

**RD SHARMA**

**Solutions**

**Class 7 Maths**

**Chapter 15**

**Ex 15.2**

**Q1. Two angles of a triangle are of measures  $150^\circ$  and  $30^\circ$ . Find the measure of the third angle.**

Let the third angle be  $x$

Sum of all the angles of a triangle =  $180^\circ$

$$105^\circ + 30^\circ + x = 180^\circ$$

$$135^\circ + x = 180^\circ$$

$$x = 180^\circ - 135^\circ$$

$$x = 45^\circ$$

Therefore the third angle is  $45^\circ$

**Q2. One of the angles of a triangle is  $130^\circ$ , and the other two angles are equal. What is the measure of each of these equal angles?**

Let the second and third angle be  $x$

Sum of all the angles of a triangle =  $180^\circ$

$$130^\circ + x + x = 180^\circ$$

$$130^\circ + 2x = 180^\circ$$

$$2x = 180^\circ - 130^\circ$$

$$2x = 50^\circ$$

$$x = \frac{50}{2}$$

$$x = 25^\circ$$

Therefore the two other angles are  $25^\circ$  each

**Q3. The three angles of a triangle are equal to one another. What is the measure of each of the angles?**

Let the each angle be  $x$

Sum of all the angles of a triangle =  $180^\circ$

$$x + x + x = 180^\circ$$

$$3x = 180^\circ$$

$$x = \frac{180}{3}$$

$$x = 60^\circ$$

Therefore angle is  $60^\circ$  each

**Q4. If the angles of a triangle are in the ratio 1 : 2 : 3, determine three angles.**

If angles of the triangle are in the ratio 1:2:3 then take first angle as 'x', second angle as '2x' and third angle as '3x'

Sum of all the angles of a triangle =  $180^\circ$

$$x + 2x + 3x = 180^\circ$$

$$6x = 180^\circ$$

$$x = \frac{180}{6}$$

$$x = 30^\circ$$

$$2x = 30^\circ \times 2 = 60^\circ$$

$$3x = 30^\circ \times 3 = 90^\circ$$

Therefore the first angle is  $30^\circ$ , second angle is  $60^\circ$  and third angle is  $90^\circ$

**Q5. The angles of a triangle are  $(x - 40)^\circ$ ,  $(x - 20)^\circ$  and  $(\frac{x}{2} - 10)^\circ$ . Find the value of x.**

Sum of all the angles of a triangle =  $180^\circ$

$$(x - 40)^\circ + (x - 20)^\circ + (\frac{x}{2} - 10)^\circ = 180^\circ$$

$$x + x + \frac{x}{2} - 40^\circ - 20^\circ - 10^\circ = 180^\circ$$

$$x + x + \frac{x}{2} - 70^\circ = 180^\circ$$

$$x + x + \frac{x}{2} = 180^\circ + 70^\circ$$

$$\frac{5x}{2} = 250^\circ$$

$$x = \frac{2}{5} \times 250^\circ$$

$$x = 100^\circ$$

Hence we can conclude that x is equal to  $100^\circ$

**Q6. The angles of a triangle are arranged in ascending order of magnitude. If the difference between two consecutive angles is  $10^\circ$ . Find the three angles.**

Let the first angle be x

Second angle be  $x + 10^\circ$

Third angle be  $x + 10^\circ + 10^\circ$

Sum of all the angles of a triangle =  $180^\circ$

$$x + x + 10^\circ + x + 10^\circ + 10^\circ = 180^\circ$$

$$3x+30=180$$

$$3x=180-30$$

$$3x=150$$

$$x=\frac{150}{3}$$

$$x=50^\circ$$

First angle is 50

$$\text{Second angle } x+10^\circ=50+10=60^\circ$$

$$\text{Third angle } x+10^\circ+10^\circ=50+10+10=70^\circ$$

***Q7. Two angles of a triangle are equal and the third angle is greater than each of those angles by  $30^\circ$ . Determine all the angles of the triangle***

Let the first and second angle be  $x$

The third angle is greater than the first and second by  $30^\circ = x+30^\circ$

The first and the second angles are equal

Sum of all the angles of a triangle =  $180^\circ$

$$x+x+x+30^\circ = 180^\circ$$

$$3x+30=180$$

$$3x=180-30$$

$$3x=150$$

$$x=\frac{150}{3}$$

$$x=50^\circ$$

$$\text{Third angle} = x+30^\circ = 50^\circ + 30^\circ = 80^\circ$$

The first and the second angle is  $50^\circ$  and the third angle is  $80^\circ$

***Q8. If one angle of a triangle is equal to the sum of the other two, show that the triangle is a right triangle.***

One angle of a triangle is equal to the sum of the other two

$$x=y+z$$

Let the measure of angles be  $x, y, z$

$$x+y+z=180^\circ$$

$$x+x=180^\circ$$

$$2x=180^\circ$$

$$x = \frac{180^\circ}{2}$$

$$x = 90^\circ$$

If one angle is  $90^\circ$  then the given triangle is a right angled triangle

**Q9. If each angle of a triangle is less than the sum of the other two, show that the triangle is acute angled.**

Each angle of a triangle is less than the sum of the other two

Measure of angles be  $x, y$  and  $z$

$$x > y + z$$

$$y < x + z$$

$$z < x + y$$

Therefore triangle is an acute triangle

**Q10. In each of the following, the measures of three angles are given. State in which cases the angles can possibly be those of a triangle:**

(i)  $63^\circ, 37^\circ, 80^\circ$

(ii)  $45^\circ, 61^\circ, 73^\circ$

(iii)  $59^\circ, 72^\circ, 61^\circ$

(iv)  $45^\circ, 45^\circ, 90^\circ$

(v)  $30^\circ, 20^\circ, 125^\circ$

(i)  $63^\circ, 37^\circ, 80^\circ = 180^\circ$

Angles form a triangle

(ii)  $45^\circ, 61^\circ, 73^\circ$  is not equal to  $180^\circ$

Therefore not a triangle

(iii)  $59^\circ, 72^\circ, 61^\circ$  is not equal to  $180^\circ$

Therefore not a triangle

(iv)  $45^\circ, 45^\circ, 90^\circ = 180$

Angles form a triangle

(v)  $30^\circ, 20^\circ, 125^\circ$  is not equal to  $180^\circ$

Therefore not a triangle

**Q11. The angles of a triangle are in the ratio 3: 4 : 5. Find the smallest angle**

Given that

Angles of a triangle are in the ratio: 3: 4: 5

Measure of the angles be  $3x$ ,  $4x$ ,  $5x$

Sum of the angles of a triangle =  $180^\circ$

$$3x + 4x + 5x = 180^\circ$$

$$12x = 180^\circ$$

$$x = \frac{180^\circ}{12}$$

$$x = 15^\circ$$

Smallest angle =  $3x$

$$= 3 \times 15^\circ$$

$$= 45^\circ$$

**Q12. Two acute angles of a right triangle are equal. Find the two angles.**

Given acute angles of a right angled triangle are equal

Right triangle: whose one of the angle is a right angle

Measured angle be  $x, x, 90^\circ$

$$x + x + 90^\circ = 180^\circ$$

$$2x = 90^\circ$$

$$x = \frac{90^\circ}{2}$$

$$x = 45^\circ$$

The two angles are  $45^\circ$  and  $45^\circ$

**Q13. One angle of a triangle is greater than the sum of the other two. What can you say about the measure of this angle? What type of a triangle is this?**

Angle of a triangle is greater than the sum of the other two

Measure of the angles be  $x, y, z$

$$x > y + z \quad \text{or}$$

$y > x + z$  or

$z > x + y$

$x$  or  $y$  or  $z > 90^\circ$  which is obtuse

Therefore triangle is an obtuse angle

**Q14. AC, AD and AE are joined. Find  $\angle FAB + \angle ABC + \angle BCD + \angle CDE + \angle DEF + \angle EFA$**

$\angle FAB + \angle ABC + \angle BCD + \angle CDE + \angle DEF + \angle EFA$

We know that sum of the angles of a triangle is  $180^\circ$

Therefore in  $\triangle ABC$ , we have

$$\angle CAB + \angle ABC + \angle BCA = 180^\circ \text{---(i)}$$

In  $\triangle ACD$ , we have

$$\angle DAC + \angle ACD + \angle CDA = 180^\circ \text{---(ii)}$$

In  $\triangle ADE$ , we have

$$\angle EAD + \angle ADE + \angle DEA = 180^\circ \text{---(iii)}$$

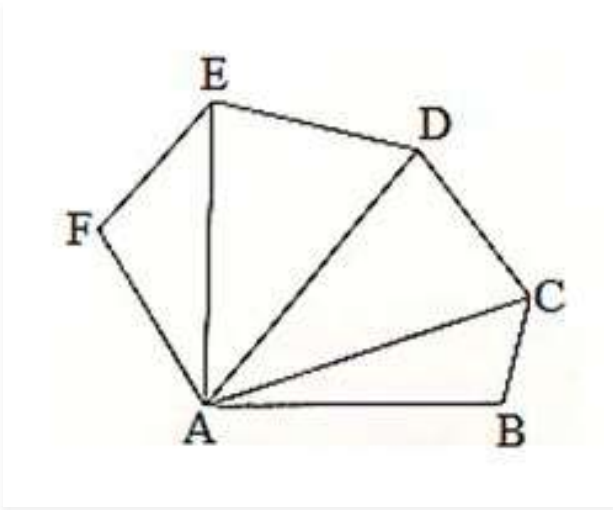
In  $\triangle AEF$ , we have

$$\angle FAE + \angle AEF + \angle EFA = 180^\circ \text{---(iv)}$$

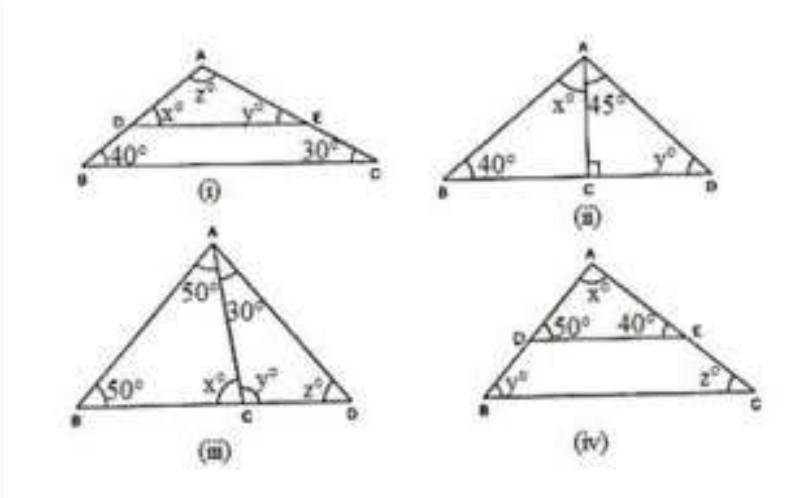
Adding (i),(ii),(iii),(iv) we get

$$\begin{aligned} & \angle CAB + \angle ABC + \angle BCA + \angle DAC + \angle ACD + \angle CDA + \angle EAD + \angle ADE + \angle DEA \\ & + \angle FAE + \angle AEF + \angle EFA \\ & = 720^\circ \end{aligned}$$

Therefore  $\angle FAB + \angle ABC + \angle BCD + \angle CDE + \angle DEF + \angle EFA = 720^\circ$



**Q15. Find  $x, y, z$  (whichever is required) from the figures given below**



(i)

In  $\triangle ABC$  and  $\triangle ADE$  we have :

$\angle ADE = \angle ABC$  (corresponding angles)

$$x = 40^\circ$$

$\angle AED = \angle ACB$  (corresponding angles)

$$y = 30^\circ$$

We know that the sum of all the three angles of a triangle is equal to  $180^\circ$

$$x + y + z = 180^\circ \text{ (Angles of } \triangle ADE)$$

$$\text{Which means : } 40^\circ + 30^\circ + z = 180^\circ$$

$$z = 180^\circ - 70^\circ$$

$$z = 110^\circ$$

Therefore, we can conclude that the three angles of the given triangle are  $40^\circ, 30^\circ$  and  $110^\circ$ .



(ii) We can see that in  $\triangle ADC$ ,  $\angle ADC$  is equal to  $90^\circ$ .

( $\triangle ADC$  is a right triangle)

We also know that the sum of all the angles of a triangle is equal to  $180^\circ$ .

Which means :  $45^\circ + 90^\circ + y = 180^\circ$  (Sum of the angles of  $\triangle ADC$  )

$$135^\circ + y = 180^\circ$$

$$y = 180^\circ - 135^\circ.$$

$$y = 45^\circ.$$

We can also say that in  $\triangle ABC$ ,  $\angle ABC + \angle ACB + \angle BAC$  is equal to  $180^\circ$ .

(Sum of the angles of  $\triangle ABC$ )

$$40^\circ + y + (x + 45^\circ) = 180^\circ$$

$$40^\circ + 45^\circ + x + 45^\circ = 180^\circ \quad (y = 45^\circ)$$

$$x = 180^\circ - 130^\circ$$

$$x = 50^\circ$$

Therefore, we can say that the required angles are  $45^\circ$  and  $50^\circ$ .

(iii) We know that the sum of all the angles of a triangle is equal to  $180^\circ$ .

Therefore, for  $\triangle ABD$ :

$$\angle ABD + \angle ADB + \angle BAD = 180^\circ \text{ (Sum of the angles of } \triangle ABD)$$

$$50^\circ + x + 50^\circ = 180^\circ$$

$$100^\circ + x = 180^\circ$$

$$x = 180^\circ - 100^\circ$$

$$x = 80^\circ$$

For  $\triangle ABC$ :

$$\angle ABC + \angle ACB + \angle BAC = 180^\circ \text{ (Sum of the angles of } \triangle ABC)$$

$$50^\circ + z + (50^\circ + 30^\circ) = 180^\circ$$

$$50^\circ + z + 50^\circ + 30^\circ = 180^\circ$$

$$z = 180^\circ - 130^\circ$$

$$z = 50^\circ$$

Using the same argument for  $\triangle ADC$ :

$$\angle ADC + \angle ACD + \angle DAC = 180^\circ \text{ (Sum of the angles of } \triangle ADC)$$

$$y + z + 30^\circ = 180^\circ$$

$$y + 50^\circ + 30^\circ = 180^\circ \quad (z = 50^\circ)$$

$$y = 180^\circ - 80^\circ$$

$$y = 100^\circ$$

Therefore, we can conclude that the required angles are  $80^\circ$ ,  $50^\circ$  and  $100^\circ$ .

(iv) In  $\triangle ABC$  and  $\triangle ADE$  we have :

$$\angle ADE = \angle ABC \text{ (Corresponding angles)}$$

$$y = 50^\circ$$

$$\text{Also, } \angle AED = \angle ACB \text{ (Corresponding angles)}$$

$$z = 40^\circ$$

We know that the sum of all the three angles of a triangle is equal to  $180^\circ$ .

$$\text{Which means : } x + 50^\circ + 40^\circ = 180^\circ \text{ (Angles of } \triangle ADE)$$

$$x = 180^\circ - 90^\circ$$

$$x = 90^\circ$$

Therefore, we can conclude that the required angles are  $50^\circ$ ,  $40^\circ$  and  $90^\circ$ .

**Q16. If one angle of a triangle is  $60^\circ$  and the other two angles are in the ratio 1 : 2, find the angles**

We know that one of the angles of the given triangle is  $60^\circ$ . (Given)

We also know that the other two angles of the triangle are in the ratio 1 : 2.

Let one of the other two angles be  $x$ .

Therefore, the second one will be  $2x$ .

We know that the sum of all the three angles of a triangle is equal to  $180^\circ$ .

$$60^\circ + x + 2x = 180^\circ$$

$$3x = 180^\circ - 60^\circ$$

$$3x = 120^\circ$$

$$x = \frac{120^\circ}{3}$$

$$x = 40^\circ$$

$$2x = 2 \times 40$$

$$2x = 80^\circ$$

Hence, we can conclude that the required angles are  $40^\circ$  and  $80^\circ$ .

**Q17. If one angle of a triangle is  $100^\circ$  and the other two angles are in the ratio 2 : 3. find the angles.**

We know that one of the angles of the given triangle is  $100^\circ$ .

We also know that the other two angles are in the ratio 2 : 3.

Let one of the other two angles be  $2x$ .

Therefore, the second angle will be  $3x$ .

We know that the sum of all three angles of a triangle is  $180^\circ$ .

$$100^\circ + 2x + 3x = 180^\circ$$

$$5x = 180^\circ - 100^\circ$$

$$5x = 80^\circ$$

$$x = \frac{80^\circ}{5}$$

$$2x = 2 \times 16$$

$$2x = 32^\circ$$

$$3x = 3 \times 16$$

$$3x = 48^\circ$$

Thus, the required angles are  $32^\circ$  and  $48^\circ$ .

**Q18. In  $\triangle ABC$ , if  $3\angle A = 4\angle B = 6\angle C$ , calculate the angles.**

We know that for the given triangle,  $3\angle A = 6\angle C$

$$\angle A = 2\angle C \text{---(i)}$$

We also know that for the same triangle,  $4\angle B = 6\angle C$

$$\angle B = \frac{6}{4}\angle C \text{---(ii)}$$

We know that the sum of all three angles of a triangle is  $180^\circ$ .

Therefore, we can say that:

$$\angle A + \angle B + \angle C = 180^\circ \text{ (Angles of } \triangle ABC) \text{---(iii)}$$

On putting the values of  $\angle A$  and  $\angle B$  in equation (iii), we get :

$$2\angle C + \frac{6}{4}\angle C + \angle C = 180^\circ \quad \frac{18}{4}\angle C = 180^\circ \quad \angle C = 40^\circ$$

From equation (i), we have:

$$\angle A = 2\angle C = 2 \times 40 \quad \angle A = 80^\circ$$

From equation (ii), we have:

$$\angle B = \frac{6}{4}\angle C = \frac{6}{4} \times 40^\circ \quad \angle B = 60^\circ$$

$$\angle A = 80^\circ, \angle B = 60^\circ, \angle C = 40^\circ$$

Therefore, the three angles of the given triangle are  $80^\circ$ ,  $60^\circ$ , and  $40^\circ$ .

**Q19. Is it possible to have a triangle, in which**

**(i) Two of the angles are right?**

**(ii) Two of the angles are obtuse?**

**(iii) Two of the angles are acute?**

**(iv) Each angle is less than  $60^\circ$ ?**

**(v) Each angle is greater than  $60^\circ$ ?**

**(vi) Each angle is equal to  $60^\circ$**

**Give reasons in support of your answer in each case.**

(i) No, because if there are two right angles in a triangle, then the third angle of the triangle must be zero, which is not possible.

(ii) No, because as we know that the sum of all three angles of a triangle is always  $180^\circ$ . If there are two obtuse angles, then their sum will be more than  $180^\circ$ , which is not possible in case of a triangle.

(iii) Yes, in right triangles and acute triangles, it is possible to have two acute angles.

(iv) No, because if each angle is less than  $60^\circ$ , then the sum of all three angles will be less than  $180^\circ$ , which is not possible in case of a triangle.

Proof:

Let the three angles of the triangle be  $\angle A$ ,  $\angle B$  and  $\angle C$ .

As per the given information,

$$\angle A < 60^\circ \dots (i)$$

$$\angle B < 60^\circ \dots (ii)$$

$$\angle C < 60^\circ \dots (iii)$$

On adding (i), (ii) and (iii), we get :

$$\angle A + \angle B + \angle C < 60^\circ + 60^\circ + 60^\circ$$

$$\angle A + \angle B + \angle C < 180^\circ$$

We can see that the sum of all three angles is less than  $180^\circ$ , which is not possible for a triangle.

Hence, we can say that it is not possible for each angle of a triangle to be less than  $60^\circ$ .

(v) No, because if each angle is greater than  $60^\circ$ , then the sum of all three angles will be greater than  $180^\circ$ , which is not possible.

Proof:

Let the three angles of the triangle be  $\angle A$ ,  $\angle B$  and  $\angle C$ . As per the given information,

$$\angle A > 60^\circ \dots (i)$$

$$\angle B > 60^\circ \dots (ii)$$

$$\angle C > 60^\circ \dots (iii)$$

On adding (i), (ii) and (iii), we get:

$$\angle A + \angle B + \angle C > 60^\circ + 60^\circ + 60^\circ$$

$$\angle A + \angle B + \angle C > 180^\circ$$

We can see that the sum of all three angles of the given triangle are greater than  $180^\circ$ , which is not possible for a triangle.

Hence, we can say that it is not possible for each angle of a triangle to be greater than  $60^\circ$ .

(vi) Yes, if each angle of the triangle is equal to  $60^\circ$ , then the sum of all three angles will be  $180^\circ$ , which is possible in case of a triangle.

Proof:

Let the three angles of the triangle be  $\angle A$ ,  $\angle B$  and  $\angle C$ . As per the given information,

$$\angle A = 60^\circ \dots (i)$$

$$\angle B = 60^\circ \dots (ii)$$

$$\angle C = 60^\circ \dots (iii)$$

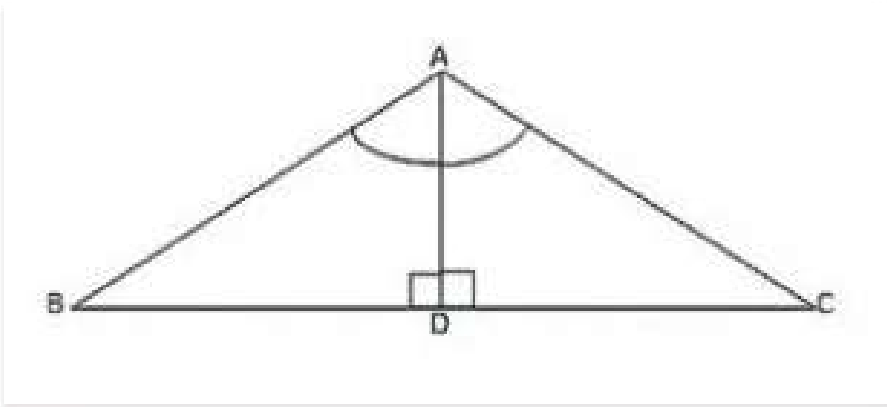
On adding (i), (ii) and (iii), we get:

$$\angle A + \angle B + \angle C = 60^\circ + 60^\circ + 60^\circ$$

$$\angle A + \angle B + \angle C = 180^\circ$$

We can see that the sum of all three angles of the given triangle is equal to  $180^\circ$ , which is possible in case of a triangle. Hence, we can say that it is possible for each angle of a triangle to be equal to  $60^\circ$ .

**Q20.** In  $\triangle ABC$ ,  $\angle A = 100^\circ$ ,  $AD$  bisects  $\angle A$  and  $AD$  perpendicular  $BC$ . Find  $\angle B$



Consider  $\triangle ABD$

$$\angle BAD = \frac{100}{2} \quad (\text{AD bisects } \angle A)$$

$$\angle BAD = 50^\circ$$

$$\angle ADB = 90^\circ \quad (\text{AD perpendicular to BC})$$

We know that the sum of all three angles of a triangle is  $180^\circ$ .

Thus,

$$\angle ABD + \angle BAD + \angle ADB = 180^\circ \quad (\text{Sum of angles of } \triangle ABD)$$

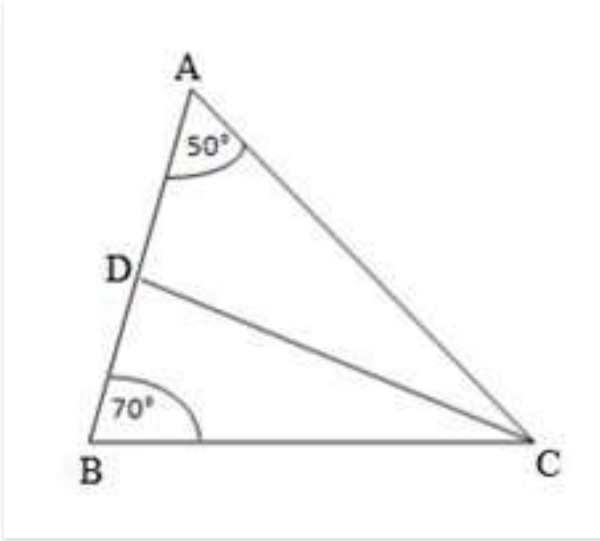
Or,

$$\angle ABD + 50^\circ + 90^\circ = 180^\circ$$

$$\angle ABD = 180^\circ - 140^\circ$$

$$\angle ABD = 40^\circ$$

**Q21.** In  $\triangle ABC$ ,  $\angle A = 50^\circ$ ,  $\angle B = 100^\circ$  and bisector of  $\angle C$  meets  $AB$  in  $D$ . Find the angles of the triangles  $ADC$  and  $BDC$



We know that the sum of all three angles of a triangle is equal to  $180^\circ$ .

Therefore, for the given  $\triangle ABC$ , we can say that :

$$\angle A + \angle B + \angle C = 180^\circ \text{ (Sum of angles of } \triangle ABC)$$

$$50^\circ + 70^\circ + \angle C = 180^\circ$$

$$\angle C = 180^\circ - 120^\circ$$

$$\angle C = 60^\circ$$

$$\angle ACD = \angle BCD = \frac{\angle C}{2} \text{ (CD bisects } \angle C \text{ and meets AB in D.)}$$

$$\angle ACD = \angle BCD = \frac{60^\circ}{2} = 30^\circ$$

Using the same logic for the given  $\triangle ACD$ , we can say that :

$$\angle DAC + \angle ACD + \angle ADC = 180^\circ$$

$$50^\circ + 30^\circ + \angle ADC = 180^\circ$$

$$\angle ADC = 180^\circ - 80^\circ$$

$$\angle ADC = 100^\circ$$

If we use the same logic for the given  $\triangle BCD$ , we can say that

$$\angle DBC + \angle BCD + \angle BDC = 180^\circ$$

$$70^\circ + 30^\circ + \angle BDC = 180^\circ$$

$$\angle BDC = 180^\circ - 100^\circ$$

$$\angle BDC = 80^\circ$$

Thus,

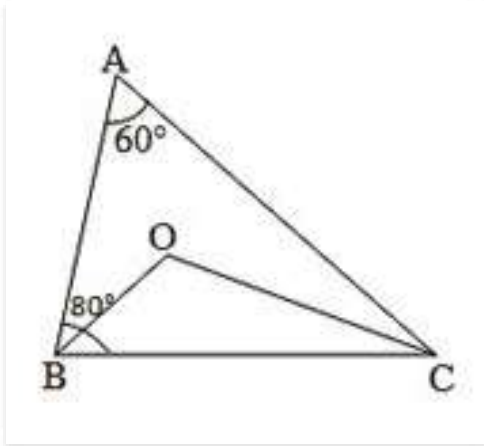
$$\text{For } \triangle ADC: \angle A = 50^\circ, \angle D = 100^\circ, \angle C = 30^\circ$$

$$\triangle BDC: \angle B = 70^\circ, \angle D = 80^\circ, \angle C = 30^\circ$$

**Q22.** In  $\triangle ABC$ ,  $\angle A = 60^\circ$ ,  $\angle B = 80^\circ$ , and the bisectors of  $\angle B$  and  $\angle C$ , meet at  $O$ . Find

(i)  $\angle C$

(ii)  $\angle BOC$



We know that the sum of all three angles of a triangle is  $180^\circ$ .

Hence, for  $\triangle ABC$ , we can say that :

$$\angle A + \angle B + \angle C = 180^\circ \text{ (Sum of angles of } \triangle ABC)$$

$$60^\circ + 80^\circ + \angle C = 180^\circ.$$

$$\angle C = 180^\circ - 140^\circ$$

$$\angle C = 40^\circ.$$

For  $\triangle OBC$ ,

$$\angle OBC = \frac{\angle B}{2} = \frac{80^\circ}{2} \text{ (OB bisects } \angle B)$$

$$\angle OBC = 40^\circ$$

$$\angle OCB = \frac{\angle C}{2} = \frac{40^\circ}{2} \text{ (OC bisects } \angle C)$$

$$\angle OCB = 20^\circ$$

If we apply the above logic to this triangle, we can say that :

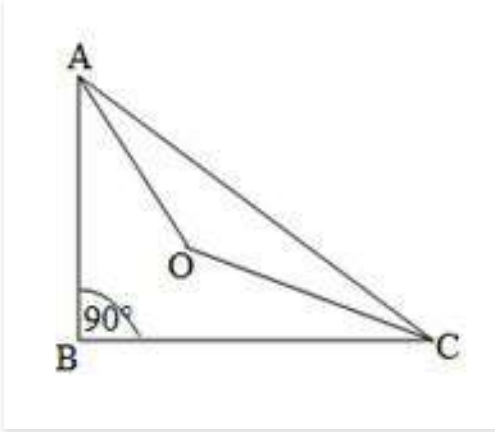
$$\angle OCB + \angle OBC + \angle BOC = 180^\circ \text{ (Sum of angles of } \triangle OBC)$$

$$20^\circ + 40^\circ + \angle BOC = 180^\circ$$

$$\angle BOC = 180^\circ - 60^\circ$$

$$\angle BOC = 120^\circ$$

**Q23. The bisectors of the acute angles of a right triangle meet at O. Find the angle at O between the two bisectors.**



We know that the sum of all three angles of a triangle is  $180^\circ$ .

Hence, for  $\triangle ABC$ , we can say that :

$$\angle A + \angle B + \angle C = 180^\circ$$

$$\angle A + 90^\circ + \angle C = 180^\circ$$

$$\angle A + \angle C = 180^\circ - 90^\circ$$

$$\angle A + \angle C = 90^\circ$$

For  $\triangle OAC$  :

$$\angle OAC = \frac{\angle A}{2} \quad (\text{OA bisects LA})$$

$$\angle OCA = \frac{\angle C}{2} \quad (\text{OC bisects LC})$$

On applying the above logic to  $\triangle OAC$ , we get :

$$\angle AOC + \angle OAC + \angle OCA = 180^\circ \quad (\text{Sum of angles of } \triangle AOC)$$

$$\angle AOC + \frac{\angle A}{2} + \frac{\angle C}{2} = 180^\circ$$

$$\angle AOC + \frac{\angle A + \angle C}{2} = 180^\circ$$

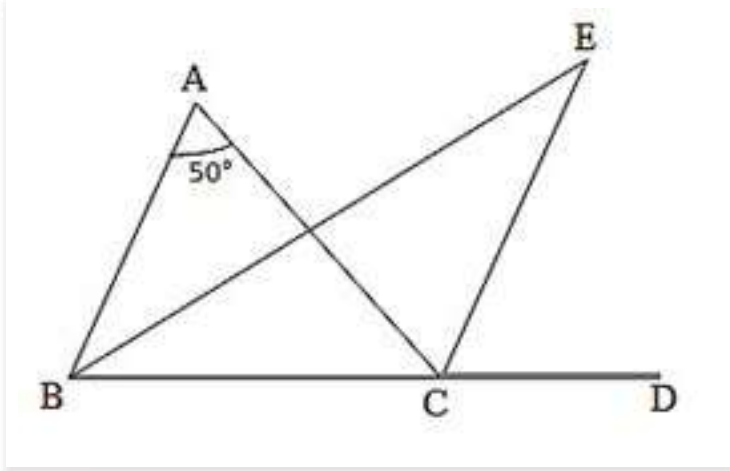
$$\angle AOC + \frac{90^\circ}{2} = 180^\circ$$

$$\angle AOC = 180^\circ - 45^\circ$$

$$\angle AOC = 135^\circ$$



**Q24.** In  $\triangle ABC$ ,  $\angle A = 50^\circ$  and  $BC$  is produced to a point  $D$ . The bisectors of  $\angle ABC$  and  $\angle ACD$  meet at  $E$ . Find  $\angle E$ .



In the given triangle,

$\angle ACD = \angle A + \angle B$  . (Exterior angle is equal to the sum of two opposite interior angles.)

We know that the sum of all three angles of a triangle is  $180^\circ$  .

Therefore, for the given triangle, we can say that :

$$\angle ABC + \angle BCA + \angle CAB = 180^\circ \text{ (Sum of all angles of } \triangle ABC \text{ )}$$

$$\angle A + \angle B + \angle BCA = 180^\circ$$

$$\angle BCA = 180^\circ - (\angle A + \angle B)$$

$$\angle ECA = \frac{\angle ACD}{2} \quad (\text{EC bisects } \angle ACD)$$

$$\angle ECA = \frac{\angle A + \angle B}{2} \quad (\angle ACD = \angle A + \angle B)$$

$$\angle EBC = \frac{\angle ABC}{2} = \frac{\angle B}{2} \text{ (EB bisects } \angle ABC)$$

$$\angle ECB = \angle ECA + \angle BCA$$

$$\angle ECB = \frac{\angle A + \angle B}{2} + 180^\circ - (\angle A + \angle B)$$

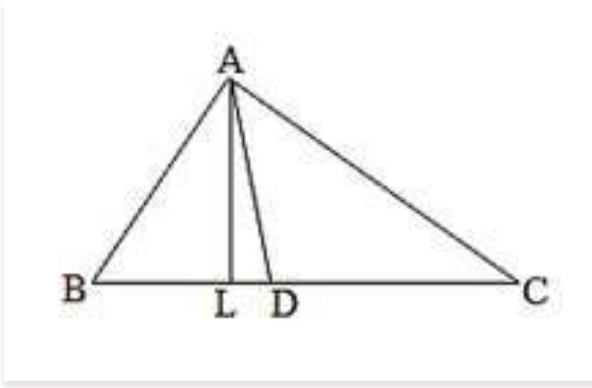
If we use the same logic for  $\triangle EBC$  , we can say that :

$$\angle EBC + \angle ECB + \angle BEC = 180^\circ \text{ (Sum of all angles of } \triangle EBC \text{ )}$$

$$\frac{\angle B}{2} + \frac{\angle A + \angle B}{2} + 180^\circ - (\angle A + \angle B) + \angle BEC = 180^\circ \quad \angle BEC = \angle A + \angle B - \left( \frac{\angle A + \angle B}{2} - \frac{\angle B}{2} \right)$$

$$\angle BEC = \frac{\angle A}{2} \quad \angle BEC = \frac{50^\circ}{2} = 25^\circ$$

**Q25.** In  $\triangle ABC$ ,  $\angle B = 60^\circ$ ,  $\angle C = 40^\circ$ ,  $AL$  perpendicular  $BC$  and  $AD$  bisects  $\angle A$  such that  $L$  and  $D$  lie on side  $BC$ . Find  $\angle LAD$



We know that the sum of all angles of a triangle is  $180^\circ$

Therefore, for  $\triangle ABC$ , we can say that :

$$\angle A + \angle B + \angle C = 180^\circ$$

Or,

$$\angle A + 60^\circ + 40^\circ = 180^\circ$$

$$\angle A = 80^\circ$$

$$\angle DAC = \frac{\angle A}{2} \quad (\text{AD bisects } \angle A)$$

$$\angle DAC = \frac{80^\circ}{2}$$

If we use the above logic on  $\triangle ADC$ , we can say that :

$$\angle ADC + \angle DCA + \angle DAC = 180^\circ \quad (\text{Sum of all the angles of } \triangle ADC)$$

$$\angle ADC + 40^\circ + 40^\circ = 180^\circ$$

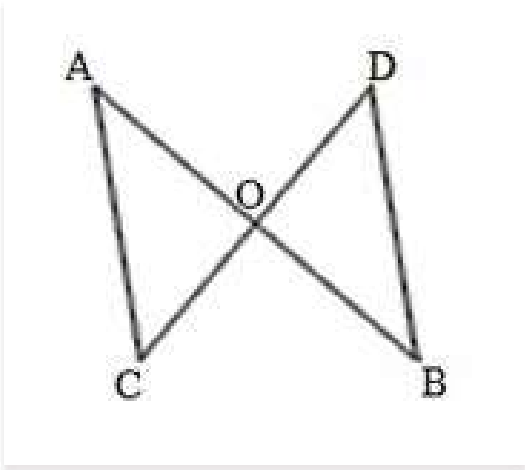
$$\angle ADC = 180^\circ - 80^\circ$$

$$\angle ADC = \angle ALD + \angle LAD \quad (\text{Exterior angle is equal to the sum of two Interior opposite angles.})$$

$$100^\circ = 90^\circ + \angle LAD \quad (\text{AL perpendicular to BC})$$

$$\angle LAD = 10^\circ$$

**Q26. Line segments AB and CD intersect at O such that AC perpendicular DB. If  $\angle CAB = 35^\circ$  and  $\angle CDB = 55^\circ$ . Find  $\angle BOD$ .**



We know that AC parallel to BD and AB cuts AC and BD at A and B, respectively.

$\angle CAB = \angle DBA$  (Alternate interior angles)

$\angle DBA = 35^\circ$

We also know that the sum of all three angles of a triangle is  $180^\circ$ .

Hence, for  $\triangle OBD$ , we can say that :

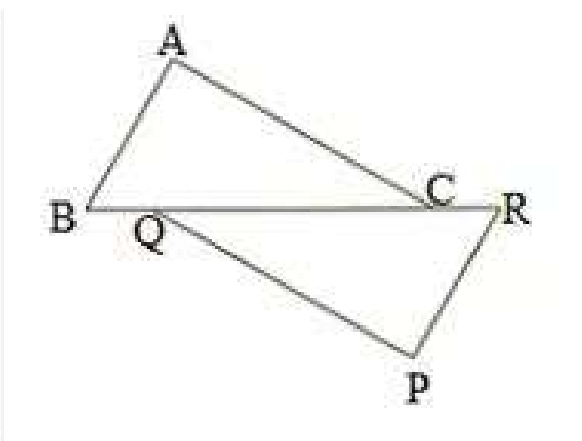
$\angle DBO + \angle ODB + \angle BOD = 180^\circ$

$35^\circ + 55^\circ + \angle BOD = 180^\circ$  ( $\angle DBO = \angle DBA$  and  $\angle ODB = \angle CDB$ )

$\angle BOD = 180^\circ - 90^\circ$

$\angle BOD = 90^\circ$

**Q27. In Fig. 22,  $\triangle ABC$  is right angled at A, Q and R are points on line BC and P is a point such that QP perpendicular to AC and RP perpendicular to AB. Find  $\angle P$**



In the given triangle, AC parallel to QP and BR cuts AC and QP at C and Q, respectively.

$\angle QCA = \angle CQP$  (Alternate interior angles)

Because RP parallel to AB and BR cuts AB and RP at B and R, respectively,

$\angle ABC = \angle PRQ$  (alternate interior angles).

We know that the sum of all three angles of a triangle is  $180^\circ$ .

Hence, for  $\triangle ABC$ , we can say that :

$$\angle ABC + \angle ACB + \angle BAC = 180^\circ$$

$$\angle ABC + \angle ACB + 90^\circ = 180^\circ \text{ (Right angled at A)}$$

$$\angle ABC + \angle ACB = 90^\circ$$

Using the same logic for  $\triangle PQR$ , we can say that :

$$\angle PQR + \angle PRQ + \angle QPR = 180^\circ$$

$$\angle ABC + \angle ACB + \angle QPR = 180^\circ \text{ (}\angle ABC = \angle PRQ \text{ and } \angle QCA = \angle CQP \text{)}$$

Or,

$$90^\circ + \angle QPR = 180^\circ \text{ (}\angle ABC + \angle ACB = 90^\circ \text{)}$$

$$\angle QPR = 90^\circ$$