Q22. In Fig. 79, $DE \parallel BC$. Find the values of x and y .



Sol:

We know that, $\angle ABC$, $\angle DAB$ are alternate interior angles

$$\angle ABC = \angle DAB$$

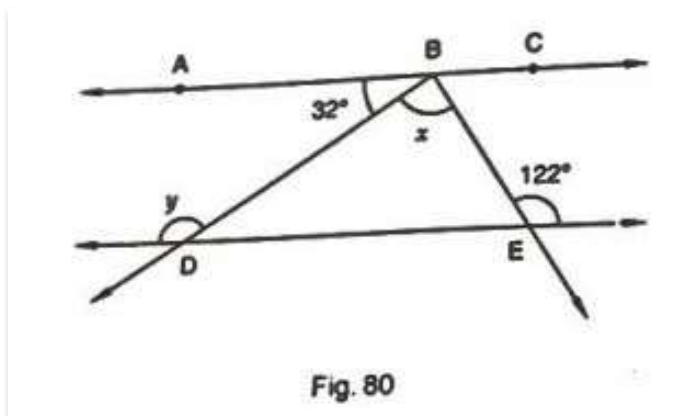
$$\text{So, } x = 40^\circ$$

And $\angle ACB$, $\angle EAC$ are alternate interior angles

$$\angle ACB = \angle EAC$$

$$\text{So, } y = 40^\circ$$

Q23. In Fig. 80, line $AC \parallel$ line DE and $\angle ABD = 32^\circ$, Find out the angles x and y if $\angle E = 122^\circ$.



Sol:

$\angle BDE = \angle ABD = 32^\circ$ – alternate interior angles

$\Rightarrow \angle BDE + y = 180^\circ$ – linear pair

$\Rightarrow 32^\circ + y = 180^\circ$

$\Rightarrow y = 180^\circ - 32^\circ$

$\Rightarrow y = 148^\circ$

$\angle ABE = \angle E = 32^\circ$ – alternate interior angles

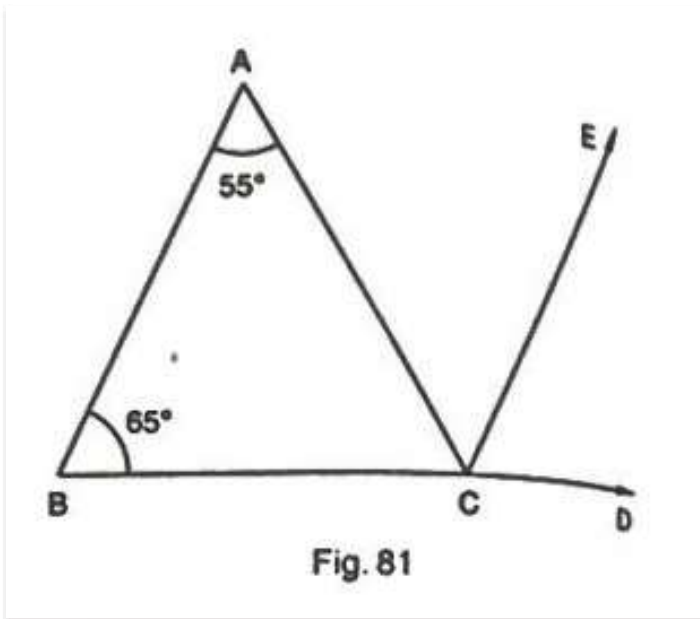
$\Rightarrow \angle ABD + \angle DBE = 122^\circ$

$\Rightarrow 32^\circ + x = 122^\circ$

$\Rightarrow x = 122^\circ - 32^\circ$

$\Rightarrow x = 90^\circ$

Q24. In Fig. 81, side BC of $\triangle ABC$ has been produced to D and $CE \parallel BA$. If $\angle ABC = 65^\circ$, $\angle BAC = 55^\circ$, find $\angle ACE$, $\angle ECD$, $\angle ACD$.



Sol:

Corresponding angles,

$\angle ABC = \angle ECD = 65^\circ$

Alternate interior angles,

$\angle BAC = \angle ACE = 55^\circ$

Now, $\angle ACD = \angle ACE + \angle ECD$

$\Rightarrow \angle ACD = 55^\circ + 65^\circ$

$= 120^\circ$

Q25. In Fig. 82, line $CA \perp AB$ \parallel line CR and line PR \parallel line BD. Find $\angle x$, $\angle y$, $\angle z$.

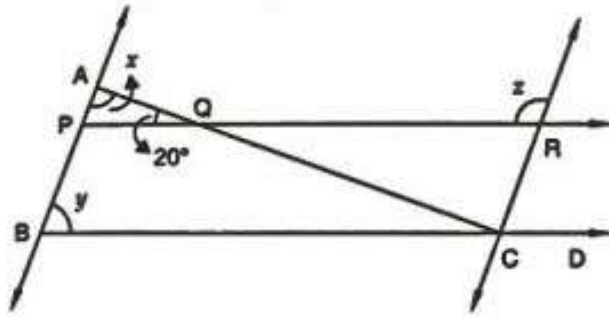


Fig. 82

Sol:

Given that, $CA \perp AB$

$$\Rightarrow \angle CAB = 90^\circ$$

$$\Rightarrow \angle AQP = 20^\circ$$

By, angle of sum property

In $\triangle APQ$

$$\Rightarrow \angle CAB + \angle AQP + \angle APQ = 180^\circ$$

$$\Rightarrow \angle APQ = 180^\circ - 90^\circ - 20^\circ$$

$$\Rightarrow \angle APQ = 70^\circ$$

y and $\angle APQ$ are corresponding angles

$$\Rightarrow y = \angle APQ = 70^\circ$$

$\angle APQ$ and $\angle z$ are interior angles

$$\Rightarrow \angle APQ + \angle z = 180^\circ$$

$$\Rightarrow \angle z = 180^\circ - 70^\circ$$

$$\Rightarrow \angle z = 110^\circ$$

Q26. In Fig. 83, $PQ \parallel RS$. Find the value of x .

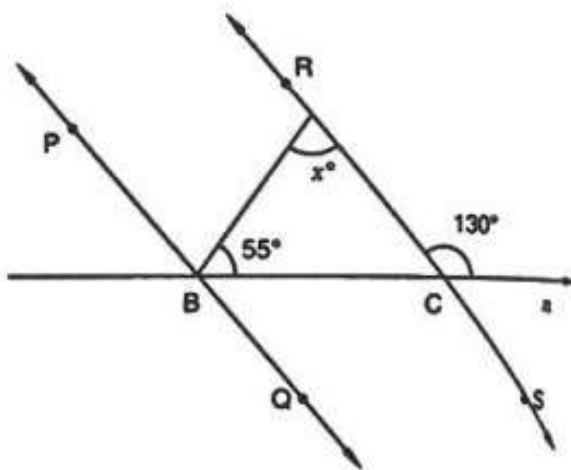


Fig. 83

Sol:

Given,

Linear pair,

$$\angle RCD + \angle RCB = 180^\circ$$

$$\Rightarrow \angle RCB = 180^\circ - 130^\circ$$

$$= 50^\circ$$

In $\triangle ABC$,

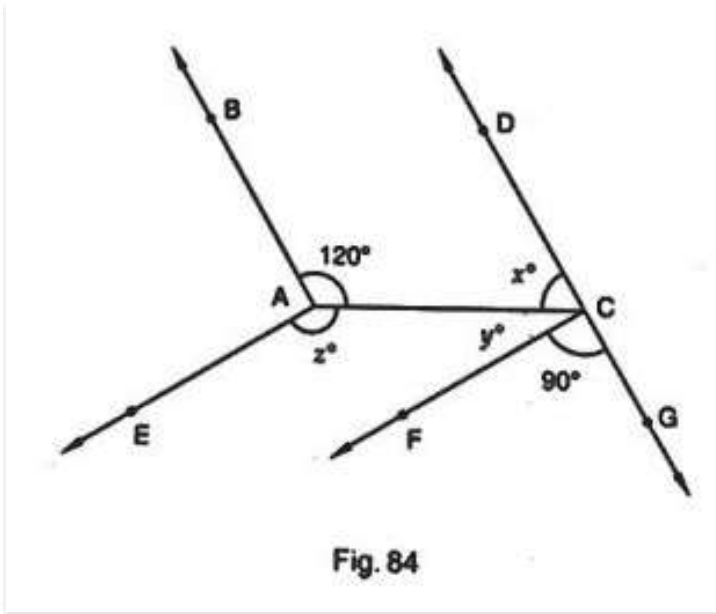
$$\angle BAC + \angle ABC + \angle BCA = 180^\circ$$

By, angle sum property

$$\Rightarrow \angle BAC = 180^\circ - 55^\circ - 50^\circ$$

$$\Rightarrow \angle BAC = 75^\circ$$

Q27. In Fig. 84, $AB \parallel CD$ and $AE \parallel CF$, $\angle FCG = 90^\circ$ and $\angle BAC = 120^\circ$. Find the value of x , y and z .



Sol:

Alternate interior angle

$$\angle BAC = \angle ACG = 120^\circ$$

$$\Rightarrow \angle ACF + \angle FCG = 120^\circ$$

$$\text{So, } \angle ACF = 120^\circ - 90^\circ$$

$$= 30^\circ$$

Linear pair,

$$\angle DCA + \angle ACG = 180^\circ$$

$$\Rightarrow \angle x = 180^\circ - 120^\circ$$

$$= 60^\circ$$

$$\angle BAC + \angle BAE + \angle EAC = 360^\circ$$

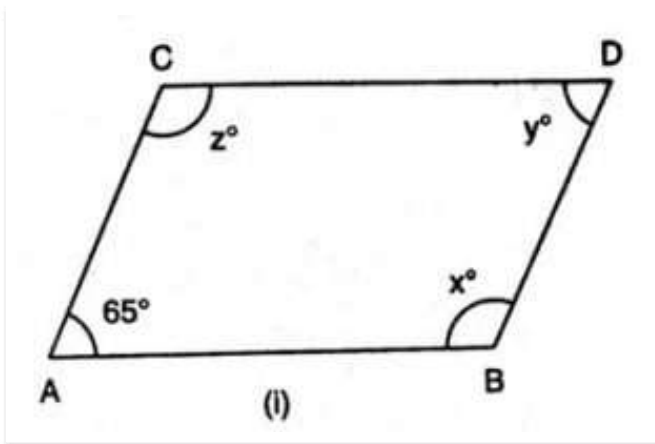
$$\angle CAE = 360^\circ - 120^\circ - (60^\circ + 30^\circ)$$

$$= 150^\circ$$

Q28. In Fig. 85, $AB \parallel CD$ and $AC \parallel BD$. Find the values of x, y, z .

Sol:

(i)



Since, $AC \parallel BD$ and $CD \parallel AB$, ABCD is a parallelogram

Adjacent angles of parallelogram,

$$\angle CAD + \angle ACD = 180^\circ$$

$$\Rightarrow \angle ACD = 180^\circ - 65^\circ$$

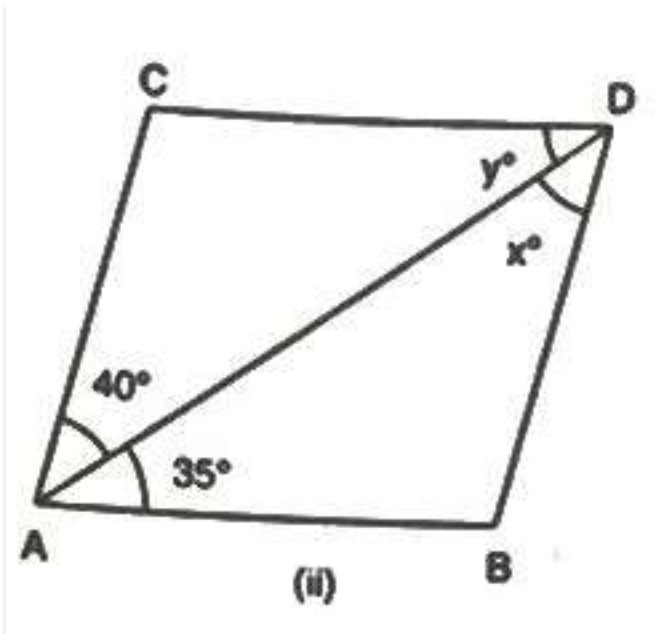
$$= 115^\circ$$

Opposite angles of parallelogram,

$$\Rightarrow \angle CAD = \angle CDB = 65^\circ$$

$$\Rightarrow \angle ACD = \angle DBA = 115^\circ$$

(ii)



here,

$AC \parallel BD$ and $CD \parallel AB$

Alternate interior angles,

$$\angle DCA = x = 40^\circ$$

$$\angle DAB = y = 35^\circ$$

Q29. In Fig. 86, state which lines are parallel and why?

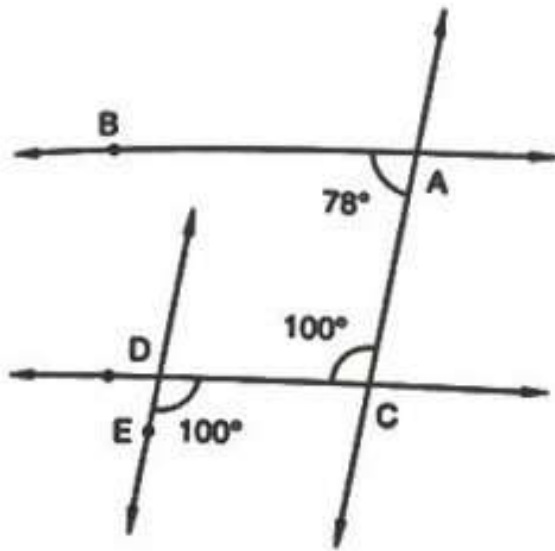


Fig. 86

Sol:

Let, F be the point of intersection of the line CD and the line passing through point E.

Here, $\angle ACD$ and $\angle CDE$ are alternate and equal angles.

So, $\angle ACD = \angle CDE = 100^\circ$

Therefore, $AC \parallel EF$

Q30. In Fig. 87, the corresponding arms of $\angle ABC$ and $\angle DEF$ are parallel. If $\angle ABC = 75^\circ$, find $\angle DEF$.

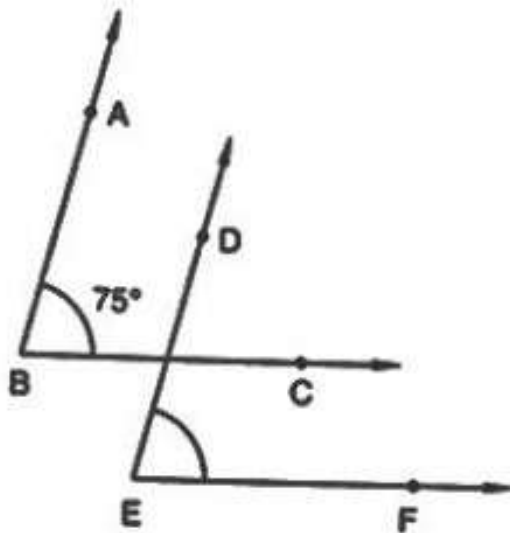


Fig. 87

Sol:

Let, G be the point of intersection of the lines BC and DE

Since, $AB \parallel DE$ and $BC \parallel EF$

The corresponding angles,

$$\Rightarrow \angle ABC = \angle DGC = \angle DEF = 100^\circ$$